

PHENOMENOLOGY WITH MASSIVE NEUTRINOS IN 2022

Concha Gonzalez-Garcia

(ICREA U. Barcelona & YITP Stony Brook)

Nov 22, 2022, U. Vienna

OUTLINE

The confirmed picture: 3ν Lepton Flavour Parameters

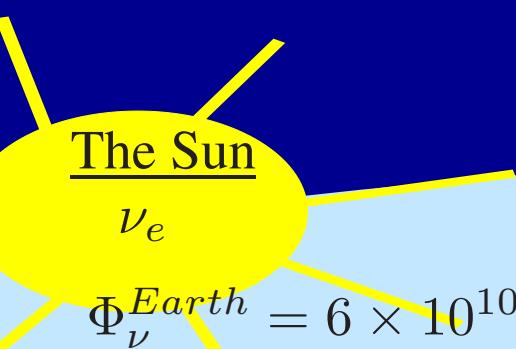
Some Q&A and some open avenues



<http://www.nu-fit.org>



Sources of ν 's



The Sun

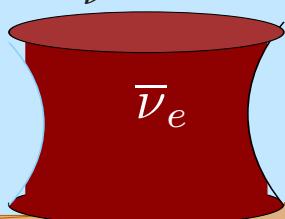
ν_e

$$\Phi_\nu^{Earth} = 6 \times 10^{10} \nu/cm^2 s$$

$$E_\nu \sim 0.1\text{--}20 \text{ MeV}$$

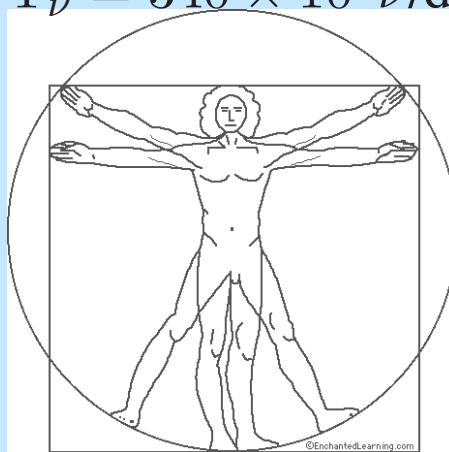
Nuclear Reactors

$$E_\nu \sim \text{few MeV}$$



$\bar{\nu}_e$

$$\frac{\text{Human Body}}{\Phi_\nu = 340 \times 10^6 \nu/\text{day}}$$



$$\frac{\text{Earth's radioactivity}}{\Phi_\nu \sim 6 \times 10^6 \nu/cm^2 s}$$

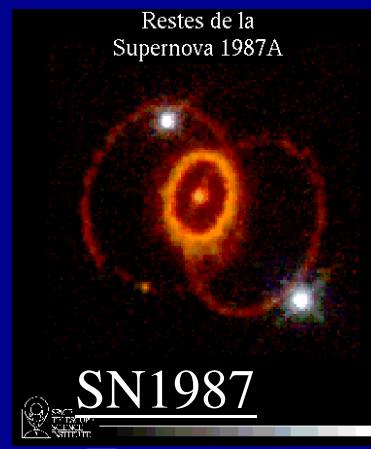


The Big Bang

$$\rho_\nu = 330/cm^3$$

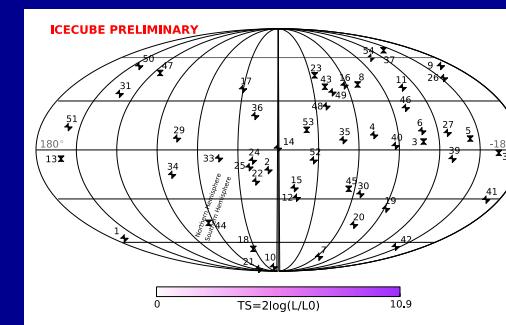
$$p_\nu = 0.0004 \text{ eV}$$

Restes de la Supernova 1987A



SN1987

$$E_\nu \sim \text{MeV}$$



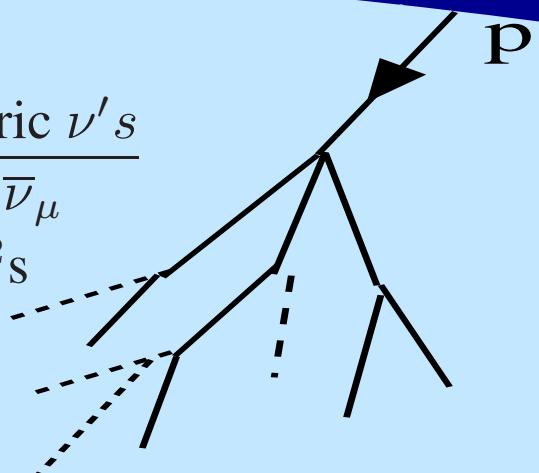
ExtraGalactic

$$E_\nu \gtrsim 30 \text{ TeV}$$

Atmospheric ν 's

$\nu_e, \nu_\mu, \bar{\nu}_e, \bar{\nu}_\mu$

$$\Phi_\nu \sim 1 \nu/cm^2 s$$



Accelerators

$$E_\nu \simeq 0.3\text{--}30 \text{ GeV}$$



Neutrinos in the Standard Model

The SM is a gauge theory based on the symmetry group

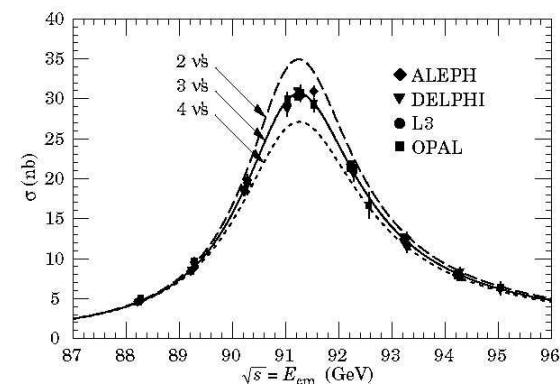
$$SU(3)_C \times SU(2)_L \times U(1)_Y \Rightarrow SU(3)_C \times U(1)_{EM}$$

With three generation of fermions

$(1, 2)_{-\frac{1}{2}}$	$(3, 2)_{\frac{1}{6}}$	$(1, 1)_{-1}$	$(3, 1)_{\frac{2}{3}}$	$(3, 1)_{-\frac{1}{3}}$
$\begin{pmatrix} \nu_e \\ e \end{pmatrix}_L$	$\begin{pmatrix} u^i \\ d^i \end{pmatrix}_L$	e_R	u_R^i	d_R^i
$\begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}_L$	$\begin{pmatrix} c^i \\ s^i \end{pmatrix}_L$	μ_R	c_R^i	s_R^i
$\begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}_L$	$\begin{pmatrix} t^i \\ b^i \end{pmatrix}_L$	τ_R	t_R^i	b_R^i

There is no ν_R

Three and only three



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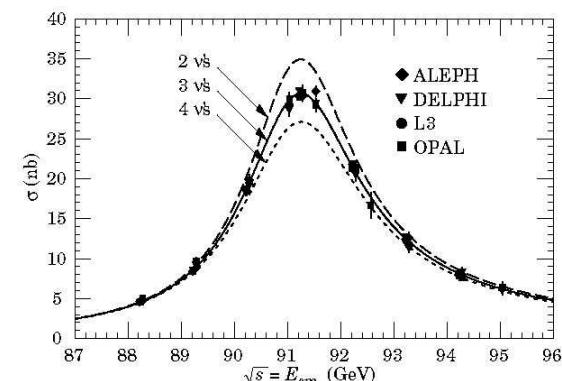


Accidental global symmetry: $B \times L_e \times L_\mu \times L_\tau$ (hence $L = L_e + L_\mu + L_\tau$)



ν strictly massless

Three and only three



- We have observed with high (or good) precision:
 - * Atmospheric ν_μ & $\bar{\nu}_\mu$ disappear most likely to ν_τ (**SK,MINOS, ICECUBE**)
 - * Accel. ν_μ & $\bar{\nu}_\mu$ disappear at $L \sim 300/800$ Km (**K2K, T2K, MINOS, NO ν A**)
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All this implies that L_α are violated

\Rightarrow There is Physics Beyond SM

- The *important* question:

What BSM?

- Today the *starting* path:

Precise determination of the low energy parametrization

The New Minimal Standard Model

- Minimal Extension to allow for LFV \Rightarrow give Mass to the Neutrino

- * Introduce ν_R AND impose L conservation \Rightarrow Dirac $\nu \neq \nu^c$:

$$\mathcal{L} = \mathcal{L}_{SM} - M_\nu \bar{\nu}_L \nu_R + h.c.$$

- * NOT impose L conservation \Rightarrow Majorana $\nu = \nu^c$

$$\mathcal{L} = \mathcal{L}_{SM} - \frac{1}{2} M_\nu \bar{\nu} \nu^C + h.c.$$

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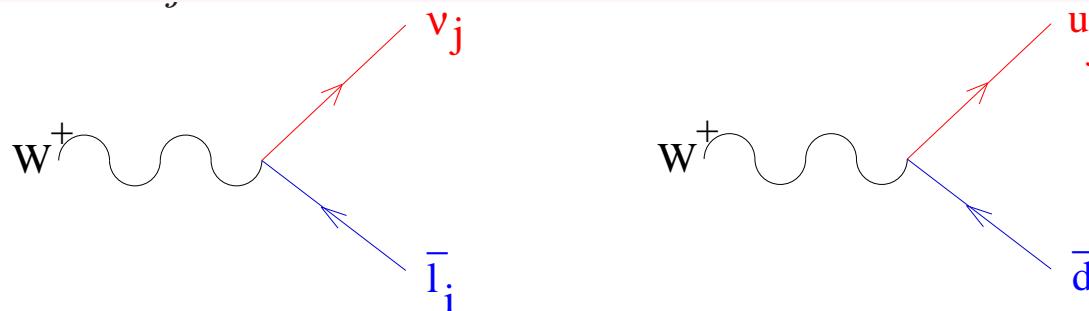
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- The charged current interactions of leptons are not diagonal (similar to quarks)

$$\frac{g}{\sqrt{2}} W_\mu^+ \sum_{i,j} (U_{\text{LEP}}^{ij} \bar{\ell}^i \gamma^\mu L \nu^j + U_{\text{CKM}}^{ij} \bar{U}^i \gamma^\mu L D^j) + h.c.$$



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- In general for $N = 3 + s$ massive neutrinos U_{LEP} is $3 \times N$ matrix

$$U_{\text{LEP}} U_{\text{LEP}}^\dagger = I_{3 \times 3} \quad \text{but in general} \quad U_{\text{LEP}}^\dagger U_{\text{LEP}} \neq I_{N \times N}$$

- U_{LEP} : $3 + 3s$ angles + $2s + 1$ Dirac phases + $s + 2$ Majorana phases

ν Mass Oscillations in Vacuum

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- If neutrinos have mass, a weak eigenstate $|\nu_\alpha\rangle$ produced in $l_\alpha + N \rightarrow \nu_\alpha + N'$

is a linear combination of the mass eigenstates ($|\nu_i\rangle$) : $|\nu_\alpha\rangle = \sum_{i=1}^n U_{\alpha i} |\nu_i\rangle$

- After a distance L it can be detected with flavour β with probability

$$P_{\alpha\beta} = \delta_{\alpha\beta} - 4 \sum_{j \neq i} \text{Re}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin^2 \left(\frac{\Delta_{ij}}{2} \right) + 2 \sum_{j \neq i} \text{Im}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin(\Delta_{ij})$$

$$\frac{\Delta_{ij}}{2} = \frac{(E_i - E_j)L}{2} = 1.27 \frac{(m_i^2 - m_j^2)}{\text{eV}^2} \frac{L/E}{\text{Km/GeV}}$$

No information on ν mass scale nor Majorana versus Dirac

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- When osc between 2-ν dominates:

$$P_{\alpha\alpha} = 1 - P_{osc} \quad \text{Disappear}$$

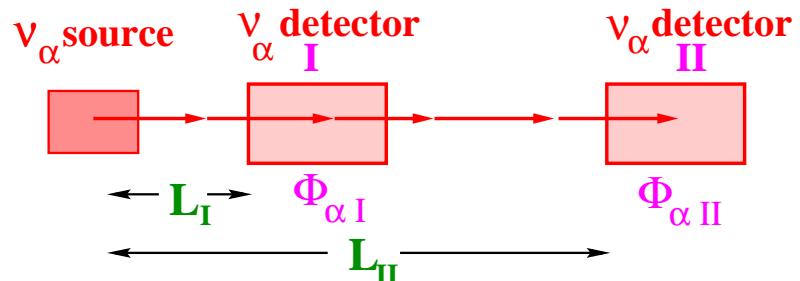
$$P_{osc} = \sin^2(2\theta) \sin^2 \left(1.27 \frac{\Delta m^2 L}{E} \right) \quad \text{Appear}$$

\Rightarrow No info on sign of Δm^2 and θ octant

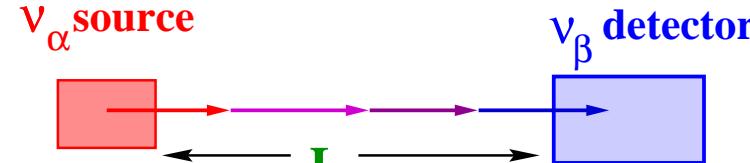
ν Oscillations: Experimental Probes

- Generically there are two types of experiments to search for ν oscillations :

Disappearance Experiment



Appearance Experiment

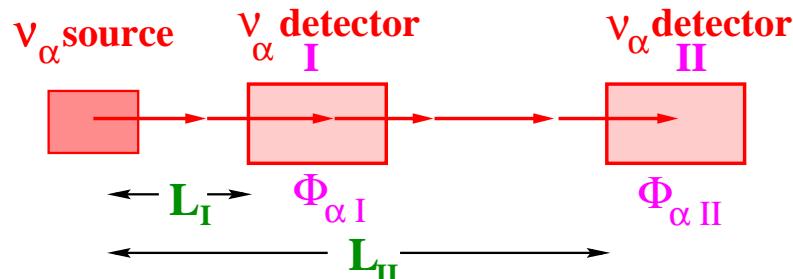


Compares $\Phi_{\alpha I}$ and $\Phi_{\alpha II}$ to look for loss

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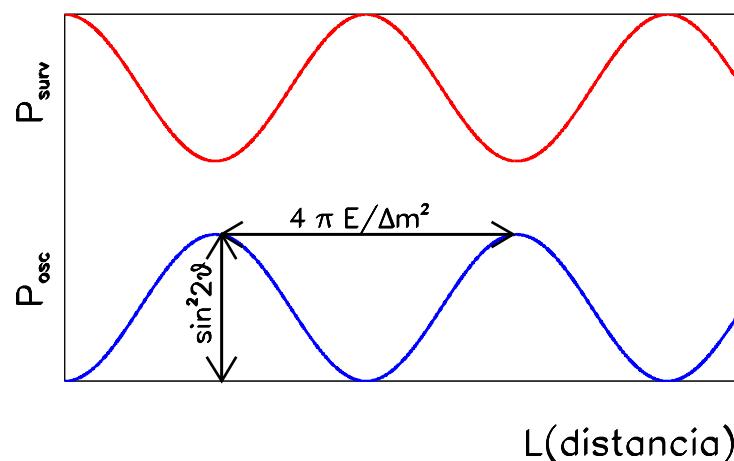
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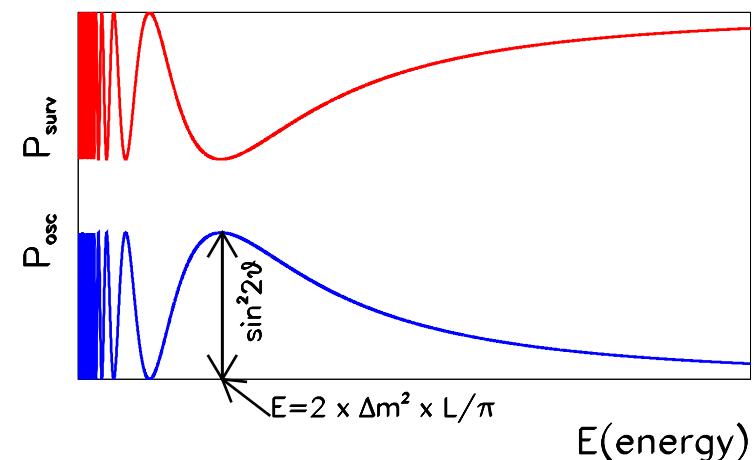
Searches for
 β diff α

Compares $\Phi_\alpha I$ and $\Phi_\alpha II$ to look for loss

- To detect oscillations we can study the neutrino flavour as function of the Distance to the source



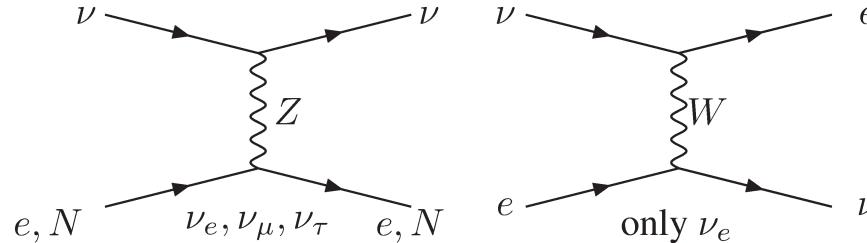
As function of the neutrino Energy



Matter Effects

- If ν cross matter regions (Sun, Earth...) it interacts *coherently*

- But Different flavours have different interactions :



\Rightarrow Effective potential in ν evolution : $V_e \neq V_{\mu, \tau} \Rightarrow \Delta V^\nu = -\Delta V^{\bar{\nu}} = \sqrt{2}G_F N_e$

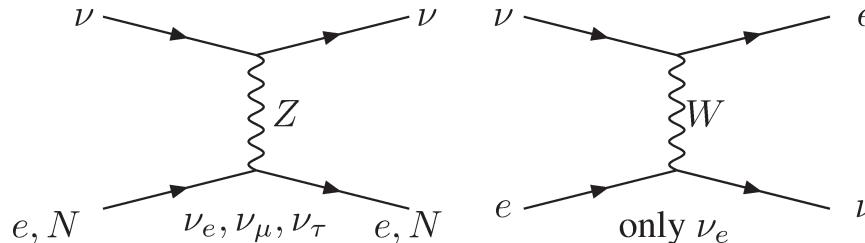
$$-i \frac{\partial}{\partial x} \begin{pmatrix} \nu_e \\ \nu_X \end{pmatrix} = \left[\begin{pmatrix} V_e - V_X - \frac{\Delta m^2}{4E} \cos 2\theta & \frac{\Delta m^2}{4E} \sin 2\theta \\ \frac{\Delta m^2}{4E} \sin 2\theta & V_X + \frac{\Delta m^2}{4E} \cos 2\theta \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_X \end{pmatrix}$$

\Rightarrow Modification of mixing angle and oscillation wavelength (MSW)

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- Mass difference and mixing in matter:

$$\Delta m_m^2 = \sqrt{(\Delta m^2 \cos 2\theta - 2E\Delta V)^2 + (\Delta m^2 \sin 2\theta)^2}$$

$$\sin(2\theta_m) = \frac{\Delta m^2 \sin(2\theta)}{\Delta m_{mat}^2}$$

\Rightarrow For solar ν' s in adiabatic regime

$$P_{ee} = \frac{1}{2} [1 + \cos(2\theta_m) \cos(2\theta)]$$

Dependence on θ octant

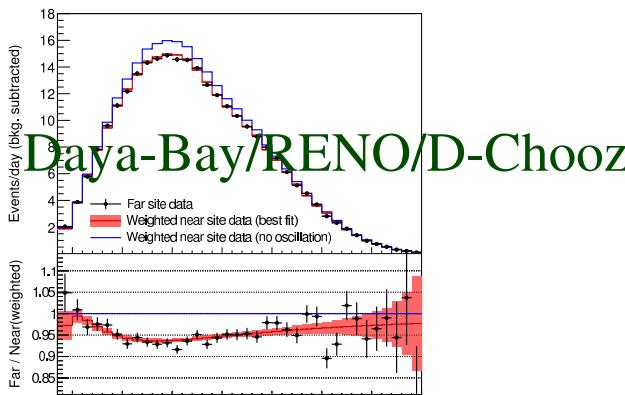
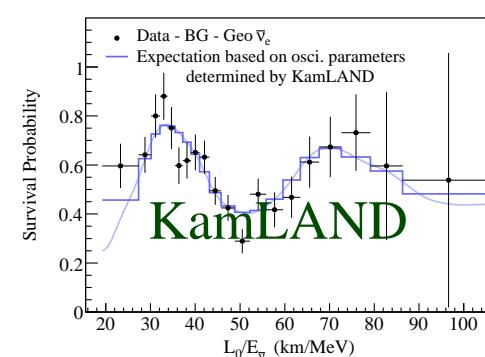
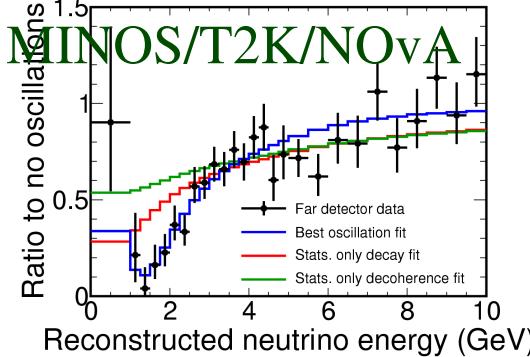
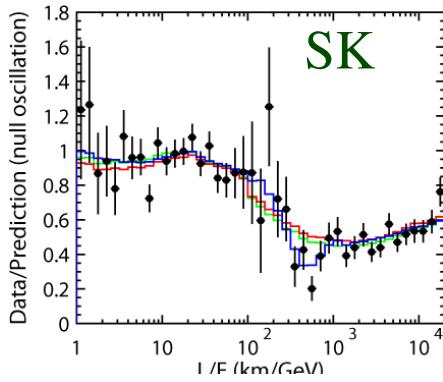
\Rightarrow In LBL terrestrial experiments

Dependence on sign of Δm^2 and θ octant

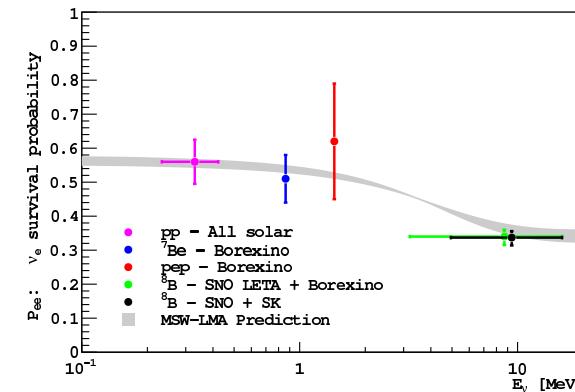
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Vacuum oscillation L/E pattern with 2 frequencies



