

41. For the harmonic oscillator calculate $\langle 0|T(\hat{x}(t)\hat{x}(0))|0\rangle$.

42. In Minkowski space consider a scalar field with cubic self interaction

$$\mathcal{L} = \frac{1}{2}(\partial_\mu\phi)(\partial^\mu\phi) - \frac{1}{2}m^2\phi^2 - \frac{1}{3!}g\phi^3$$

and calculate $\frac{Z[J]}{Z[0]}$ to $O(g)$.

43. For the above model calculate $\langle 0|T(\hat{\phi}(x_1)\hat{\phi}(x_2))|0\rangle$ and $\langle 0|T(\hat{\phi}(x_1)\hat{\phi}(x_2)\hat{\phi}(x_3))|0\rangle$ to $O(g)$. Perform the Fourier transform to momentum space and give an interpretation in terms of Feynman diagrams.

44. For the above model calculate all terms of $\frac{Z[J]}{Z[0]}$ which are relevant for $\langle 0|T(\phi(x_1)\phi(x_2))|0\rangle$ and $\langle 0|T(\phi(x_1)\phi(x_2)\phi(x_3))|0\rangle$ to $O(g^2)$. Obtain these ground state expectation values and give an interpretation in terms of Feynman diagrams.