MSW conversion in Sun



3 ν Flavour Parameters

Concha Gonzalez-Garcia 11

- For for 3 ν 's : 3 Mixing angles + 1 Dirac Phase + 2 Majorana Phases

$$U_{\text{LEP}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta_{\text{CP}}} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta_{\text{CP}}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{21} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\eta_1} & 0 & 0 \\ 0 & e^{i\eta_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

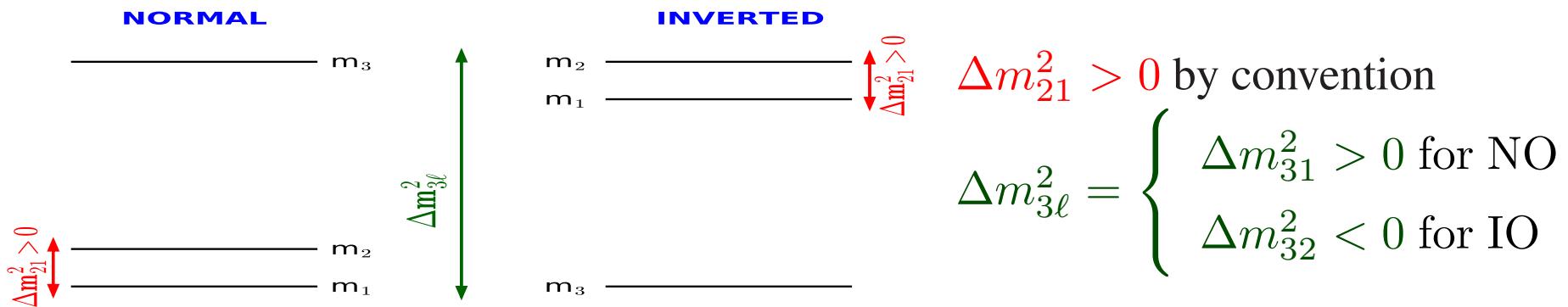
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Concha Gonzalez-Garcia 11-a

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- Convention: $0 \leq \theta_{ij} \leq 90^\circ$ $0 \leq \delta \leq 360^\circ \Rightarrow$ 2 Orderings



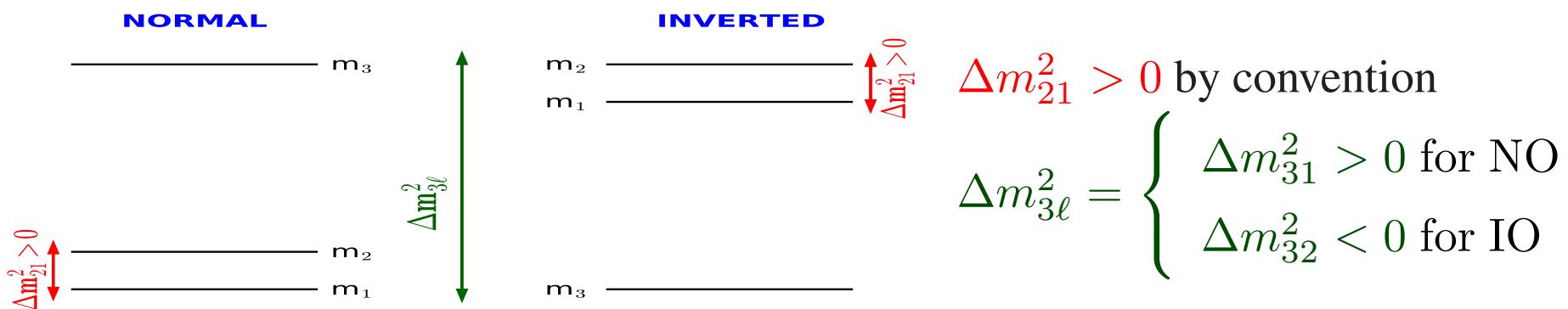
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Concha Gonzalez-Garcia 11-b

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Experiment	Dominant Dependence	Important Dependence
Solar Experiments	θ_{12}	$\Delta m_{21}^2, \theta_{13}$
Reactor LBL (KamLAND)	Δm_{21}^2	θ_{12}, θ_{13}
Reactor MBL (Daya Bay, Reno, D-Chooz)	$\theta_{13} \Delta m_{3\ell}^2$	
Atmospheric Experiments (SK, IC)		$\theta_{23}, \Delta m_{3\ell}^2, \theta_{13}, \delta_{\text{CP}}$
Acc LBL ν_μ Disapp (Minos, T2K, NOvA)	$\Delta m_{3\ell}^2 \theta_{23}$	
Acc LBL ν_e App (Minos, T2K, NOvA)	δ_{CP}	θ_{13}, θ_{23}

Data to be Described

Solar experiments

- Chlorine total rate, 1 data point.
- Gallex & GNO total rates, 2 points.
- SAGE total rate, 1 data point.
- SK1 E and zenith spect, 44 points.
- SK2 E and D/N spect, 33 points.
- SK3 E and D/N spect, 42 points.
- SK4 2970-day E spectrum and D/N asym, 24 points.
- SNO combined analysis, 7 points.
- Borexino Ph-I 740.7-day low-E spect 33 points.
- Borexino Ph-I 246-day high-E spect ,6 points.
- Borexino Ph-II 408-day low-E spect, 42 points.

Reactor experiments

- KamLAND DS1,DS2&DS3 spectra with Daya-Bay fluxes 69 points
- DChooz FD/ND ratios with 1276-day (FD) and 587-day (ND) exposures , 26 points.
- Daya-Bay 1958-day EH2/EH1 & EH3/EH1 ratios,52 points.
Missing new 3158 day spectra.
- Reno 2908-day FD/ND ratios 45 points.

Atmospheric experiments

- IceCube/DeepCore 3-year data, 64 points.
- *SK I-IV 328 and 372 kton-years (χ^2 table provided by SK).*
Missing SK-V (not table available yet).

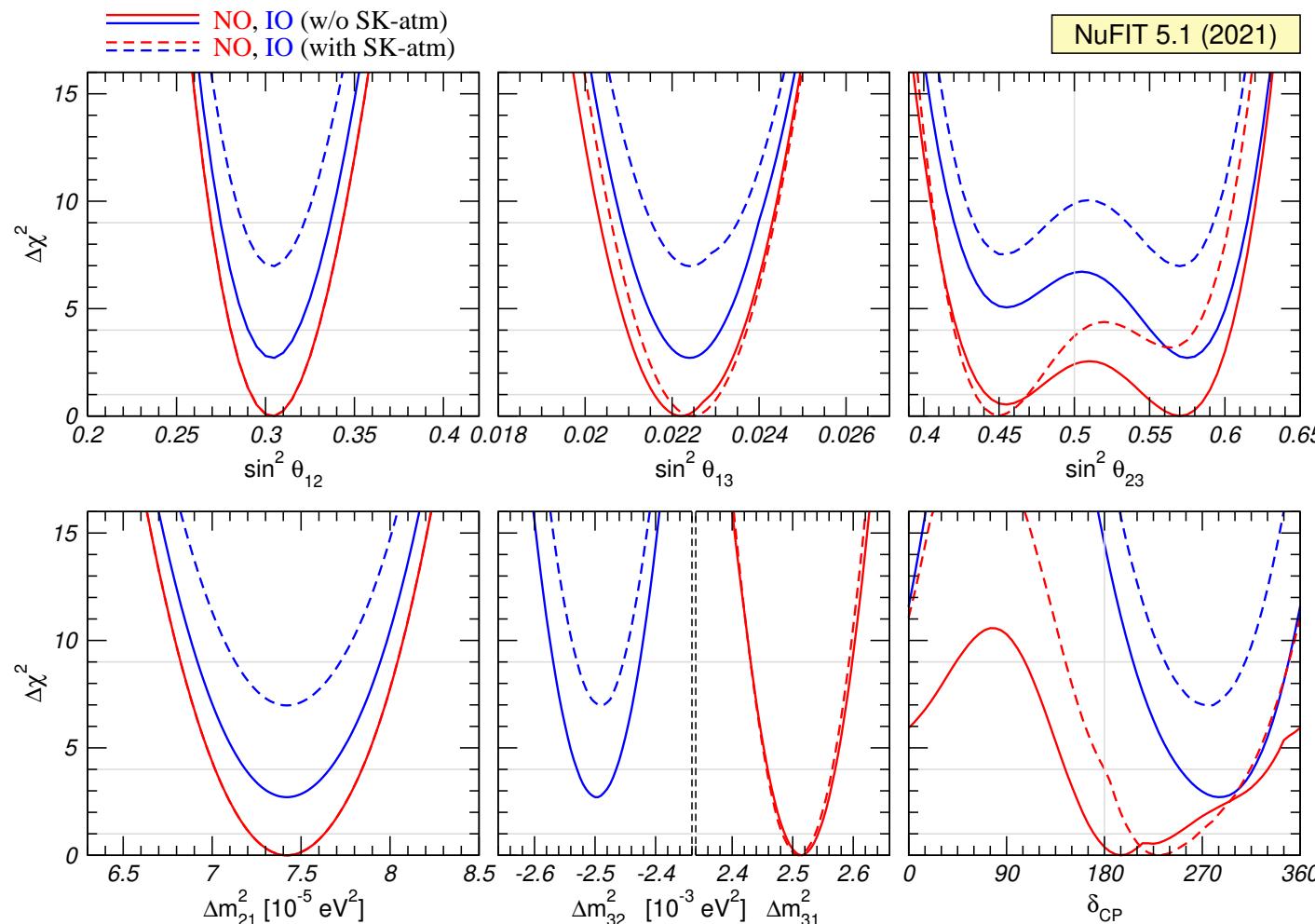
Accelerator experiments

- MINOS 10.71×10^{20} pot ν_μ -disapp data, 39 points.
- MINOS 3.36×10^{20} pot $\bar{\nu}_\mu$ -disapp data , 14 points.
- MINOS 10.6×10^{20} pot ν_e -app data , 5 points.
- MINOS 3.3×10^{20} pot $\bar{\nu}_e$ -app data , 5 points.
- T2K 19.7×10^{20} pot ν_μ -disapp data, 35 points.
- T2K 19.7×10^{20} pot ν_e -app data, 23 points CCQE and 16 points CC1 π .
- T2K 16.3×10^{20} pot $\bar{\nu}_\mu$ -disapp, 35 points.
- T2K 16.3×10^{20} pot $\bar{\nu}_e$ -app, 23 points.
- NO ν A 13.6×10^{20} pot ν_μ -disapp data , 76 points.
- NO ν A 13.6×10^{20} pot ν_e -app data , 13 points.
- NO ν A 12.5×10^{20} pot $\bar{\nu}_\mu$ -disapp, 76 points.
- NO ν A 12.5×10^{20} pot $\bar{\nu}_e$ -app, 13 points.

Summary: Global 3 ν Flavour Parameters

Global 6-parameter fit <http://www.nu-fit.org>

Esteban, G-G, Maltoni, Schwetz, Zhou, JHEP'20 [2007.14792], G-G, Maltoni, Schwetz, 2111.03086



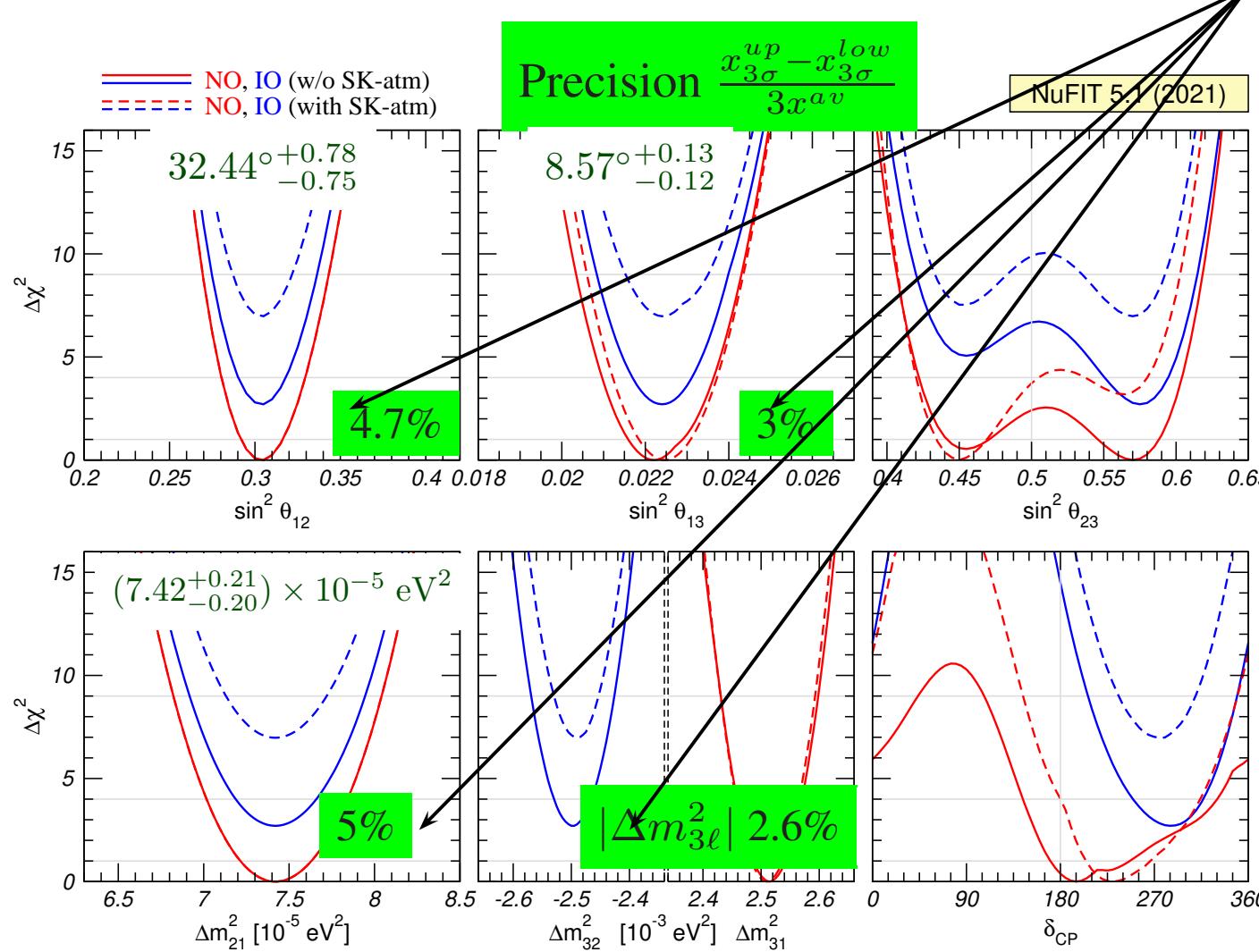
SK-atm $\equiv \chi^2$ table from
SK1-4 for 372 kton-years

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Esteban, G-G, Maltoni, Schwetz, Zhou, JHEP'20 [2007.14792], G-G, Maltoni, Schwetz, 2111.03086

- 4 well-known parameters:
 $\theta_{12}, \theta_{13}, \Delta m_{21}^2, |\Delta m_{3\ell}^2|$



Summary: Global 3 ν Flavour Parameters

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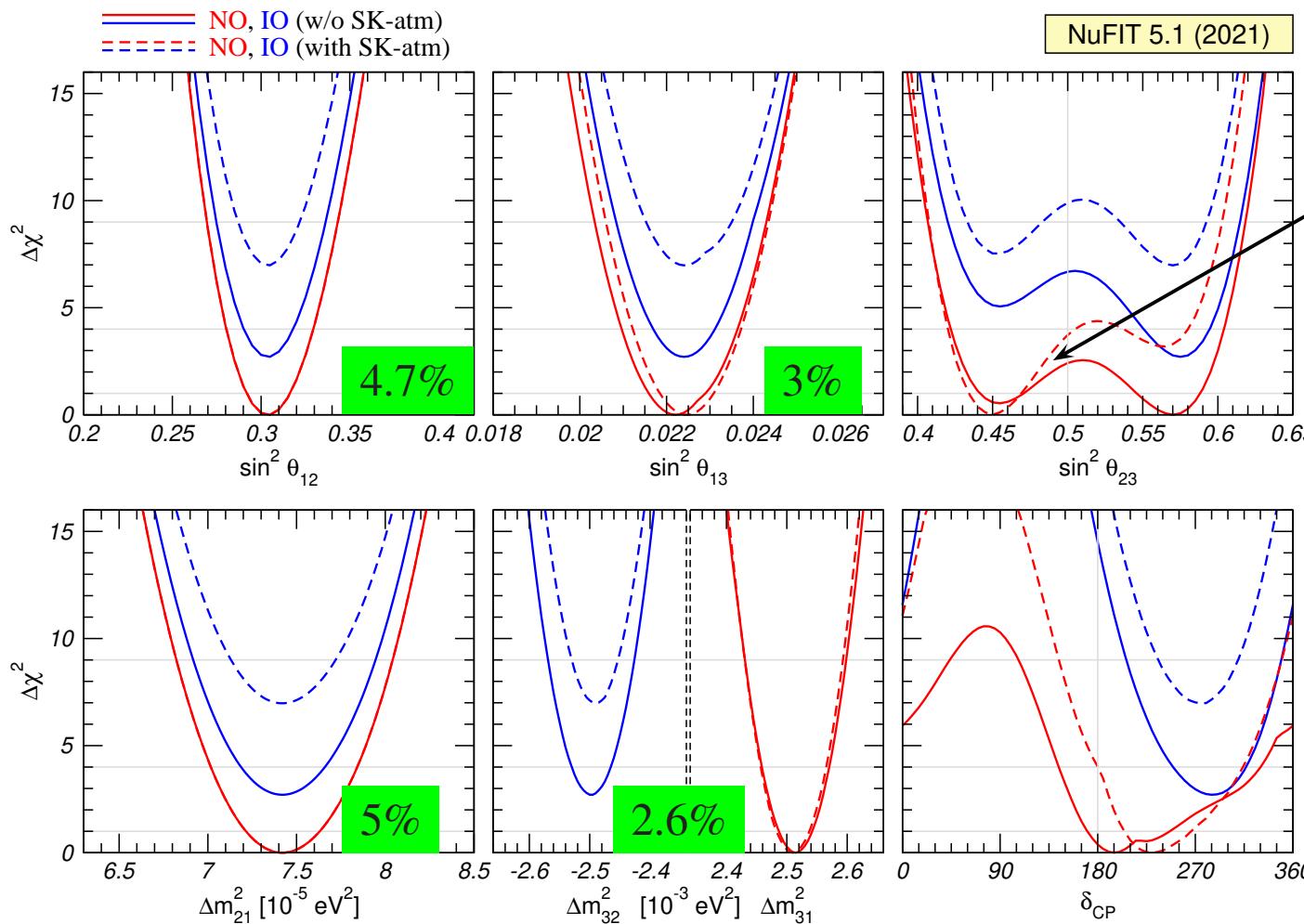
- 4 well-known parameters:

$$\theta_{12}, \theta_{13}, \Delta m_{21}^2, |\Delta m_{3\ell}^2|$$

Δm_{21}^2 Solar vs KLAND

Tension Resolved

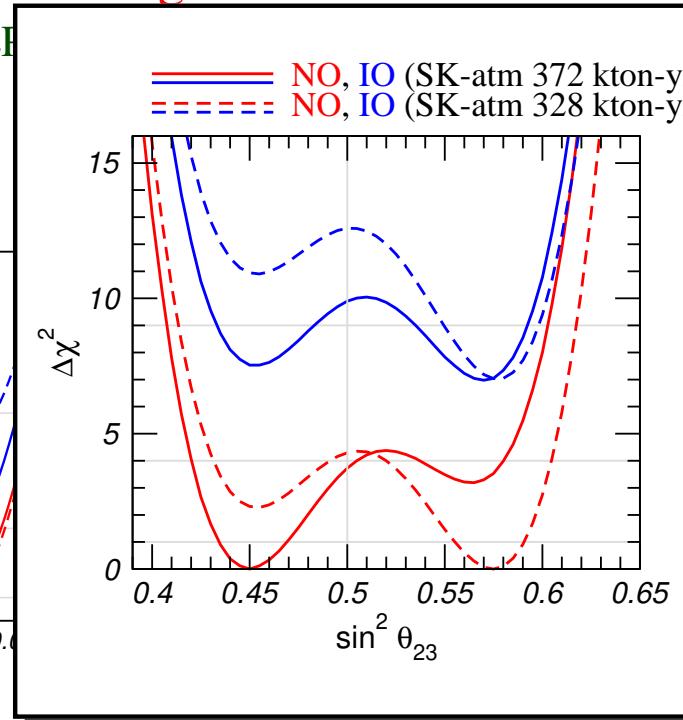
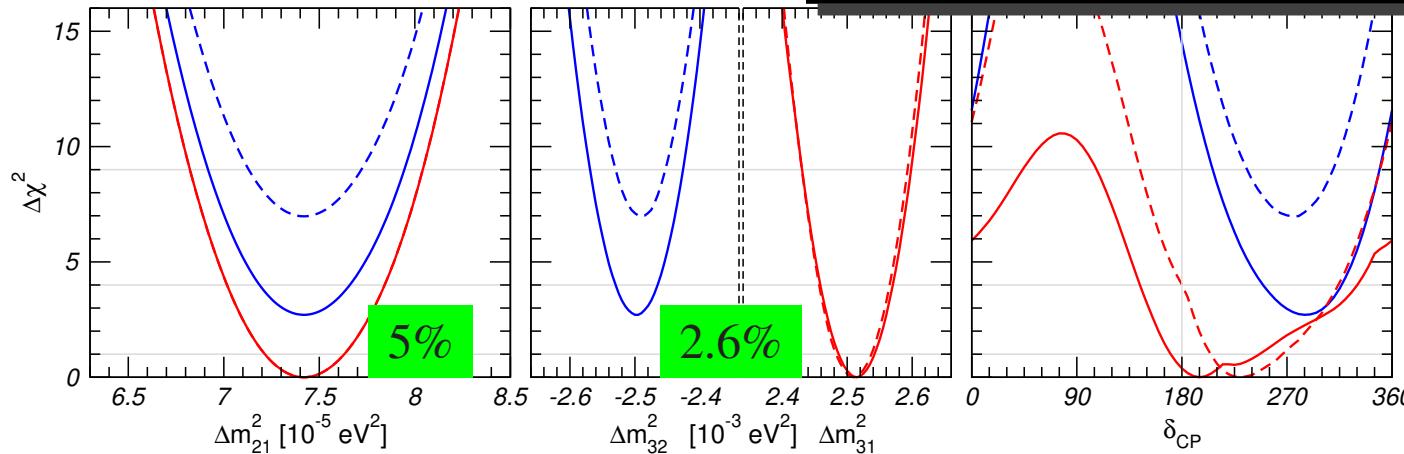
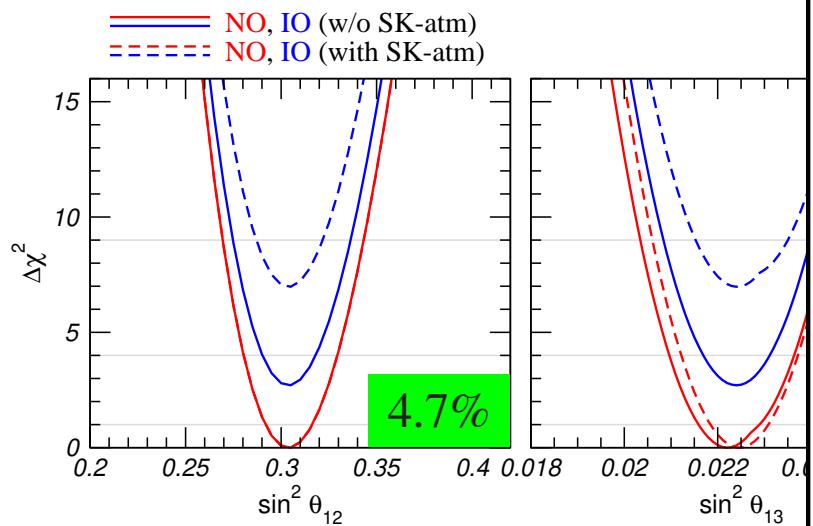
- θ_{23} : Least known angle
Maximal? Octant?
non-robust wrt ATM



Summary: Global 3 ν Flavour Parameters

Global 6-parameter fit <http://www.nu-fit.org>

Esteban, G-G, Maltoni, Schwetz, Zhou, JHEP



arXiv:1211.03086
All-known parameters:
 $\sin^2 \theta_{13}$, Δm^2_{21} , $|\Delta m^2_{3\ell}|$
Solar vs KLAND
on Resolved
Least known angle
Normal? Octant?
Robust wrt ATM

Summary: Global 3 ν Flavour Parameters

Global 6-parameter fit <http://www.nu-fit.org>

Esteban, G-G, Maltoni, Schwetz, Zhou, JHEP'20 [2007.14792], G-G, Maltoni, Schwetz, 2111.03086

- 4 well-known parameters:

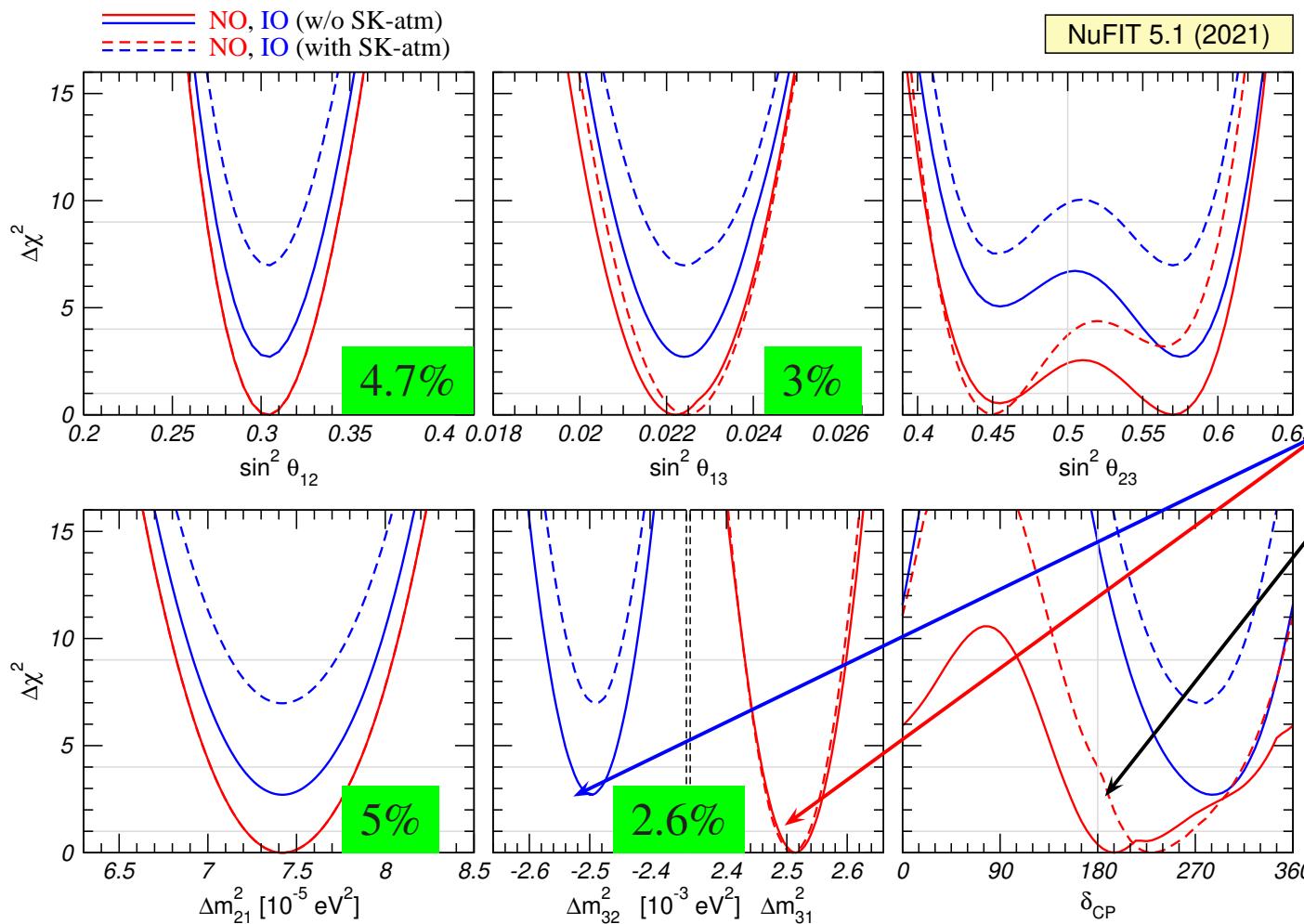
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Δm_{21}^2 Solar vs KLAND

Tension Resolved

- θ_{23} : Least known angle
Maximal? Octant?
non-robust wrt ATM
- Ordering NO or IO?

CPV?:



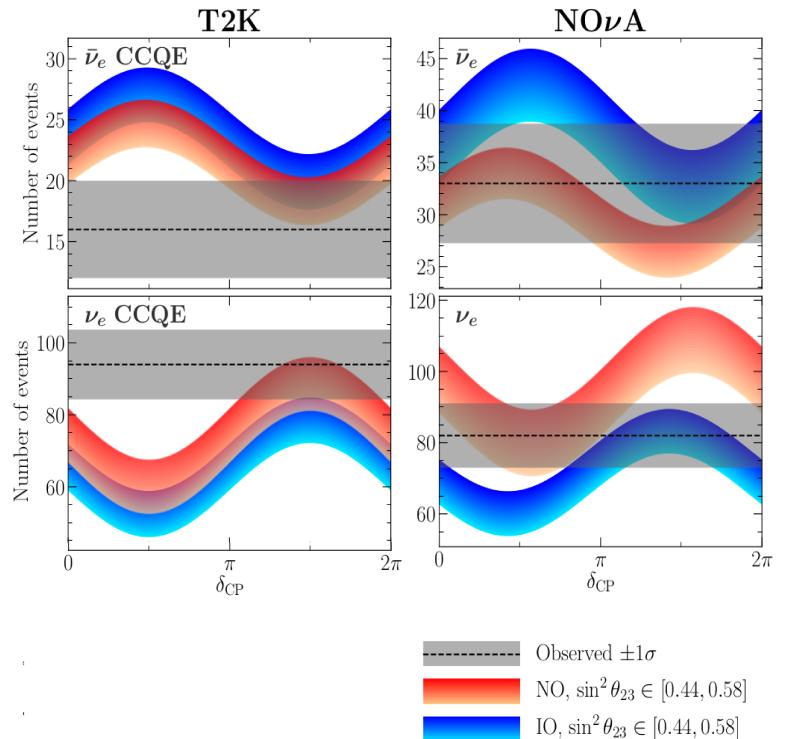
CPV and Ordering in LBL: ν_e appearace

lez-Garcia 17

- Dominant information from ν_e apperance in LBL

$$P_{\mu e} \simeq s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{31}}{B_{\mp}} \right)^2 \sin^2 \left(\frac{B_{\mp} L}{2} \right) + \tilde{J} \frac{\Delta_{21}}{V_E} \frac{\Delta_{31}}{B_{\mp}} \sin \left(\frac{V_E L}{2} \right) \sin \left(\frac{B_{\mp} L}{2} \right) \cos \left(\frac{\Delta_{31} L}{2} \pm \delta_{CP} \right)$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2}{4E} \quad B_{\pm} = \Delta_{31} \pm V_E \quad \tilde{J} = c_{13} \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 2\theta_{12}$$



\Rightarrow Each T2K and NO ν A favour **NO**

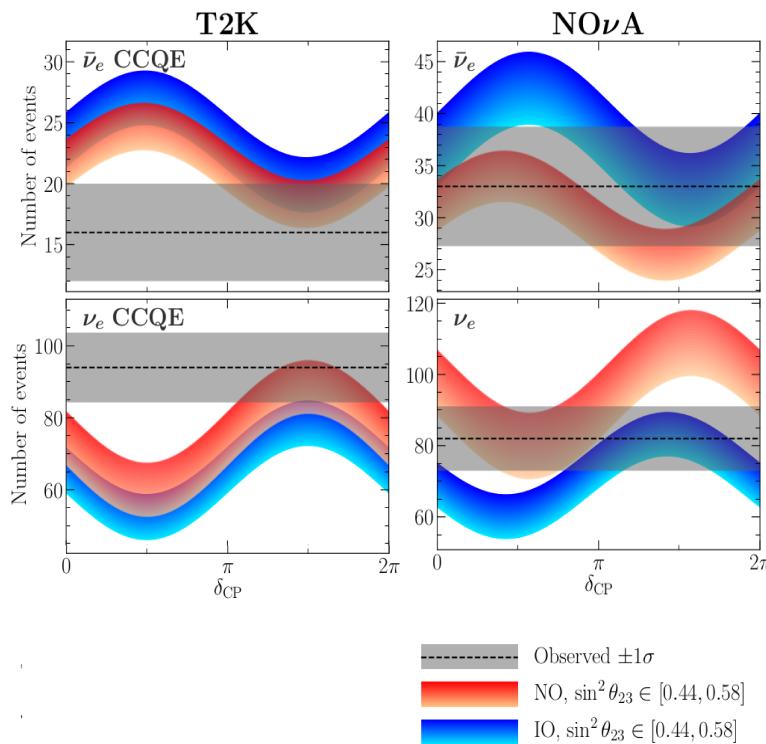
CPV and Ordering in LBL: ν_e appearace

z-Garcia 17-a

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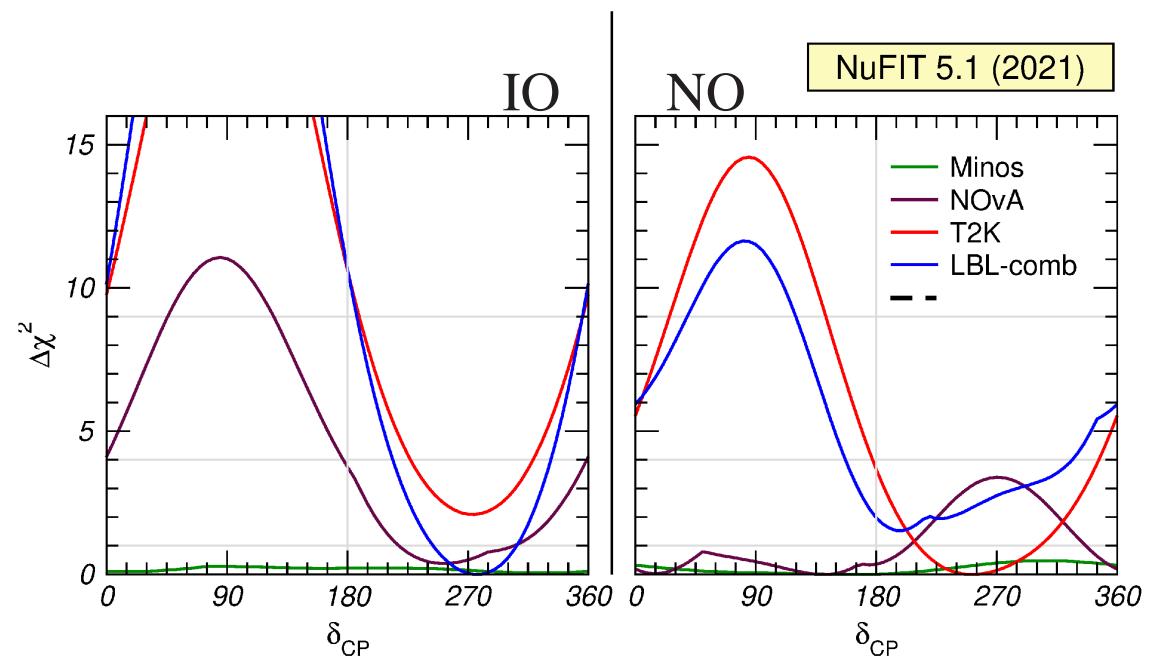
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⇒ Each T2K and NO ν A favour **NO**

But tension in favoured values of δ_{CP} in NO



⇒ IO best fit in LBL combination

Δm_{3l}^2 in LBL & Reactors

- At LBL determined in ν_μ and $\bar{\nu}_\mu$ disappearance spectrum

$$\Delta m_{\mu\mu}^2 \simeq \Delta m_{3l}^2 + \frac{c_{12}^2 \Delta m_{21}^2}{s_{12}^2 \Delta m_{21}^2} \begin{matrix} \text{NO} \\ \text{IO} \end{matrix} + \dots$$

- At MBL Reactors (Daya-Bay, Reno, D-Chooz) determined in $\bar{\nu}_e$ disapp spectrum

$$\Delta m_{ee}^2 \simeq \Delta m_{3l}^2 + \frac{s_{12}^2 \Delta m_{21}^2}{c_{12}^2 \Delta m_{21}^2} \begin{matrix} \text{NO} \\ \text{IO} \end{matrix} \quad \text{Nunokawa,Parke,Zukanovich (2005)}$$

\Rightarrow Contribution to NO/IO from combination of LBL with reactor data

Δm_{3l}^2 in LBL & Reactors

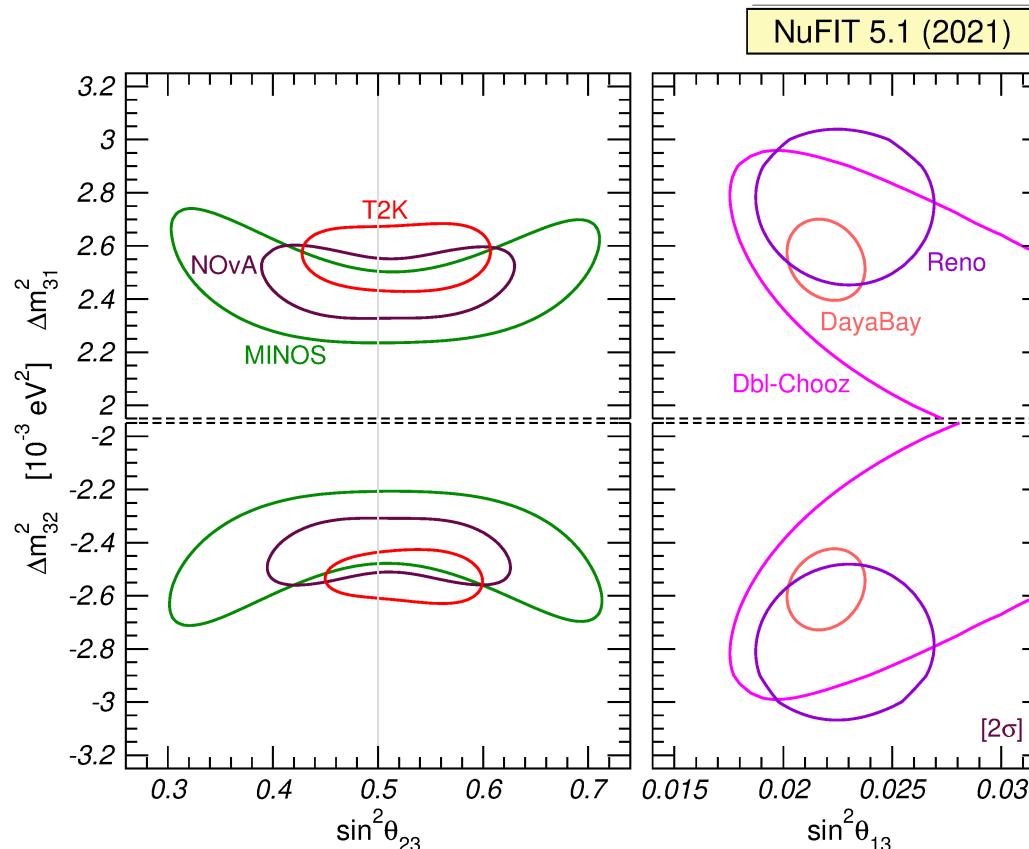
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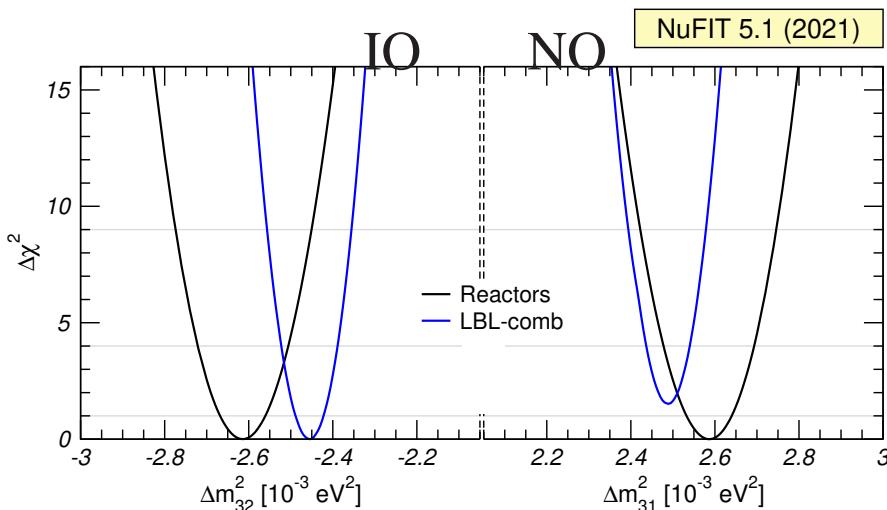
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- T2K and NO ν A more compatible in IO \Rightarrow IO best fit in LBL combination
- LBL/Reactor complementarity in Δm_{3l}^2 \Rightarrow NO best fit in LBL+Reactors

Δm_{3l}^2 in LBL & Reactors

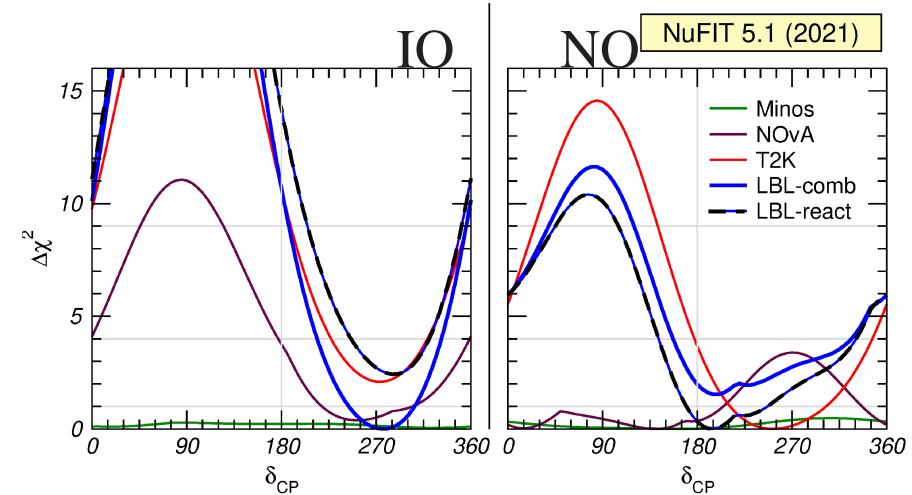
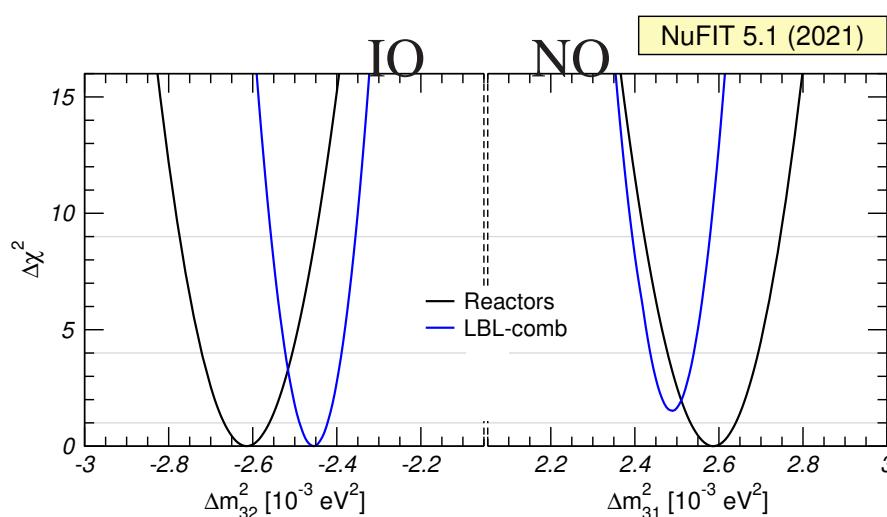
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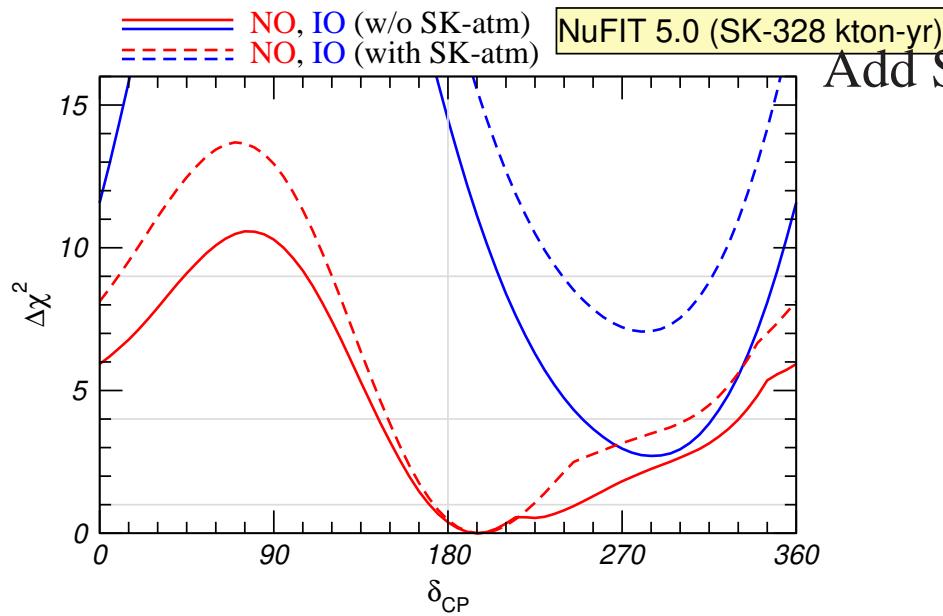


- T2K and NO ν A more compatible in IO \Rightarrow IO best fit in LBL combination
- LBL/Reactor complementarity in Δm_{3l}^2 \Rightarrow NO best fit in LBL+Reactors
- in NO: b.f $\delta_{CP} = 195^\circ$ \Rightarrow CPC allowed at 0.6σ
- in IO: b.f $\delta_{CP} \sim 270^\circ$ \Rightarrow CPC disfavoured at 3σ

Ordering and CPV including ATM

ATM results added to global fit using SK χ^2 tables

- NUFIT 5.0: included SK I-IV 328 kton-years table
- NUFIT 5.1: include SK I-IV 372.8 kton-years table



Add SK-atm table \Rightarrow favouring of NO:

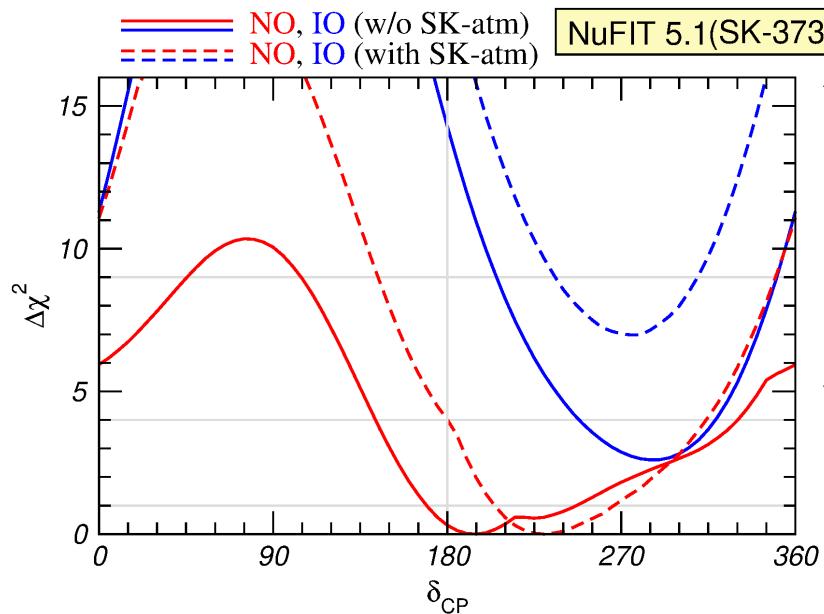
$$\Delta\chi^2_{NO-IO, w/o SK-atm} = 2.7$$

$$\Delta\chi^2_{NO-IO, with SK-atm} = 7.1$$

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- NUFIT 5.1: include SK I-IV 372.8 kton-years table



Add either SK-atm table \Rightarrow favouring of NO:

$$\Delta\chi^2_{\text{NO-IO, w/o SK-atm}} = 2.7$$

$$\Delta\chi^2_{\text{NO-IO, with SK-atm}} = 7.1$$

Add new table \Rightarrow slight increase of significance of CPV in NO

w/o SK-Atm b.f $\delta_{\text{CP}} = 195^\circ$ CPC at 0.6σ

with SK-Atm: b.f $\delta_{\text{CP}} = 230^\circ$ CPC at 2σ

Flavour Parameters: Mixing Matrix

- We have the three leptonic mixing angles determined (at $\pm 3\sigma/6$)

$$|U|_{3\sigma} = \begin{pmatrix} 0.801 \rightarrow 0.844 & 0.513 \rightarrow 0.579 & 0.143 \rightarrow 0.156 \\ 0.233 \rightarrow 0.507 & 0.461 \rightarrow 0.694 & 0.639 \rightarrow 0.778 \\ 0.261 \rightarrow 0.526 & 0.471 \rightarrow 0.701 & 0.611 \rightarrow 0.761 \end{pmatrix}$$

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- Good progress but still precision very far from:

$$|V|_{\text{CKM}} = \begin{pmatrix} 0.97427 \pm 0.00015 & 0.22534 \pm 0.0065 & (3.51 \pm 0.15) \times 10^{-3} \\ 0.2252 \pm 0.00065 & 0.97344 \pm 0.00016 & (41.2^{+1.1}_{-5}) \times 10^{-3} \\ (8.67^{+0.29}_{-0.31}) \times 10^{-3} & (40.4^{+1.1}_{-0.5}) \times 10^{-3} & 0.999146^{+0.000021}_{-0.000046} \end{pmatrix}$$

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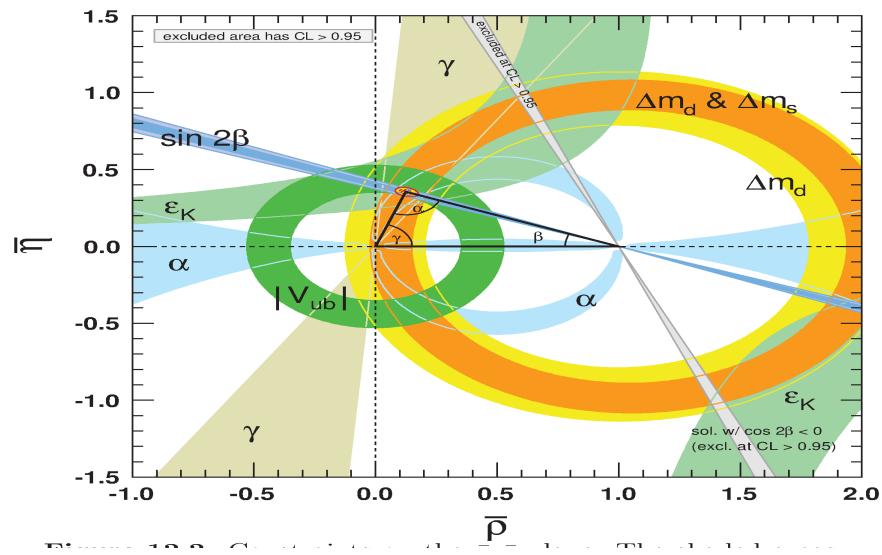
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- Also very different flavour mixing of leptons vs quarks

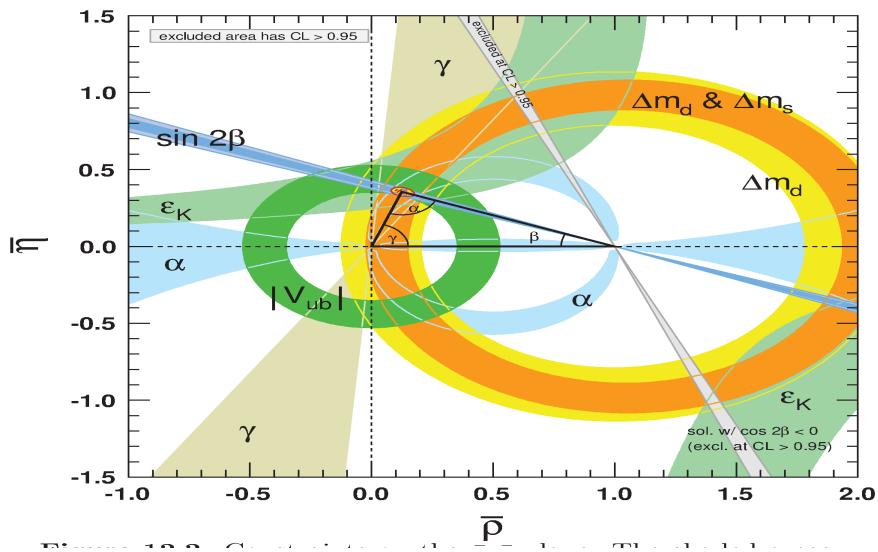
3ν Mixing: Leptonic Unitarity Triangle

Unitarity triangle in quark sector

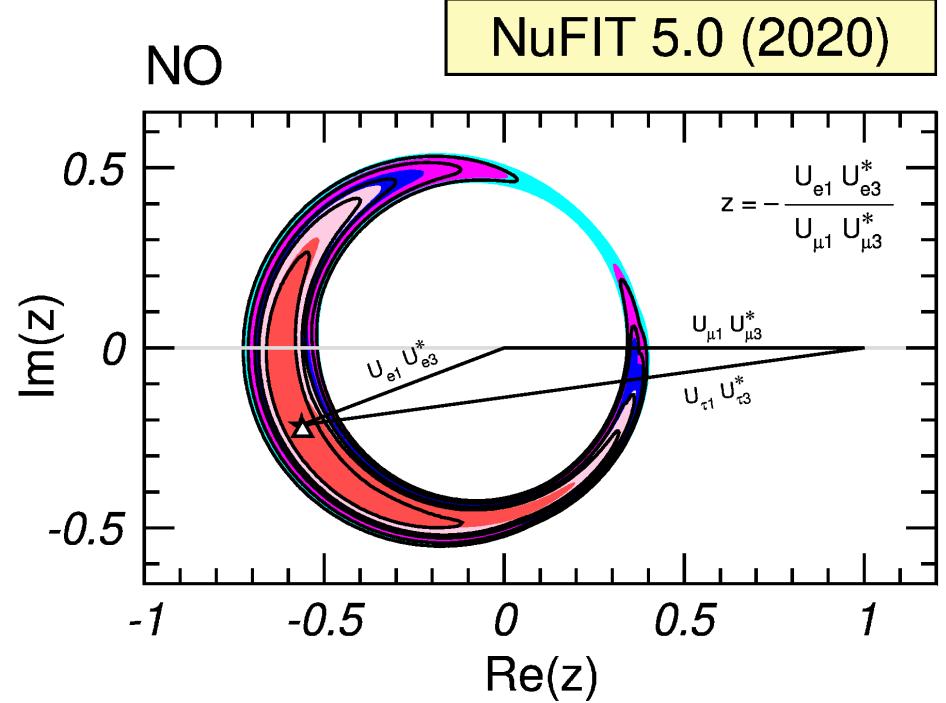


3 ν Mixing: Leptonic Unitarity Triangle

Unitarity triangle in quark sector



The equivalent in the leptonic sector



Near Future for CP and Ordering: Strategies

- $\nu/\bar{\nu}$ comparison with or without Earth matter effects in $\nu_\mu \rightarrow \nu_e$ & $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ at LBL:
DUNE (wide band beam, L=1300 km), HK (narrow band beam, L=300 km)

$$P_{\mu e} \simeq s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{31}}{\Delta_{31} \pm V} \right)^2 \sin^2 \left(\frac{\Delta_{31} \pm V L}{2} \right) + 8 J_{CP}^{\max} \frac{\Delta_{12}}{V} \frac{\Delta_{31}}{\Delta_{31} \pm V} \sin \left(\frac{VL}{2} \right) \sin \left(\frac{\Delta_{31} \pm VL}{2} \right) \cos \left(\frac{\Delta_{31} L}{2} \pm \delta_{CP} \right)$$

$$J_{CP}^{\max} = c_{13}^2 s_{13} c_{23} s_{23} c_{12} s_{12}$$

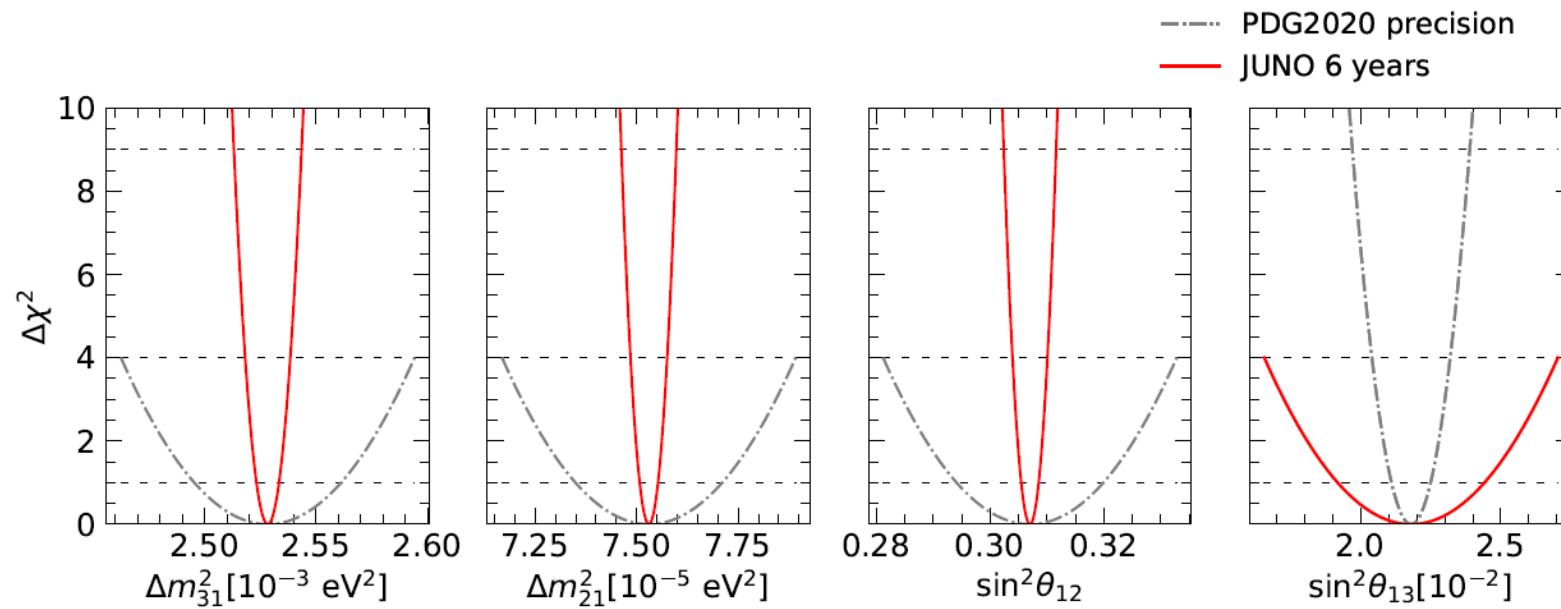
- Challenge: Parameter degeneracies, Normalization uncertainty, E_ν reconstruction
- Earth matter effects in large statistics ATM ν_μ disapp : HK, INO, PINGU, ORCA ...
– Challenge: ATM flux contains both ν_μ and $\bar{\nu}_\mu$, ATM flux uncertainties
- Reactor experiment at $L \sim 60$ km (vacuum) able to observe
the difference between oscillations with Δm_{31}^2 and Δm_{32}^2 : JUNO, RENO-50

$$P_{\nu_e, \nu_e} = 1 - c_{13}^4 \sin^2 2\theta_{12} \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E} \right) - \sin^2 2\theta_{13} \left[c_{12}^2 \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right) + s_{12}^2 \sin^2 \left(\frac{\Delta m_{32}^2 L}{4E} \right) \right]$$

- Challenge: Energy resolution

JUNO: Sensitivity to Oscillation Parameters

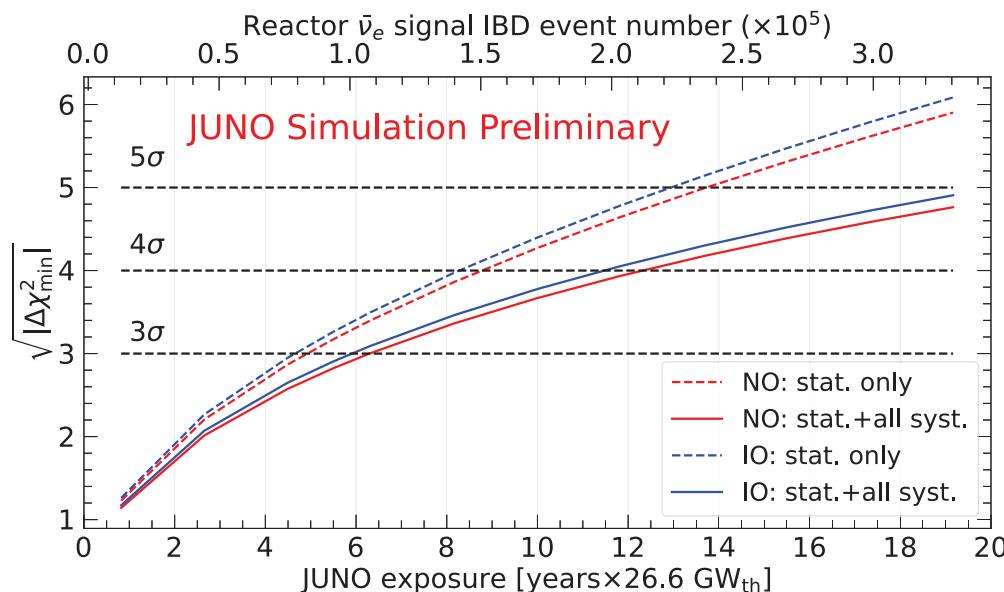
	Central Value	PDG2020	100 days	6 years	20 years
$\Delta m_{31}^2 (\times 10^{-3} \text{ eV}^2)$	2.5283	± 0.034 (1.3%)	± 0.021 (0.8%)	± 0.0047 (0.2%)	± 0.0029 (0.1%)
$\Delta m_{21}^2 (\times 10^{-5} \text{ eV}^2)$	7.53	± 0.18 (2.4%)	± 0.074 (1.0%)	± 0.024 (0.3%)	± 0.017 (0.2%)
$\sin^2 \theta_{12}$	0.307	± 0.013 (4.2%)	± 0.0058 (1.9%)	± 0.0016 (0.5%)	± 0.0010 (0.3%)
$\sin^2 \theta_{13}$	0.0218	± 0.0007 (3.2%)	± 0.010 (47.9%)	± 0.0026 (12.1%)	± 0.0016 (7.3%)



2204.13249

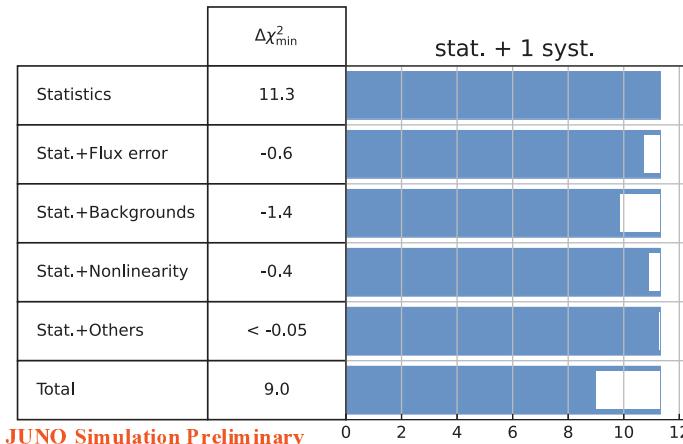


SENSITIVITY TO NEUTRINO MASS ORDERING



- ✓ JUNO+TAO, 6 years $\times 26.6$ GW exposure: $\sim 3\sigma$
- ✓ +1% external constrain on Δm_{32}^2 : $> 4\sigma$
- ✓ combined with accelerator/atmospheric experiment: $> 5\sigma$
→ sensitivity boost due to tension for wrong ordering

Impact of systematics:



- Paper under preparation.
- Combination of reactor and atmospheric channels within JUNO is investigated.

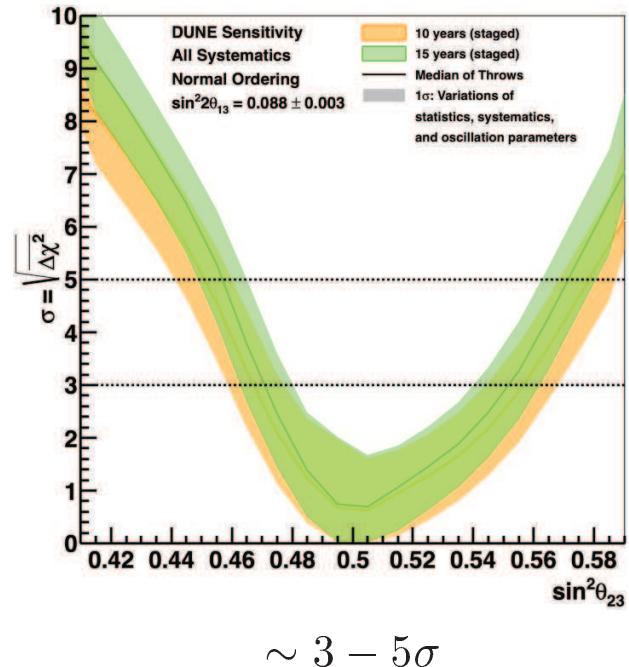
▶ Extra

[2008.11280], JUNO+IceCube [1911.06745]

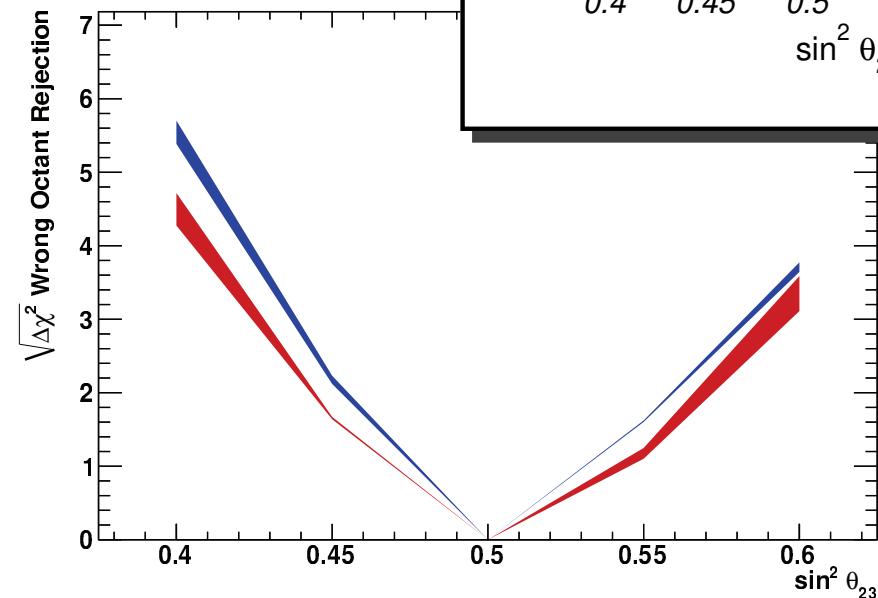


DUNE & Hyper-Kamiokande: θ_{23}

θ_{23} octant: future sensitivities



DUNE 2002.03005

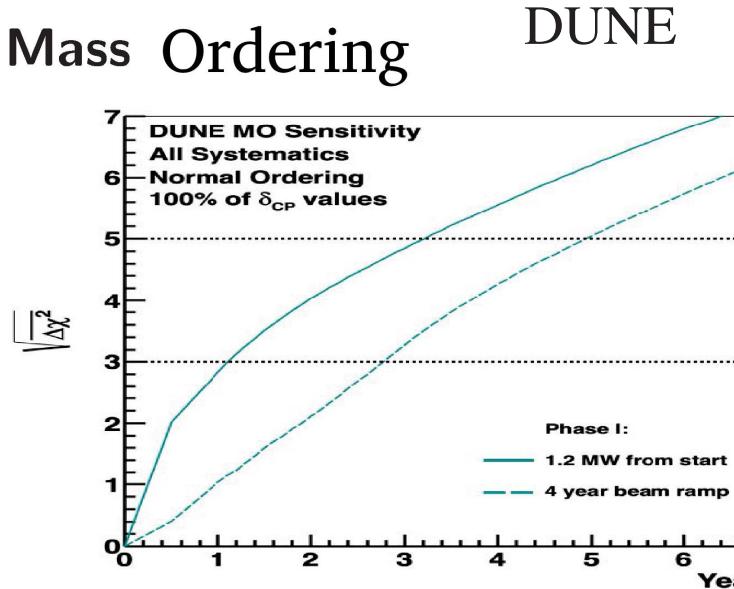


Beam+Atm $\Rightarrow \sim 3 - 6\sigma$

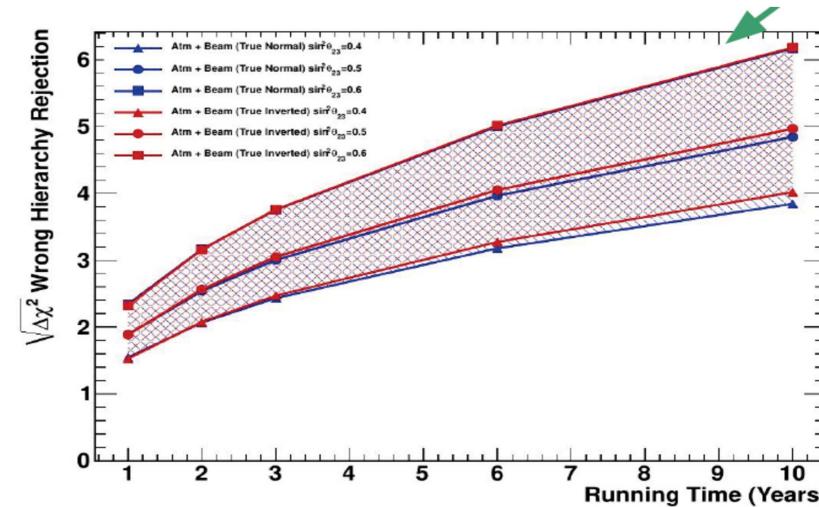
HK 1805.04163

DUNE & Hyper-Kamiokande: CPV and MO

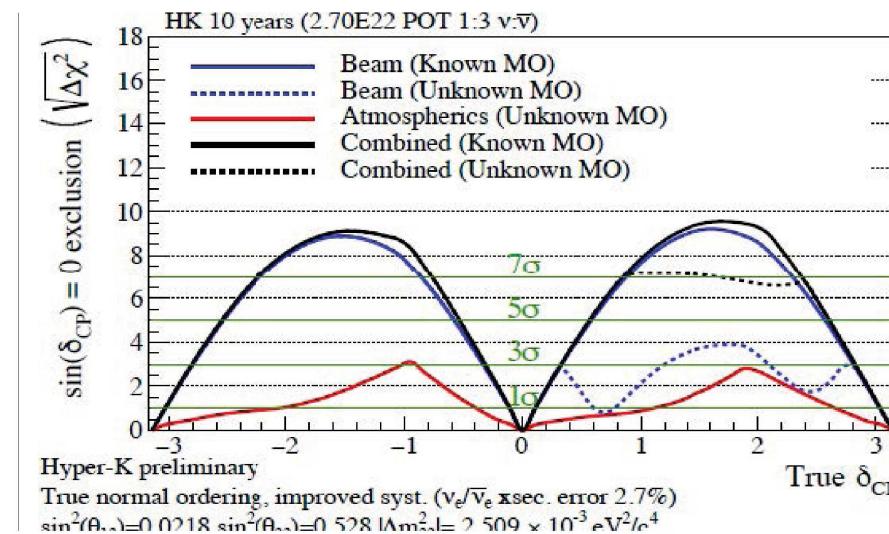
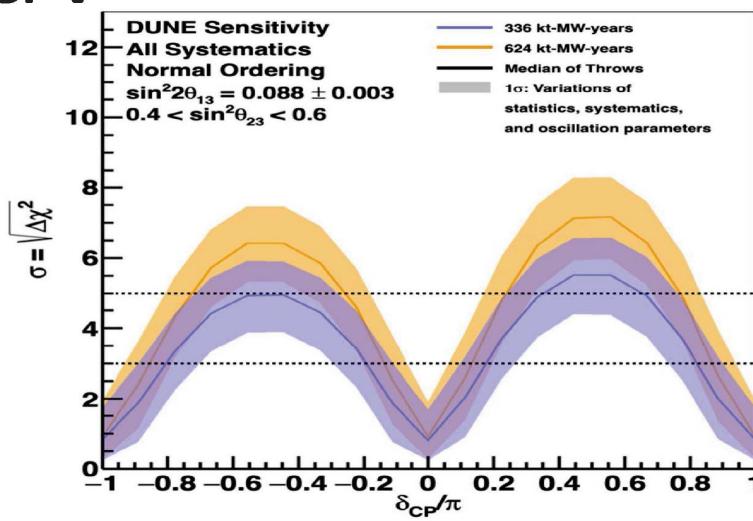
Mass Ordering



Hyper-Kamiokande



CPV



Confirmed LE Picture and today's List of Q&A

- At least two neutrinos are massive \Rightarrow There is NP
- Updated 3ν fit
 - Robust determination of θ_{12} , θ_{13} , Δm_{21}^2 , $|\Delta m_{3\ell}^2|$
 - Mass ordering, θ_{23} Octant, CPV depend on subdominant 3ν -effects
 \Rightarrow interplay of LBL/reactor/ATM results

	best fit MO	$\Delta\chi^2(\text{MO})$	best fit δ_{CP}	$\Delta\chi^2(\text{CPC})$	oct. θ_{23}	$\Delta\chi^2(\text{oct})$
LBL	IO	1.5	275°	2.0	2nd	2.2
+reactors	NO	2.7	195°	0.4	2nd	0.5
+ SK-Atm 328 kt-y (NuFIT 5.0)	NO	7.1	197°	0.5	2nd	2.5
or + SK-Atm 373 kt-y (NuFIT 5.1)	NO	7.0	230°	4.0	1st	3.2

\Rightarrow not statistically significant yet

\Rightarrow definitive answer will likely require new experiments

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\Rightarrow not statistically significant yet

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- Only three light states?

Beyond 3ν 's: Light Sterile Neutrinos

- Several Observations which can be Interpreted as Oscillations with $\Delta m^2 \sim \text{eV}^2$

LSND & MiniBoone

LSND 2001:

Signal $\nu_\mu \rightarrow \nu_e$ (3.8σ)

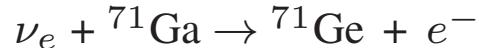
MiniBooNE 2020:

$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ & $\nu_\mu \rightarrow \nu_e$
(639 ± 132.8 events)

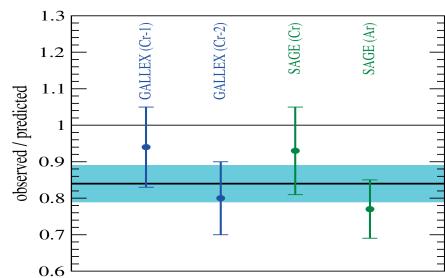
Gallium Anomaly

Acero, Giunti, Laveder, 0711.4222
Giunti, Laveder, 1006.3244

Radioactive Sources (^{51}Cr , ^{37}Ar)
in calibration of Ga Solar Exp;



Give a rate lower than expected



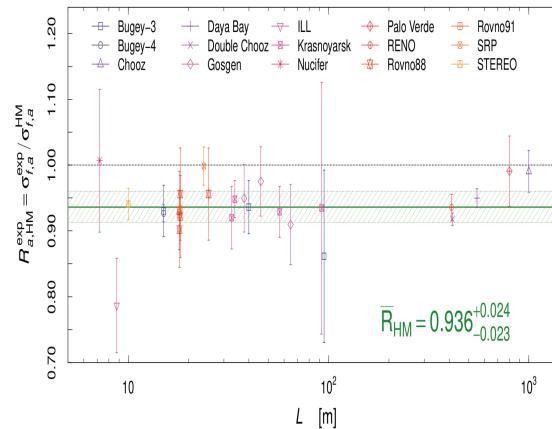
Explained as ν_e disappearance

Reactor Anomaly (2011)

Huber, 1106.0687
Mention et al., 1101.2755

New reactor flux calculation

\Rightarrow Deficit in data at $L \lesssim 100$ m



Explained as $\bar{\nu}_e$ disappearance

Beyond 3ν 's: Light Sterile Neutrinos

Gonzalez-Garcia 31-a

- Several Observations which can be Interpreted as Oscillations with $\Delta m^2 \sim \text{eV}^2$

LSND & MiniBoone

LSND 2001:

Signal $\nu_\mu \rightarrow \nu_\tau$ Oscillation Interpretation Requires new (sterile) ν 's calculation

MiniBooNE 2011:

$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ & $\nu_\mu \rightarrow (\bar{\nu}_e + \nu_e)$ (639 ± 132.8)

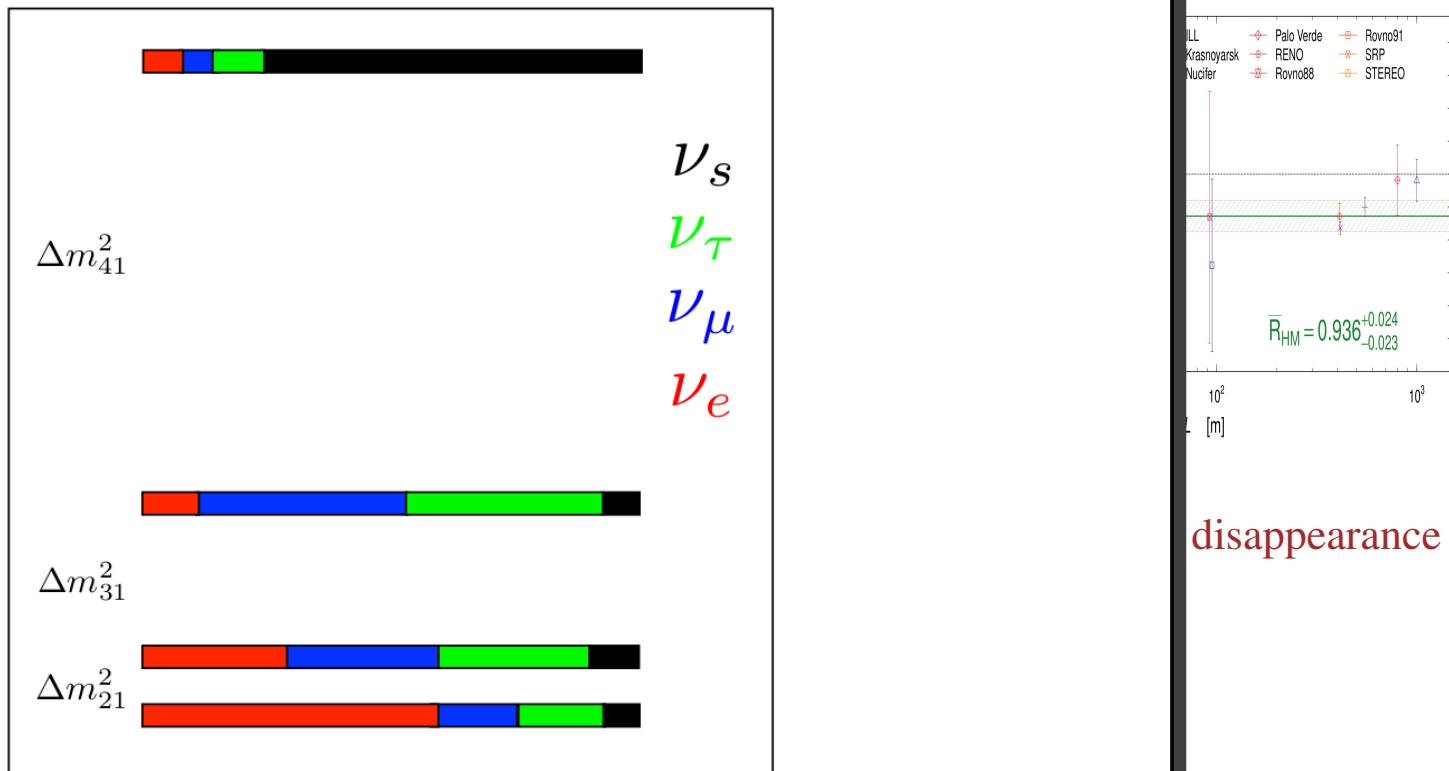
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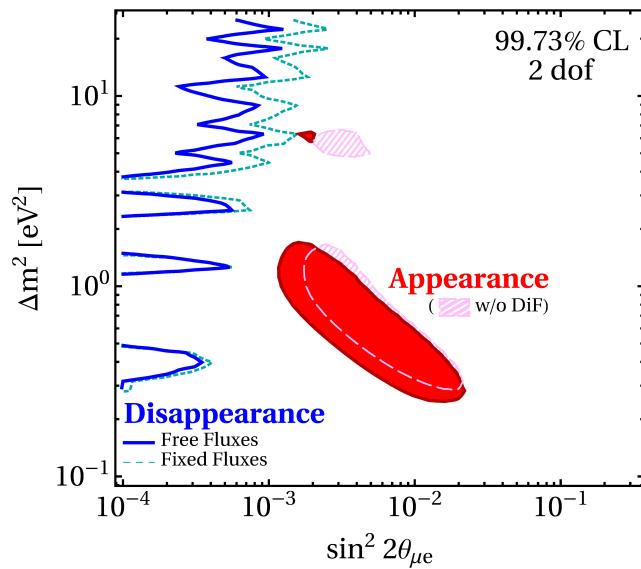
Gonzalez-Garcia 32

LSND & MiniBoone

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e \text{ & } \nu_\mu \rightarrow \nu_e$$

$$\sin^2 2\theta_{\mu e} \sim \frac{1}{4} \sin^2 2\theta_{ee} \sin^2 2\theta_{\mu\mu}$$

Strong tension with
non-observation of ν_μ dissap



Dentler et al, 1803.10661

Purely sterile oscillation
robustly disfavoured
additional SM or NP effects?

Beyond 3ν 's: Light Sterile Neutrinos

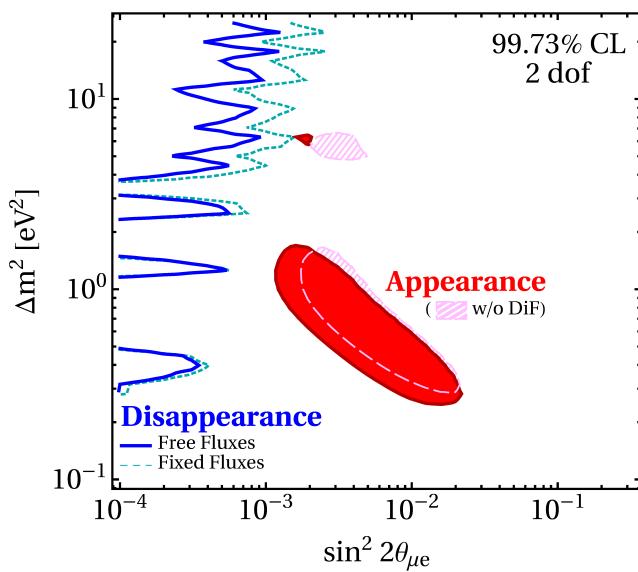
Gonzalez-Garcia 32-a

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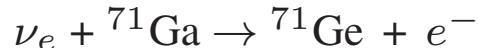


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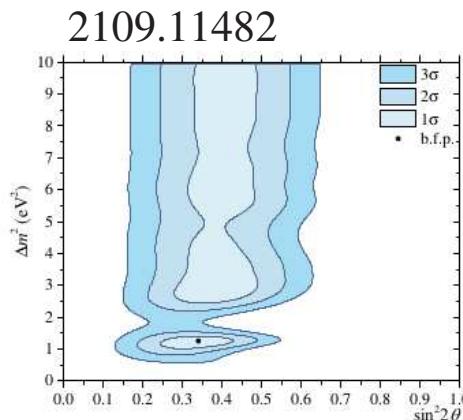
Acero et al, 0711.4222; Giunti, Laveder, 1006.3244



Rate lower than expected

Explained as ν_e disappearance

Confirming results from BEST



Requires large mixings

Ruled out/tension by solar ν' s

Goldhagen et al 2109.14898

Berryman et al 2111.12530

Beyond 3ν 's: Light Sterile Neutrinos

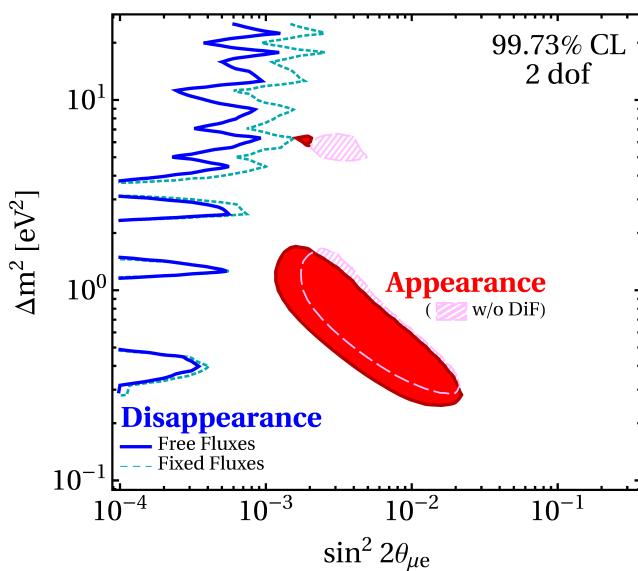
Gonzalez-Garcia 32-b

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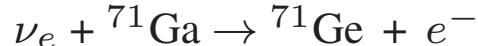


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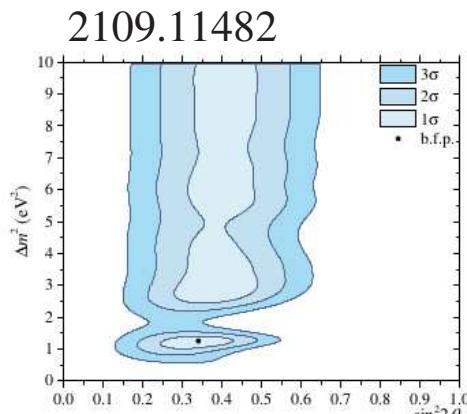
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Huber, 1106.068, Mention et al, 1101.2755

2011 reactor flux calculation \Rightarrow

Deficit in $R = \frac{\text{data}}{\text{predict}}$ at $L \lesssim 100$ m

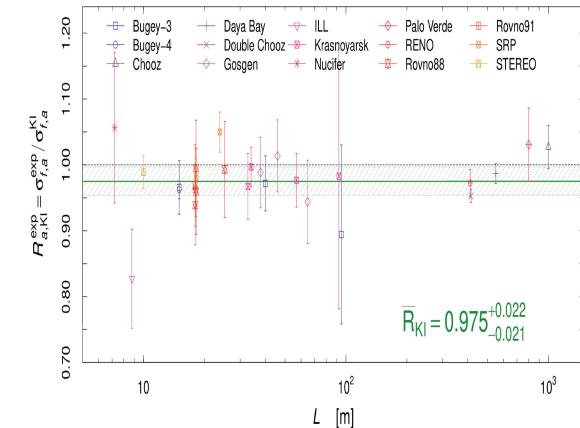
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2022 with updated inputs (${}^{235}\text{U}$)

Berryman Huber, 2005.01756

Kipeikin et al, 2103.01486

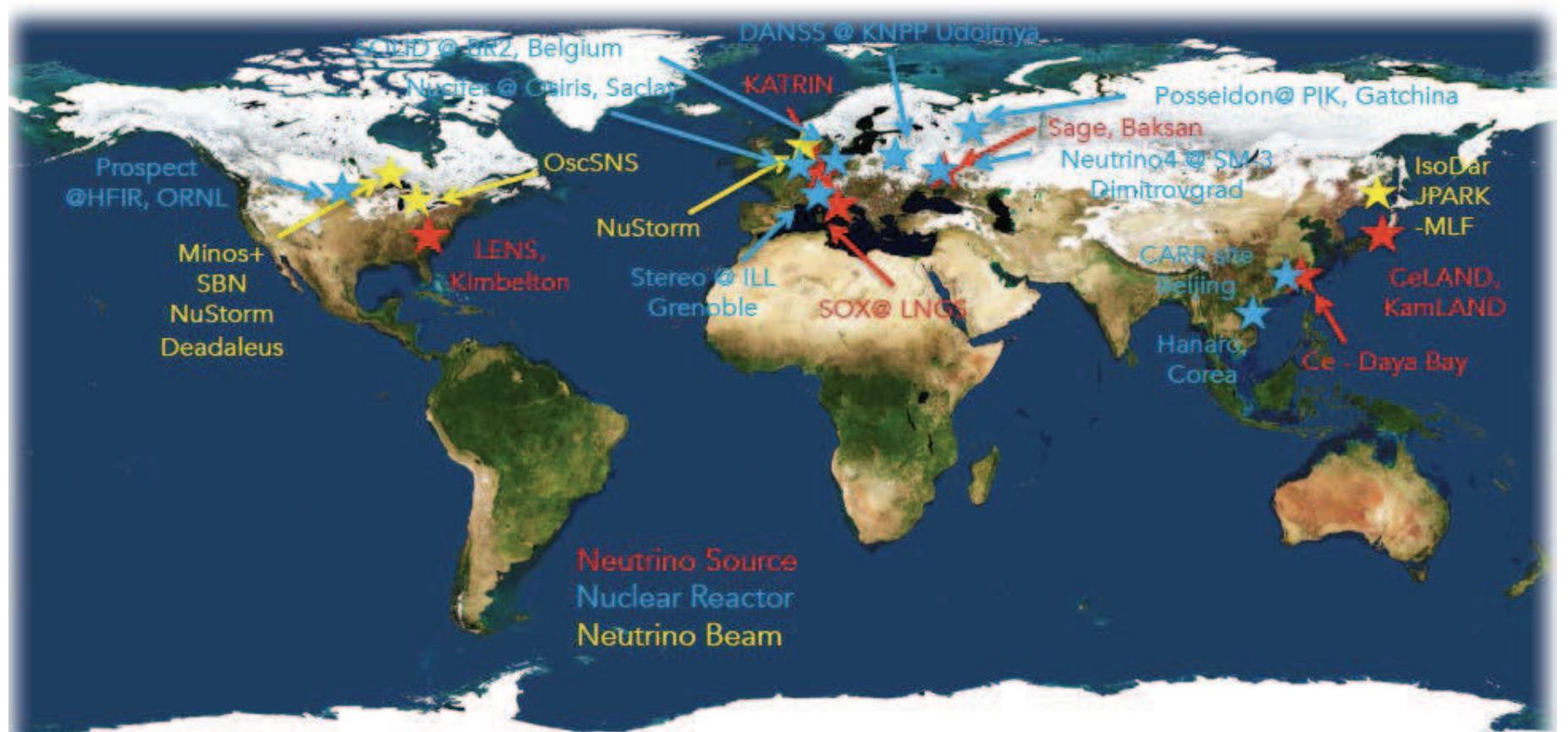
Giunti et al, 2110.06820



(Fig from Giunti et al, 2110.06820)

Anomaly $\sim 1\sigma$
with new fluxes

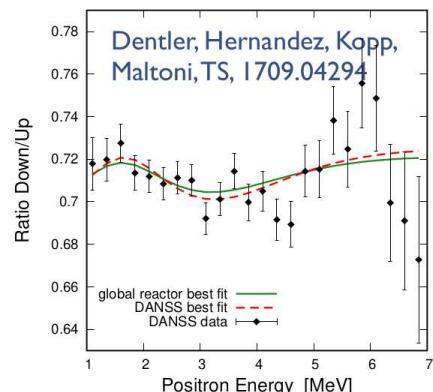
Searches for eV sterile neutrinos



This talk: (anti-) ν_e disappearance only

$$P_{ee} = 1 - \sin^2 2\theta_{ee} \sin^2 \frac{\Delta m_{41}^2}{4E} \quad \& \quad \sin^2 2\theta_{ee} = |U_{e4}|^2 \left(1 - |U_{e4}|^2\right)$$

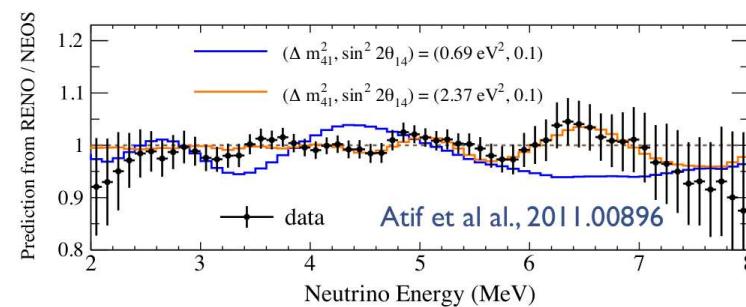
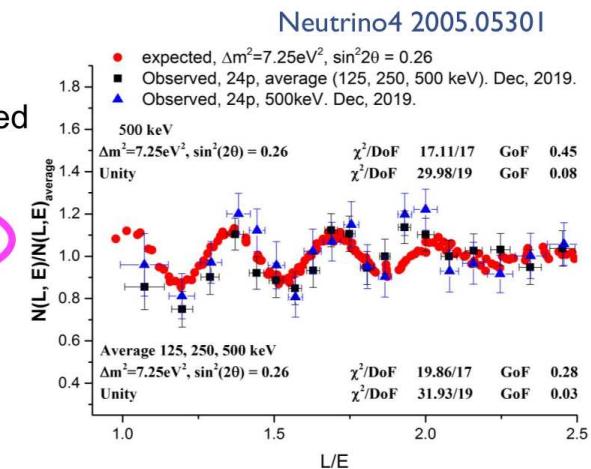
Recent relative spectral measurements



~~DANSS: relative spectra @ L = 10.7 and 12.7 m
prev. $\sim 2\sigma$ hint decr. $\sim 1.5\sigma$~~
DANSS talk @ ICHEP20 (update at EPS-HEP21)

segmented detectors:
STEREO [arXiv:1912.06582]
 $L = 9$ to 11 m $\Delta\chi^2(\text{no osc}) \approx 9$
PROSPECT [arXiv:2006.11210]
 $L = 6.7$ to 9.2 m

Neutrino4: segmented detector, $L = 6.25$ to 11.9 m, 216 bins in L/E , $\text{"}3\sigma\text{"}$ indication



NEOS: spectrum at $L = 24$ m, relative to RENO (or DayaBay) near detectors: $\Delta\chi^2(\text{no osc}) = 11.7$

Spectral ratios at different baselines \Rightarrow Independent of flux normalizations.

But low statistical significance (Wilks theorem fails) Berryman, et al 2111.12530

MC estimation of prob distribution \Rightarrow no significant indication of ν_s oscillations

Confirmed Low Energy Picture and MY List of Q&A

- At least two neutrinos are massive \Rightarrow There is NP
- 3ν scenario: Robust determination of $\theta_{12}, \theta_{13}, \Delta m_{21}^2, |\Delta m_{3\ell}^2|$
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- Other NP at play?

Non Standard ν Interactions (NSI)

At dimension-6 new 4-fermion interactions involving ν 's.

Some can affect CC process in production and detection

$$(\bar{\nu}_\alpha \gamma_\mu P_L \ell_\beta)(\bar{f}' \gamma^\mu P f)$$

and can be strongly constrained with charged lepton processes

Some affect only NC ν interactions

$$(\bar{\nu}_\alpha \gamma_\mu P_L \nu_\beta)(\bar{f} \gamma^\mu P f)$$

and are more poorly constrained

Including non-standard neutrino NC interactions with fermion f

$$\mathcal{L}_{\text{NSI}}^{\text{NC}} = -2\sqrt{2}G_F \varepsilon_{\alpha\beta}^{fP} (\bar{\nu}_\alpha \gamma^\mu L \nu_\beta) (\bar{f} \gamma_\mu P f), \quad P = L, R$$

NC-Non Standard ν Interactions in ν -OSC

rcia 37-a

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$$H_{\text{mat}} = \sqrt{2}G_F N_e(r) \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} + \sqrt{2}G_F N_e(r) \begin{pmatrix} \varepsilon_{ee} & \varepsilon_{e\mu} & \varepsilon_{e\tau} \\ \varepsilon_{e\mu}^* & \varepsilon_{\mu\mu} & \varepsilon_{\mu\tau} \\ \varepsilon_{e\tau}^* & \varepsilon_{\mu\tau}^* & \varepsilon_{\tau\tau} \end{pmatrix}$$

$$\varepsilon_{\alpha\beta}(r) \equiv \sum_{f=ued} \frac{N_f(r)}{N_e(r)} \varepsilon_{\alpha\beta}^{fV} \Rightarrow 3\nu \text{ evolution depends on 6 (vac) + 8 per } f \text{ (mat)}$$

NC-Non Standard ν Interactions in ν -OSC

Sec 37-b

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\Rightarrow Parameters degeneracies

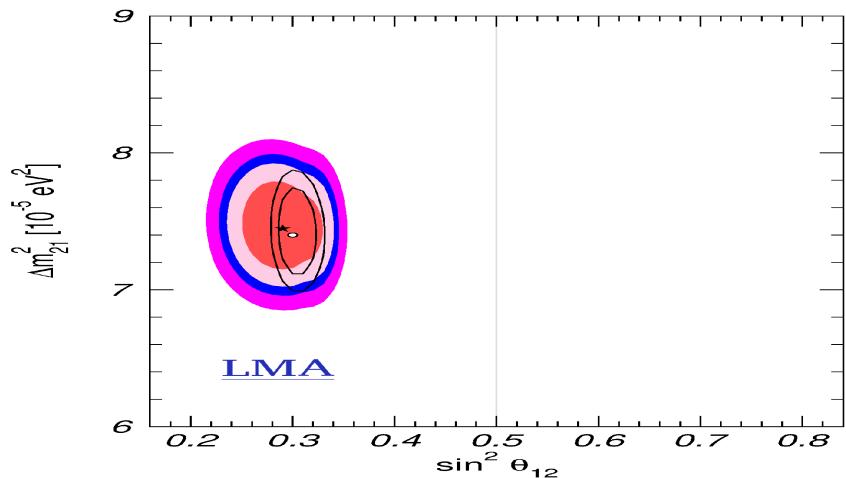
In particular $H \rightarrow -H^*$ \Rightarrow same Probabilities \Rightarrow invariance under simultaneously:

$$\begin{array}{ll} \theta_{12} \leftrightarrow \frac{\pi}{2} - \theta_{12}, & (\varepsilon_{ee} - \varepsilon_{\mu\mu}) \rightarrow -(\varepsilon_{ee} - \varepsilon_{\mu\mu}) - 2, \\ \Delta m_{31}^2 \rightarrow -\Delta m_{32}^2, & (\varepsilon_{\tau\tau} - \varepsilon_{\mu\mu}) \rightarrow -(\varepsilon_{\tau\tau} - \varepsilon_{\mu\mu}), \\ \delta \rightarrow \pi - \delta, & \varepsilon_{\alpha\beta} \rightarrow -\varepsilon_{\alpha\beta}^* \quad (\alpha \neq \beta), \end{array}$$

\Rightarrow Degeneracies in θ_{12} octant and mass ordering

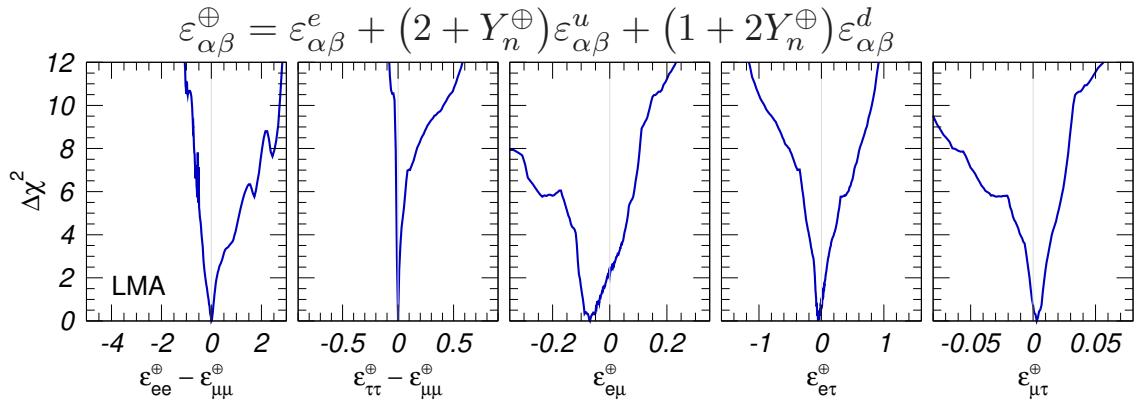
NSI: Bounds/Degeneracies from/in Oscillation data

Esteban *et al.* JHEP'18[1805.04530] Coloma, Esteban, MCGG, Maltoni, JHEP'19[1911.09109] (updated 2020)



	LMA
$\varepsilon_{ee}^u - \varepsilon_{\mu\mu}^u$	$[-0.072, +0.321]$
$\varepsilon_{\tau\tau}^u - \varepsilon_{\mu\mu}^u$	$[-0.001, +0.018]$
$\varepsilon_{e\mu}^u$	$[-0.050, +0.020]$
$\varepsilon_{e\tau}^u$	$[-0.077, +0.098]$
$\varepsilon_{\mu\tau}^u$	$[-0.006, +0.007]$

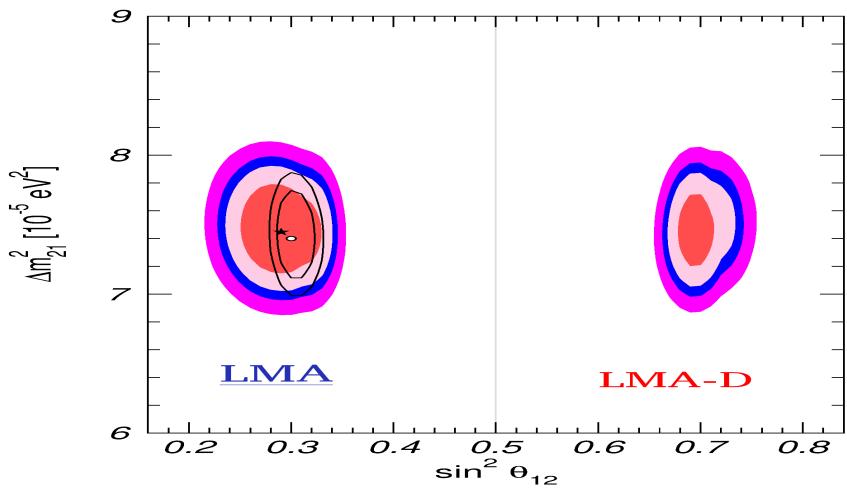
- Standard Fit \equiv LMA \Rightarrow Bounds $\mathcal{O}(1\% - 10\%)$
 \Rightarrow Maximum effect at LBL experiments:



\Rightarrow To be considered in effects/sensitivity studies
at DUNE, HK... (tables available)

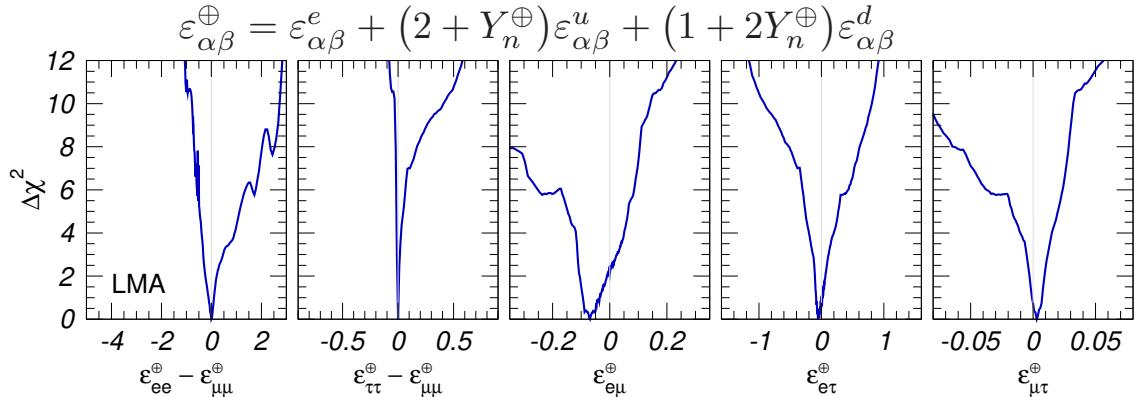
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	LMA	$\text{LMA} \oplus \text{LMA-D}$
$\varepsilon_{ee}^u - \varepsilon_{\mu\mu}^u$	$[-0.072, +0.321]$	$\oplus [-1.042, -0.743]$
$\varepsilon_{\tau\tau}^u - \varepsilon_{\mu\mu}^u$	$[-0.001, +0.018]$	$[-0.016, +0.018]$
$\varepsilon_{e\mu}^u$	$[-0.050, +0.020]$	$[-0.050, +0.059]$
$\varepsilon_{e\tau}^u$	$[-0.077, +0.098]$	$[-0.111, +0.098]$
$\varepsilon_{\mu\tau}^u$	$[-0.006, +0.007]$	$[-0.006, +0.007]$

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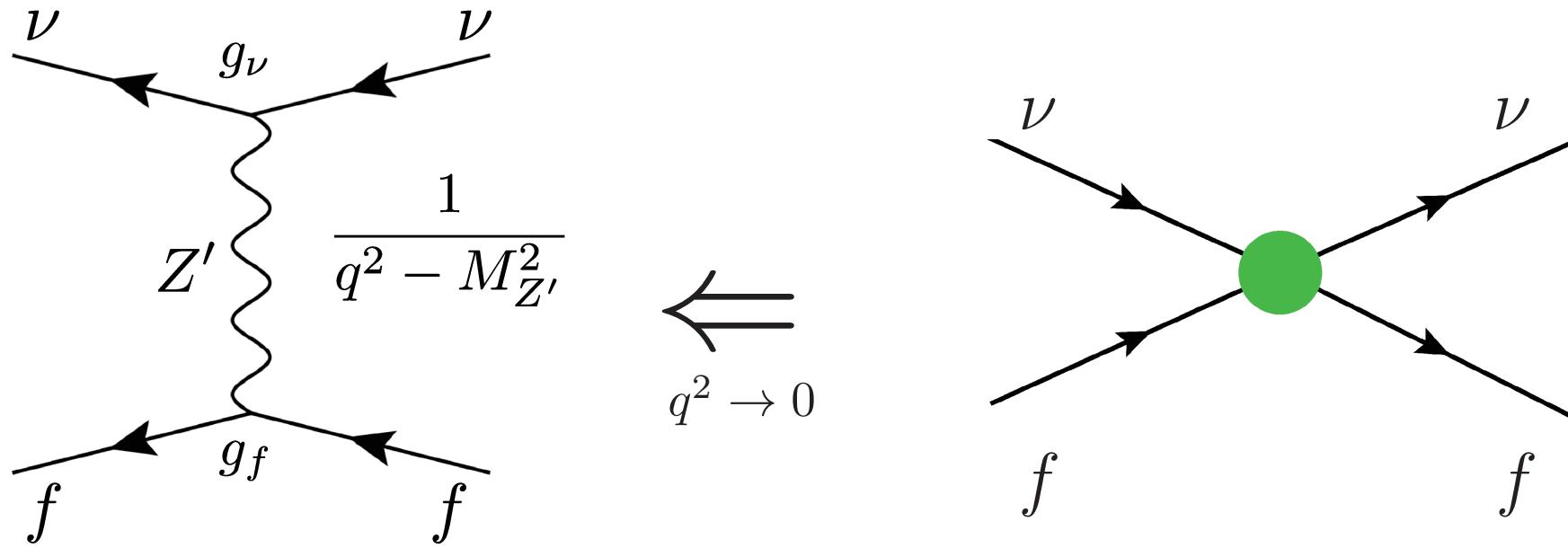
- Degenerate solution $\equiv \text{LMA-D}$
- Miranda, Tortola, Valle, hep-ph/0406280
- $\Rightarrow \theta_{12} \leftrightarrow \frac{\pi}{2} - \theta_{12}$ & $(\varepsilon_{ee} - \varepsilon_{\mu\mu}) \rightarrow -(\varepsilon_{ee} - \varepsilon_{\mu\mu}) - 2$
- \Rightarrow Requires NSI $\sim G_F$ (light mediators?)

Farzan 1505.06906, and Shoemaker 1512.09147

Oscillation bounds on Z'/Dark Photons

Coloma, MCGG, Maltoni, JHEP'21 [2009.14220]

Interpreting

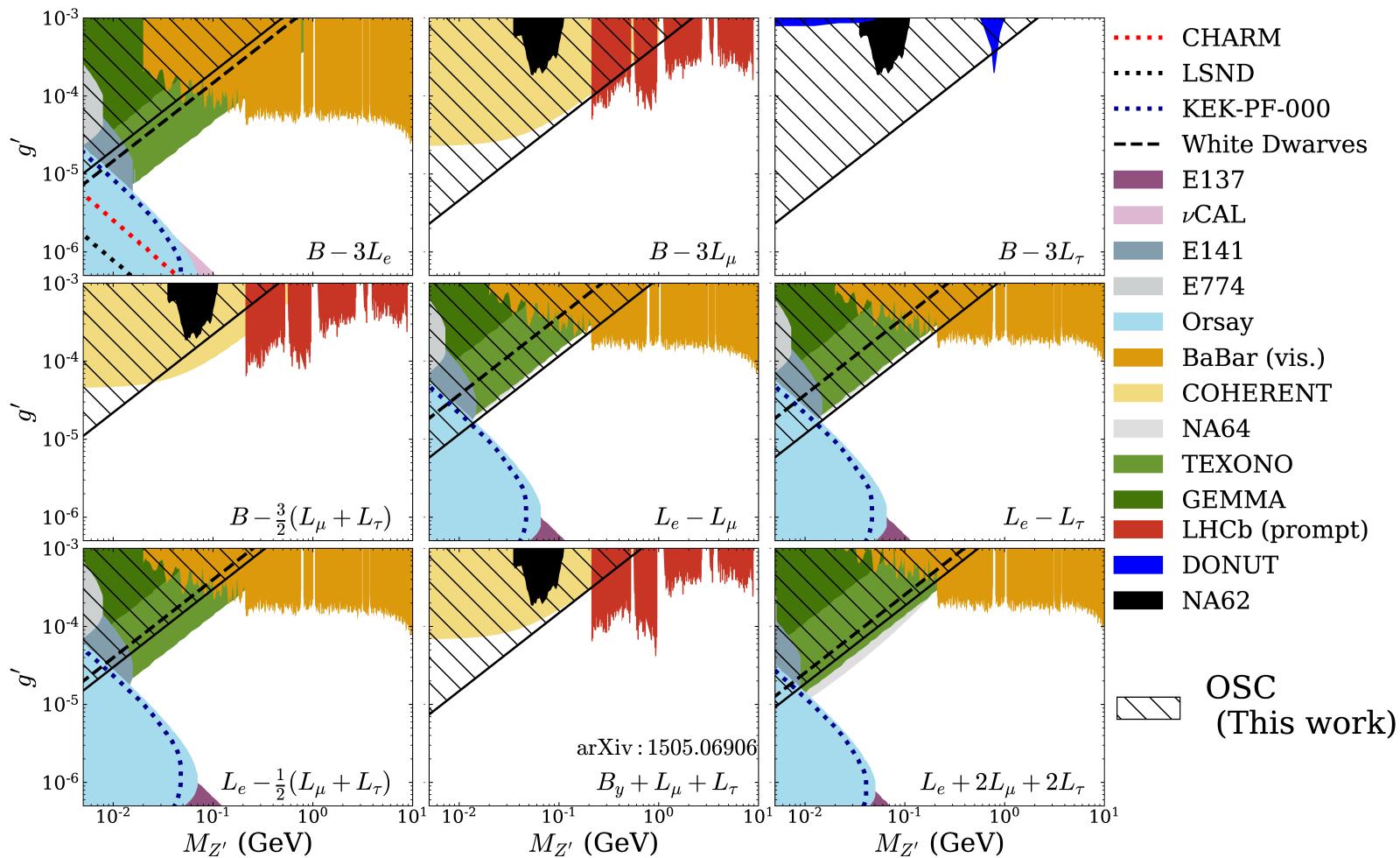


$$\frac{g'^2}{M_{Z'}^2} q'_f q'_\nu \quad \Leftarrow \quad \epsilon_{\alpha\beta}^f$$

Z' Models: ν Oscillations Bounds

Coloma, MCGG, Maltoni ArXiv:2009.14220

$M_{Z'} \gtrsim \mathcal{O}(\text{MeV}) \Rightarrow$ Contact Interaction in H_{mat}



\Rightarrow Bounds from Oscillations stronger than scattering bounds on some models

Z' Models: Long Range Regime

For extremely light Z' the potential encountered by ν at \vec{x} depends on the integral of the source density within a radius $\sim 1/M_{Z'}$ around it

$$\text{We can still formally write } H_{\text{mat}} = \sqrt{2}G_F N_e(r) \begin{pmatrix} 1 + \varepsilon_{ee}(\vec{x}) & 0 & 0 \\ 0 & \varepsilon_{\mu\mu}(\vec{x}) & 0 \\ 0 & 0 & \varepsilon_{\tau\tau}(\vec{x}) \end{pmatrix}$$

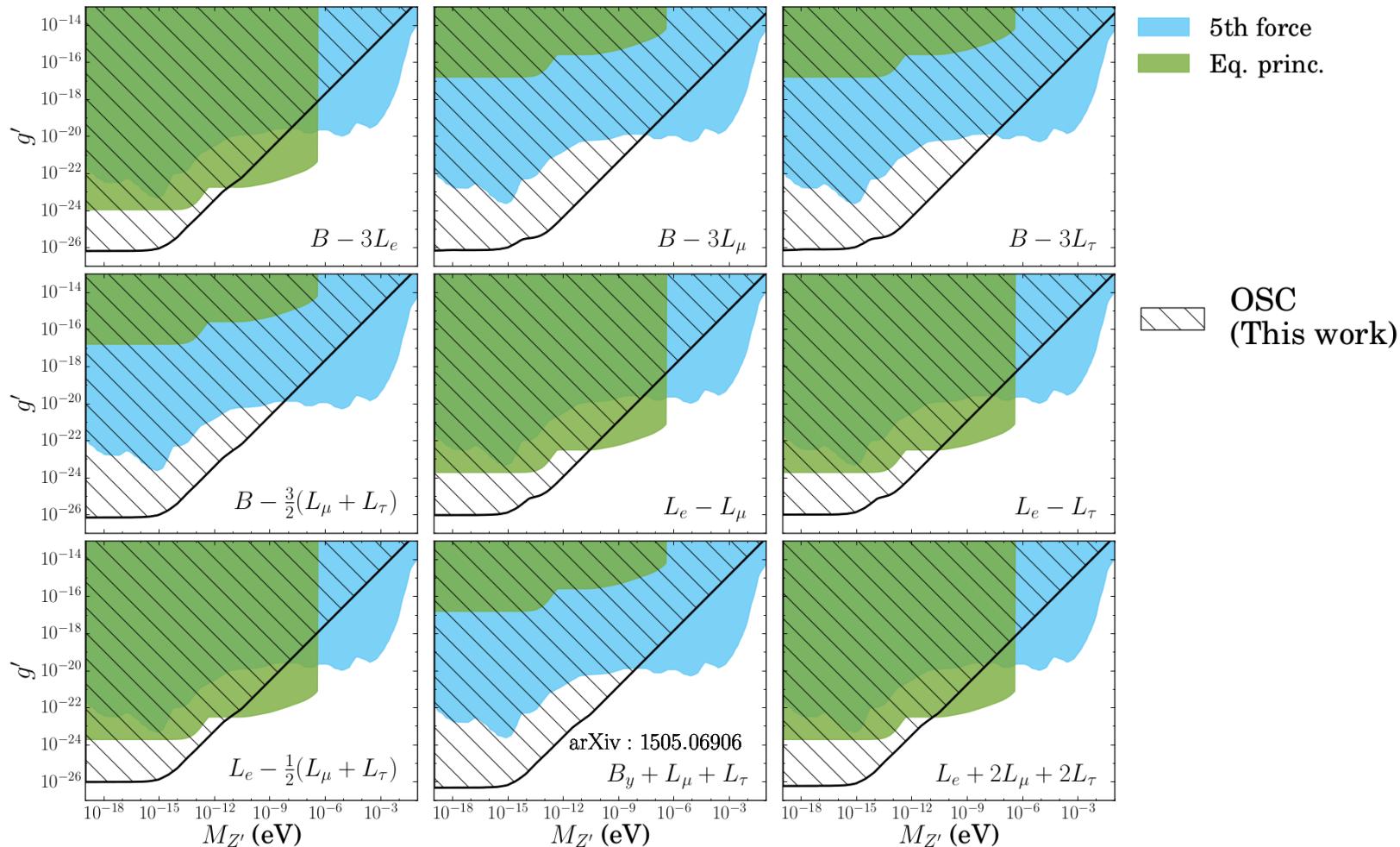
$$\varepsilon_{\alpha\beta}(\vec{x}) \equiv \sum_f \frac{\hat{N}_f(\vec{x}, M_{Z'})}{N_e(r)} \varepsilon_{\alpha\beta}^f \quad \hat{N}_f(\vec{x}, M_{Z'}) \equiv \frac{4\pi}{M_{Z'}^2} \int N_f(\vec{\rho}) \frac{e^{-M_{Z'}|\vec{\rho}-\vec{x}|}}{|\vec{\rho}-\vec{x}|} d^3\vec{\rho}$$

de Holanda, MCGG, Masso,Zukanovich hep-ph/0609094

$Z'/\text{Dark-photon}$: Bounds from ν Oscillations

Coloma, MCGG, Maltoni, JHEP'21 [2009.14220]

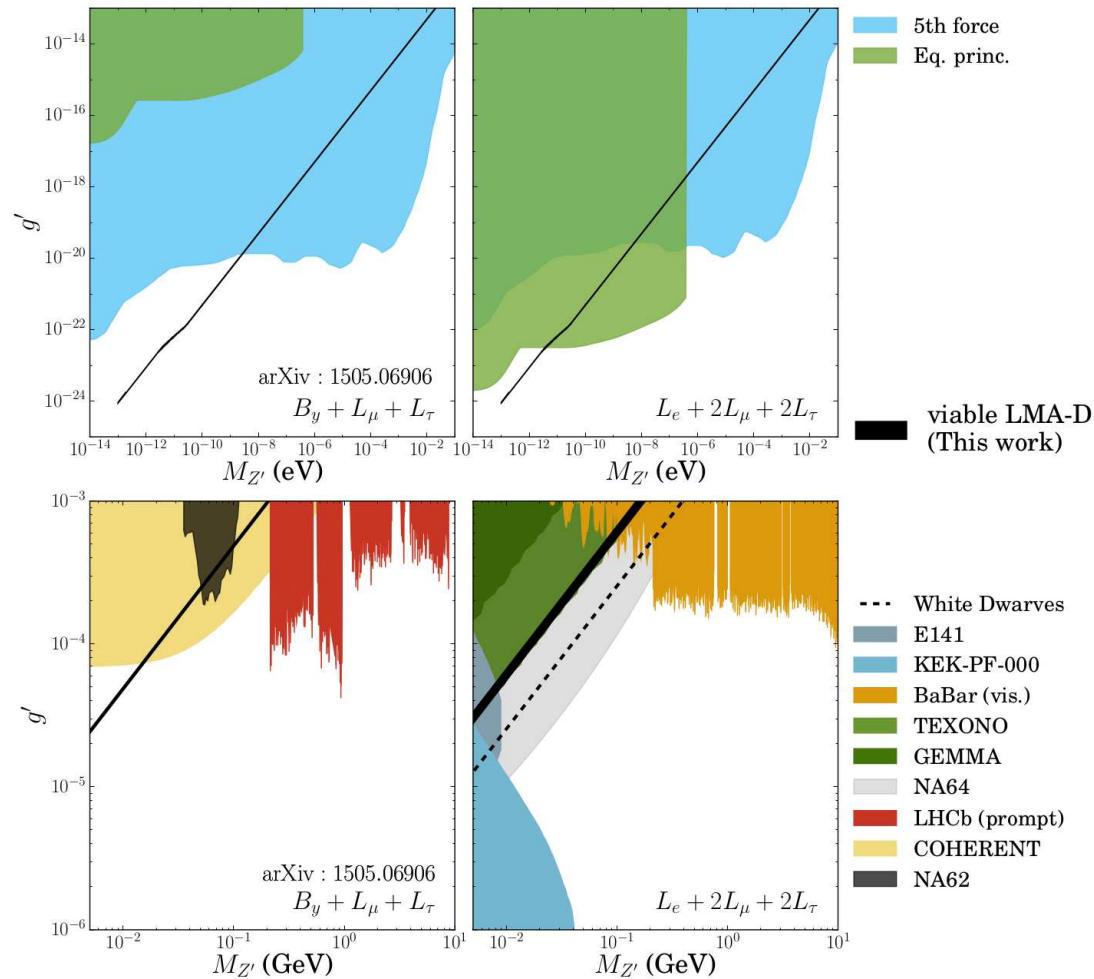
Very light ($M' \lesssim \mathcal{O}(\text{eV})$) mediator \Rightarrow Long Range Force to Contact Interaction in H_{mat}



\Rightarrow Bounds from Oscillations stronger than 5th force and VEP experiments

Z' Models: Viable models for LMA-D

Survey 10000 set of models characterized by the six relevant fermion $U(1)$ charges
 About 5% lead to a viable LMA-D solution. Two examples



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 - Cosmological effects?: No signal yet
- Other NP at play? Only subdominant allowed. But for NSI
 - No hint in present experiments \Rightarrow bounds on effects at future experiments
 - But degenerate solution Dark-LMA not excluded
 - Bounds on flavoured dark-photon/Z' models
- What about a UV complete model which answers?:
 - Why are neutrinos so light? \equiv The Origin of Neutrino Mass
 - Why are lepton mixing so different from quark's? \equiv The Flavour Puzzle

Bottom-up: Light ν from Generic New Physics

If SM is an effective low energy theory, for $E \ll \Lambda_{\text{NP}}$

- The same particle content as the SM and same pattern of symmetry breaking
- But there can be non-renormalizable ($\text{dim} > 4$) operators

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 \Rightarrow First NP effect \Rightarrow dim=5 operator. Only one and violates Lepton Number

$$\mathcal{O}_5 = \frac{Z_{ij}^\nu}{\Lambda_{\text{NP}}} \left(\overline{L_{L,i}} \tilde{\phi} \right) \left(\tilde{\phi}^T L_{L,j}^C \right) \Rightarrow (M_\nu)_{ij} = Z_{ij}^\nu \frac{v^2}{\Lambda_{\text{NP}}}$$

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Implications:

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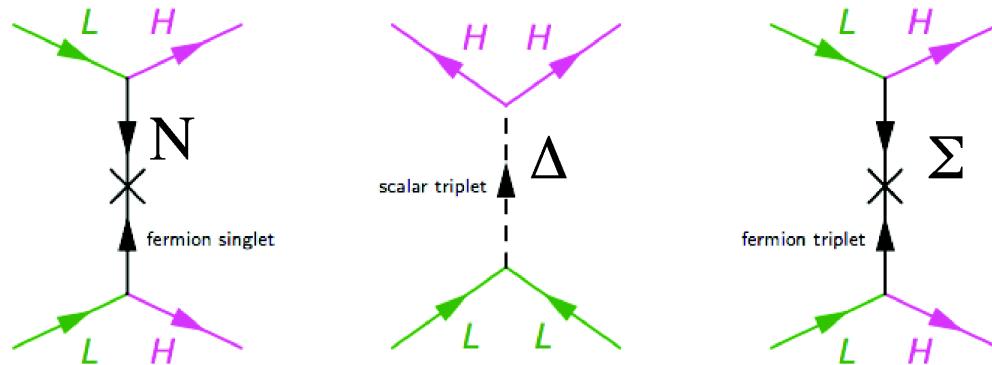
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- $m_\nu > \sqrt{\Delta m_{\text{atm}}^2} \sim 0.05 \text{ eV}$ for $Z^\nu \sim 1 \Rightarrow \Lambda_{\text{NP}} \sim 10^{15} \text{ GeV} \Rightarrow \Lambda_{\text{NP}} \sim \text{GUT scale}$
 \Rightarrow Leptogenesis possible
- [But if $Z^\nu \sim (Y_e)^2 \Rightarrow \Lambda_{\text{NP}} \sim \text{TeV scale}$]

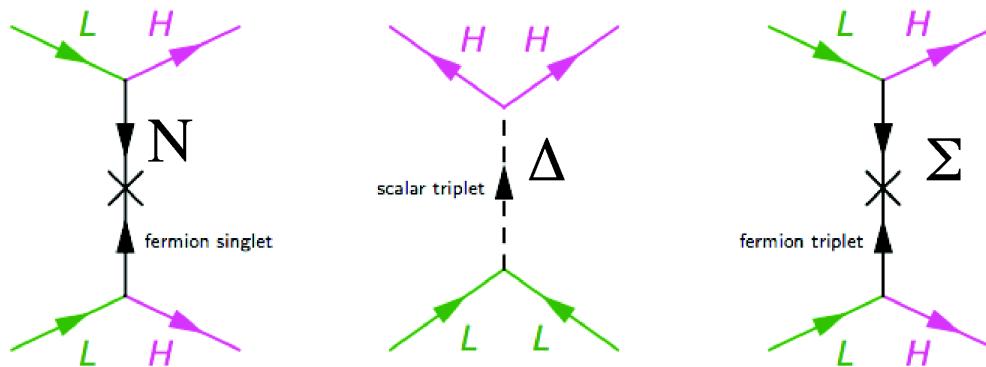
Model Degeneracy at Low Energy

\mathcal{O}_5 is generated for example by tree-level exchange of singlet ($N_i \equiv (1, 1)_0$) (Type-I) or triplet fermions ($N_i \equiv \Sigma_i \equiv (1, 3)_0$) (Type-III) or a scalar triplet $\Delta \equiv (1, 3)_1$ (Type-II)



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- For fermionic see-saw $-\mathcal{L}_{\text{NP}} = -i\overline{N}_i \not{D} N_i + \frac{1}{2} M_{Nij} \overline{N}_i^c N_j + \lambda_{\alpha j}^\nu \overline{L}_\alpha \tilde{\phi} N_j [\tau]$
 $\Rightarrow \mathcal{O}_5 = \frac{(\lambda^\nu{}^T \lambda^\nu)_{\alpha\beta}}{\Lambda_{\text{NP}}} \left(\overline{L}_\alpha \tilde{\phi} \right) \left(\tilde{\phi}^T L_\beta^C \right)$ with $\Lambda_{\text{NP}} = M_N$
- For scalar see-saw $-\mathcal{L}_{\text{NP}} = f_{\Delta\alpha\beta} \overline{L}_\alpha \Delta L_\beta^C + M_\Delta^2 |\Delta|^2 + \kappa \phi^T \Delta^\dagger \phi \dots$
 $\Rightarrow \mathcal{O}_5 = \frac{f_{\Delta\alpha\beta}}{\Lambda_{\text{NP}}} \left(\overline{L}_\alpha \tilde{\phi} \right) \left(\tilde{\phi}^T L_\beta^C \right)$ with $\Lambda_{\text{NP}} = \frac{M_\Delta^2}{\kappa}$

Very different physics, but same ν parameters: How to proceed?

Model Degeneracy at Low Energy

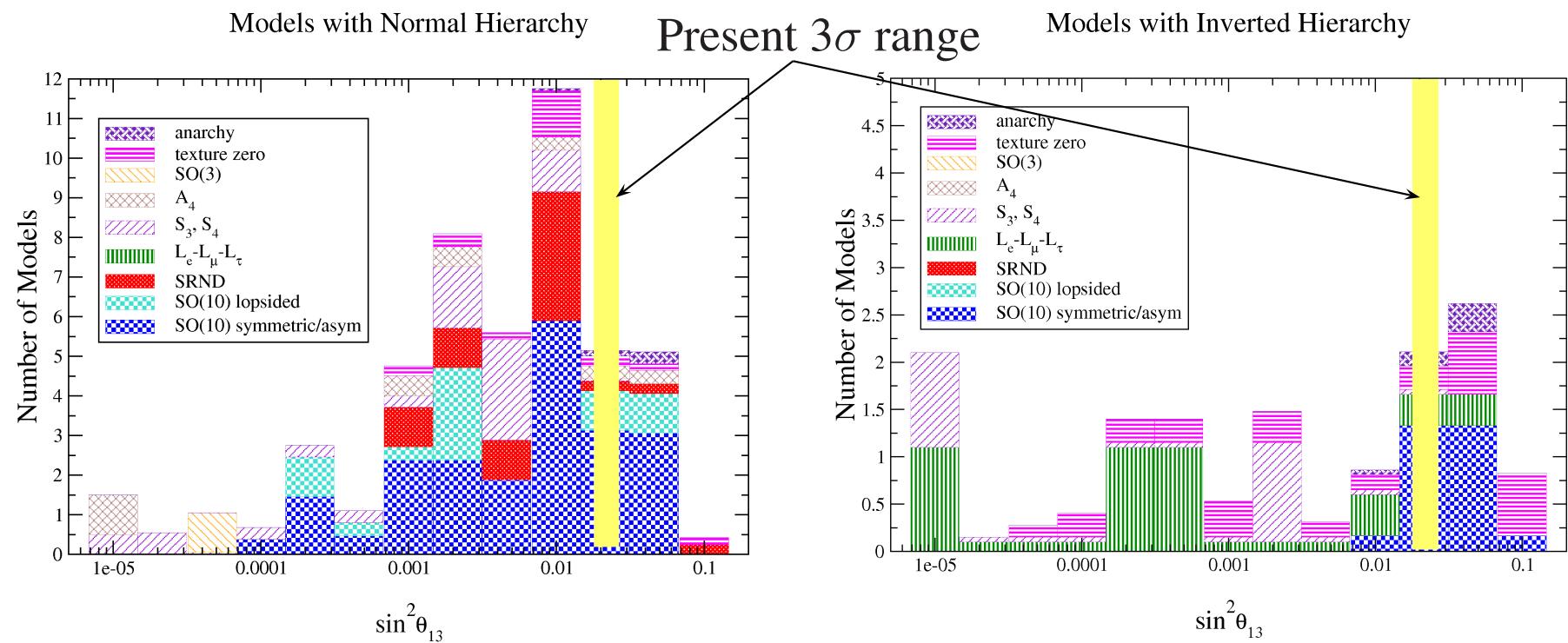
Same \mathcal{O}_5 can be generated by very different High Energy physics

Very different physics, but same ν parameters: How to proceed?

- Top-down: Assume some specific model and work out the relations

Modeling Lepton Flavour: 2006 to 2022

- Survey of 63 ν mass models in 2006 (Albright, M-C Chen, hep-ph/0608136)



- Determination of θ_{13} has given us important handle in flavour modeling
- Next *frontier* is the ordering

Model Degeneracy at Low Energy

Same \mathcal{O}_5 can be generated by very different High Energy physics

Very different physics, but same ν parameters: How to proceed?

- Top-down: Assume some specific model and work out the relations
- Search for additional information from charged LFV, collider signals ...

Connection to CLFV & Collider Signatures?

- ν oscillation \Rightarrow Lepton Flavour is not conserved and generically new Λ_{NP} scale

If only $\mathcal{O}_5 \Rightarrow Br(\tau \rightarrow \mu\gamma) \sim 10^{-41}$ too small and $\Lambda_{\text{NP}} \sim v^2/m_\nu$ too high

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So may be

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New Physics scale Λ_{LN} responsible for the small m_ν from

New Physics scale Λ_{LF} ($\ll \Lambda_{LN}$) controlling of LFV

and if heavy state mass $M \sim \Lambda_{LF} \sim \text{TeV} \Rightarrow$ Collider signatures

Furthermore if $c_{6,i} \propto c_5^{\text{some power}} \Rightarrow$ LFV and coll signals directly related to M_ν

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Minimal Lepton Flavour Violation

Cirigliano, Grinstein, Isidori, Wise(05); Davidson, Palorini (06); Gavela, Hambye, Hernandez,Hernandez (09)
Alonso, Isidori, Merlo, Munoz, Nardi(11)

MLFV & Collider Signatures

cha Gonzalez-Garcia 52

- Minimal Flavour Violation Hypothesis: Chivukula, Georgi (87) Buras, Gambino, Gorbahn, Jager, Silvestrini,(01) d'Ambrosio, Giudice, Isidori, Strumia (02)

Yukawas are the only source of flavour violation in and beyond SM

Very predictive and successful to explain quark flavour data

For leptons more subtle since BSM fields are required to generate majorana M_ν

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a Gonzalez-Garcia 52-a

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- Scalar (Type-II) see-saw is MLFV

$$c_{5,\alpha\beta} = f_{\Delta\alpha\beta} \frac{\kappa}{M_\Delta} \quad c_{6,\alpha\beta\gamma\rho} = f_{\Delta\alpha\beta}^\dagger f_{\Delta\gamma\rho}$$

- If $M_\Delta \lesssim \text{TeV}$

⇒ Production of triplet scalars: $H^{\pm\pm}$, H^\pm , A_0 , H_0

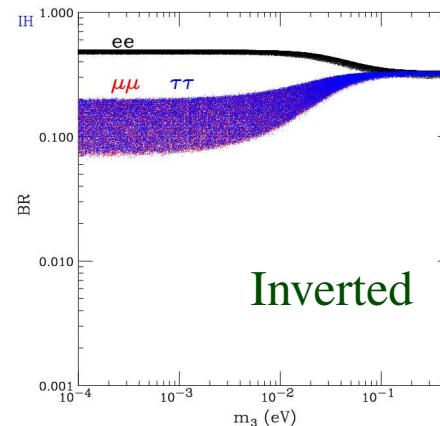
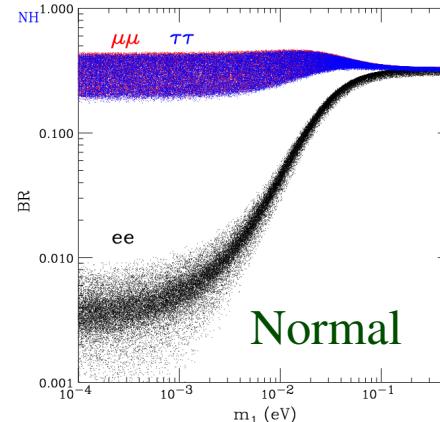
$$pp \rightarrow H^{++} H^{--}$$

$$pp \rightarrow H^{++} H^-$$

Striking Signatures

$$\Rightarrow H^{\pm\pm} l_i^\pm l_j^\pm, H^\pm \rightarrow l_i^\pm \nu_j$$

predicted by neutrino parameters



Akeroyd *et al*, Chao *et al*, Fileviez *et al*
Garayoa *et al*, Han *et al*, Kadastik *et al* ...

MLFV & Collider Signatures

- MLFV Fermionic (I or III) Inverse see-saw

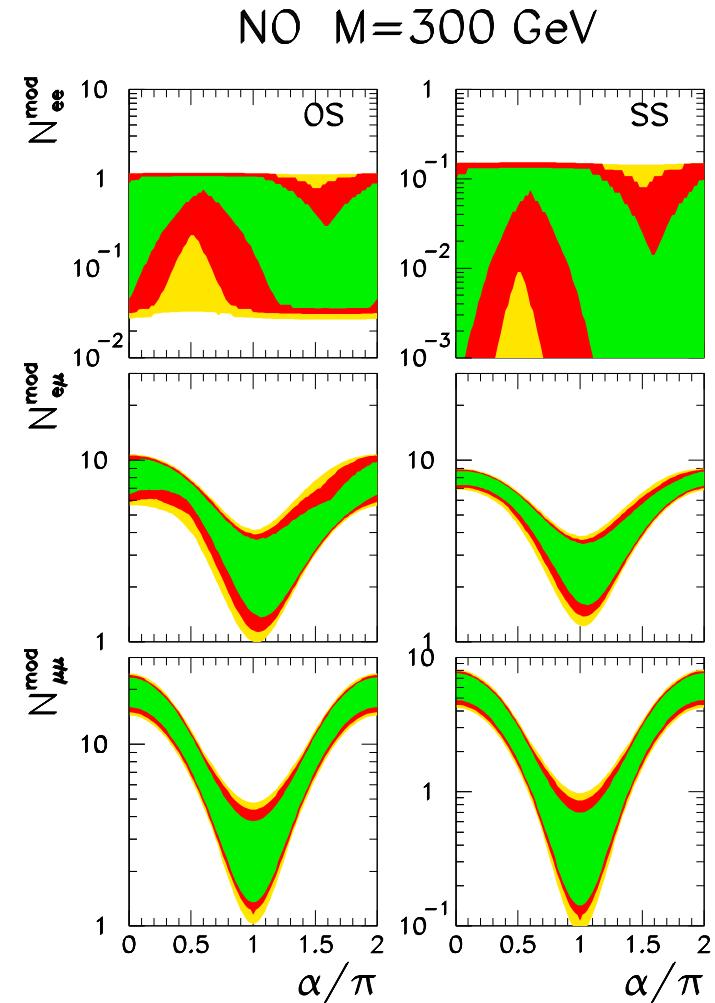
Gavela, Hambye, Hernandez,Hernandez (09)

- one massless ν & one CP phase α
- Yukawas $\lambda_{\alpha N}$ determined by ν parameters

- At LHC:

- Type-I unobservable but Type-III observable

$$pp \rightarrow F(\rightarrow \ell_\alpha X) F'(\rightarrow \ell_\beta X')$$
- Rates predictable in terms of ν parameters
- Unambiguous constraints from existing data
- Best with final state flavour and charge info



Rosa-Agostinho,Eboli, MCGG 1708.08456

Confirmed Low Energy Picture and MY List of Q&A

- At least two neutrinos are massive \Rightarrow There is NP
- 3ν scenario: Robust determination of θ_{12} , θ_{13} , Δm_{21}^2 , $|\Delta m_{3\ell}^2|$
 - large lepton mixing very different from quark CKM
 - Mass ordering, θ_{23} Octant, CPV depend on subdominant 3ν -effects
 - \Rightarrow not statistically significant yet
 - \Rightarrow definitive answer will likely require new experiments
- More than 3ν light states?: Not coherently supported by SBL anomalies
- What about mass scale and Dirac vs Majorana?
 - Only model independent probe of m_ν β decay: $\sum m_i^2 |U_{ei}|^2 \leq (0.8 \text{ eV})^2$
 - Dirac or Majorana?: We do not know, anxiously waiting for ν -less $\beta\beta$ decay
 - Cosmological effects?: No signal yet
- Other NP at play? Only subdominant allowed. But for NSI
 - No hint in present experiments \Rightarrow bounds on effects at future experiments
 - But degenerate solution Dark-LMA not excluded
 - Bounds on flavoured dark-photon/Z' models
- What about a UV complete model which answers?:
 - Why are neutrinos so light? \equiv The Origin of Neutrino Mass
 - Why are lepton mixing so different from quark's? \equiv The Flavour Puzzle

Answer will require some positive signal in colliders, CLFV ... experiments

THANK YOU

BACK-UP SLIDES

Summary: Global 3 ν Flavour Parameters

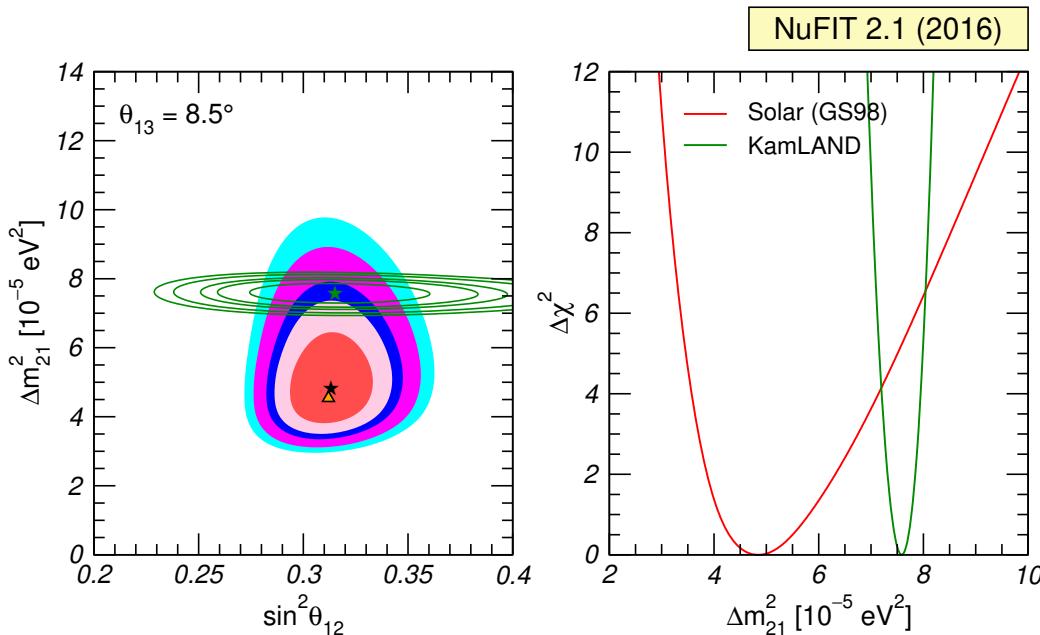
Evolution of global 3 flavour fit

Gonzalez-Garcia, Maltoni, TS [arXiv:2111.03086]

	2012 NuFIT 1.0	2014 NuFIT 2.0	2016 NuFIT 3.0	2018 NuFIT 4.0	2021 NuFIT 5.1	
θ_{12}	15%	14%	14%	14%	14%	1.07
θ_{13}	30%	15%	11%	8.9%	9.0%	3.3
θ_{23}	43%	32%	32%	27%	27%	1.6
Δm_{21}^2	14%	14%	14%	16%	16%	0.88
$ \Delta m_{3\ell}^2 $	17%	11%	9%	7.8%	6.7% [6.5%]	2.5
δ_{CP}	100%	100%	100%	100% [92%]	100% [83%]	1 [1.2]
$\Delta\chi^2_{IO-NO}$	± 0.5	-0.97	+0.83	+4.7 [+9.3]	+2.6 [+7.0]	
↑						
w/o [w] SK atm data						
improvement factor from 2012 to 2021						

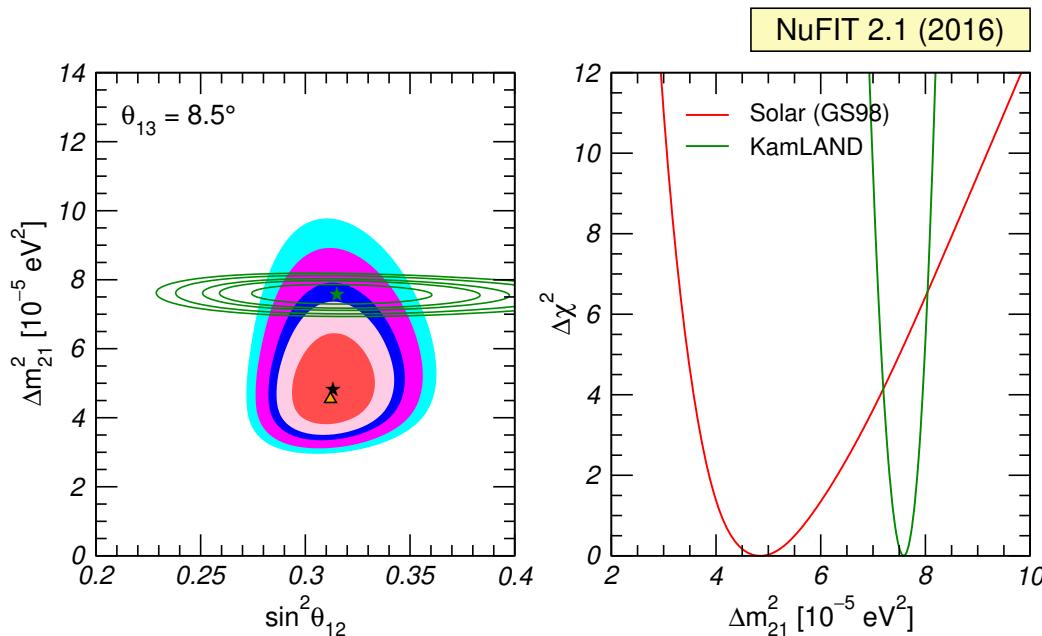
relat. precision at 3σ :
$$\frac{2(x^+ - x^-)}{(x^+ + x^-)}$$

- Last decade: after including $\theta_{13} \simeq 9^\circ$ the comparison of KamLAND vs Solar



θ_{12} better than 1σ agreement
But $\sim 2\sigma$ tension on Δm_{12}^2

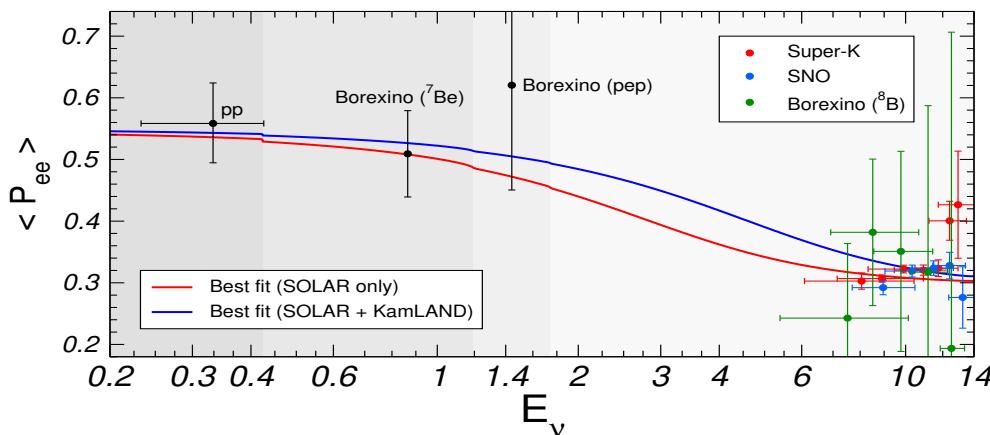
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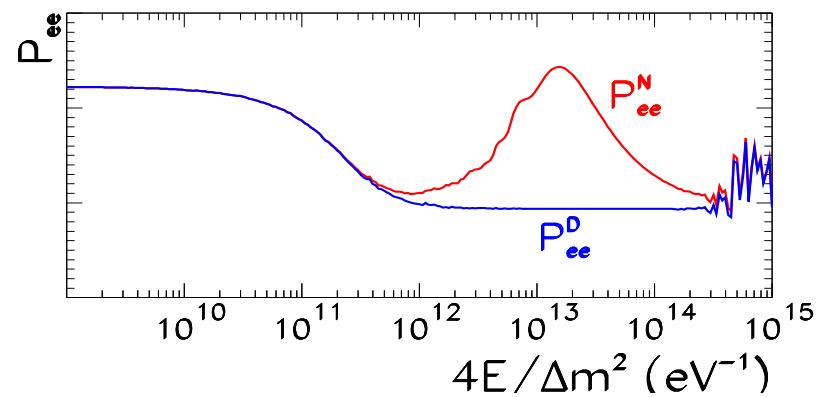
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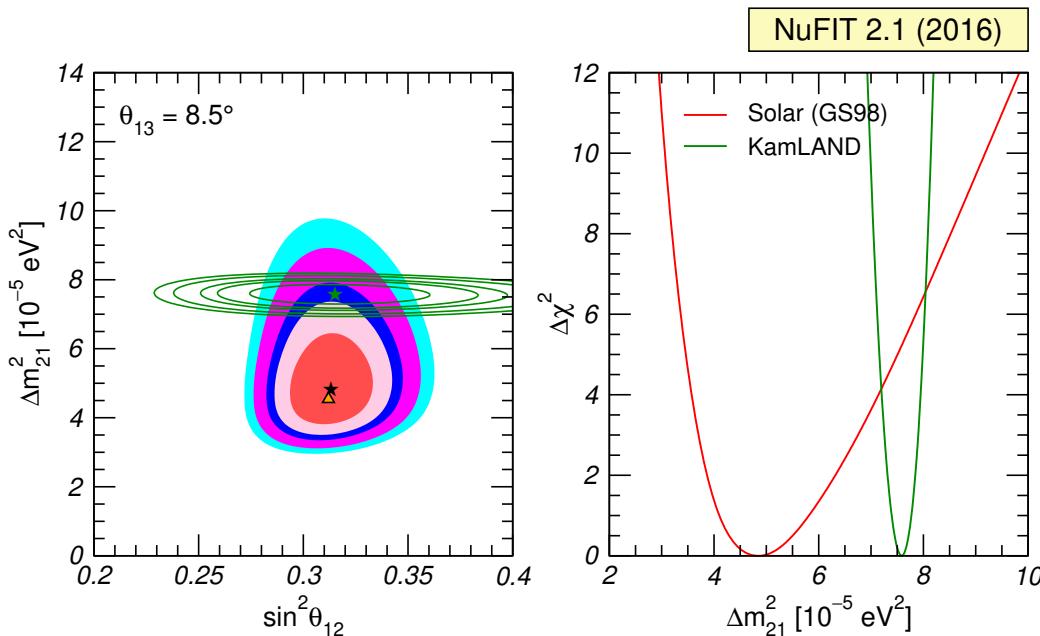
Smaller-than-expected MSW low-E turn-up
in SK/SNO spectrum at global b.f.



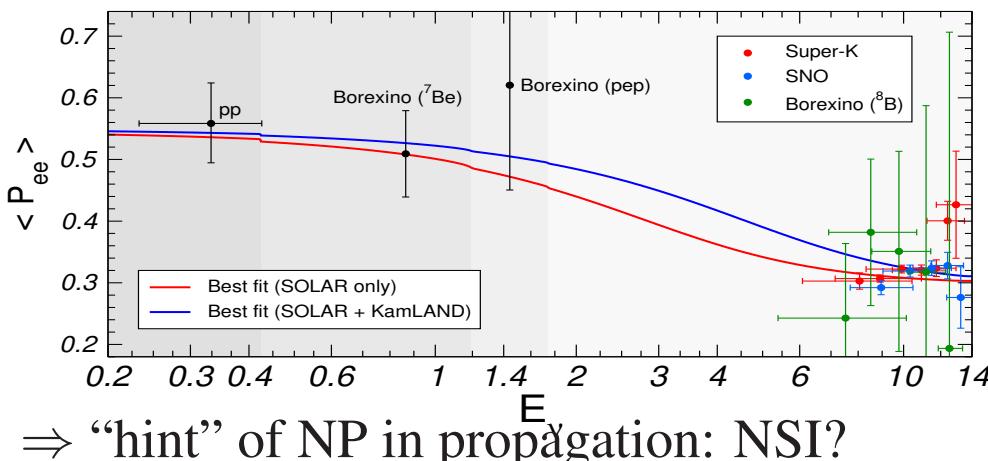
“too large” of Day/Night at SK
 $A_{D/N, SK4-2055} = [-3.1 \pm 1.6(\text{stat.}) \pm 1.4(\text{sys.})]\%$



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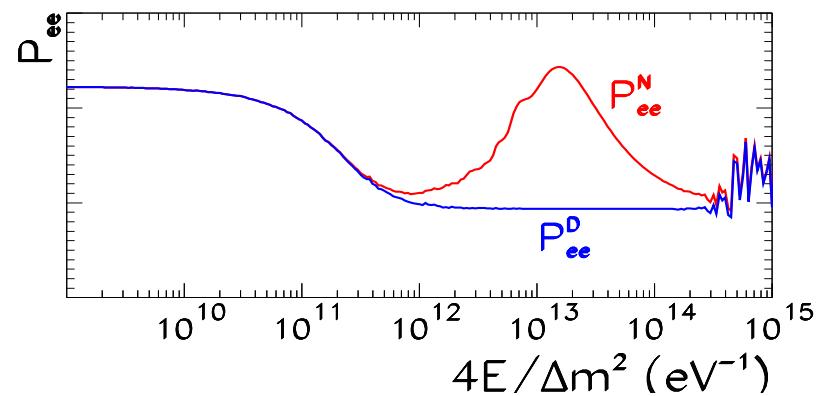


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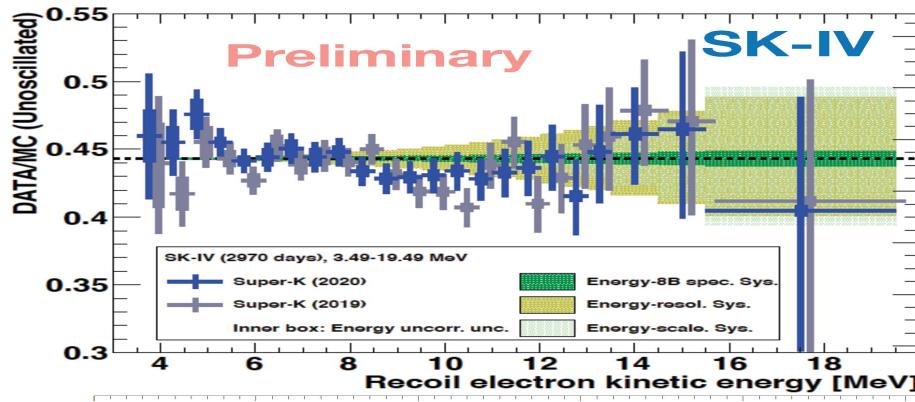
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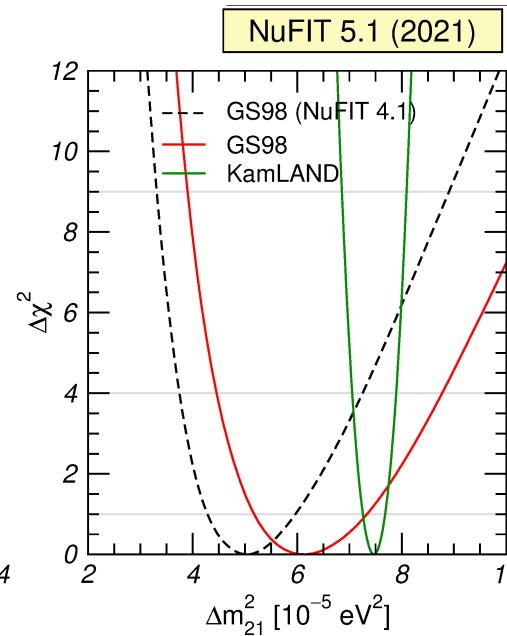
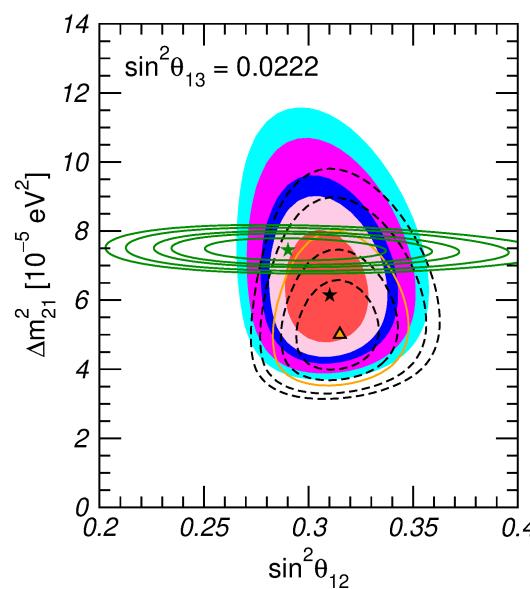


- AFTER NU2020: With SK4 2970 days data

Slightly more pronounced low-E turn-up



- In NuFIT 5.1



\Rightarrow Agreement of Δm_{21}^2 between solar and KamLAND at 1 σ

Smaller of Day/Night at

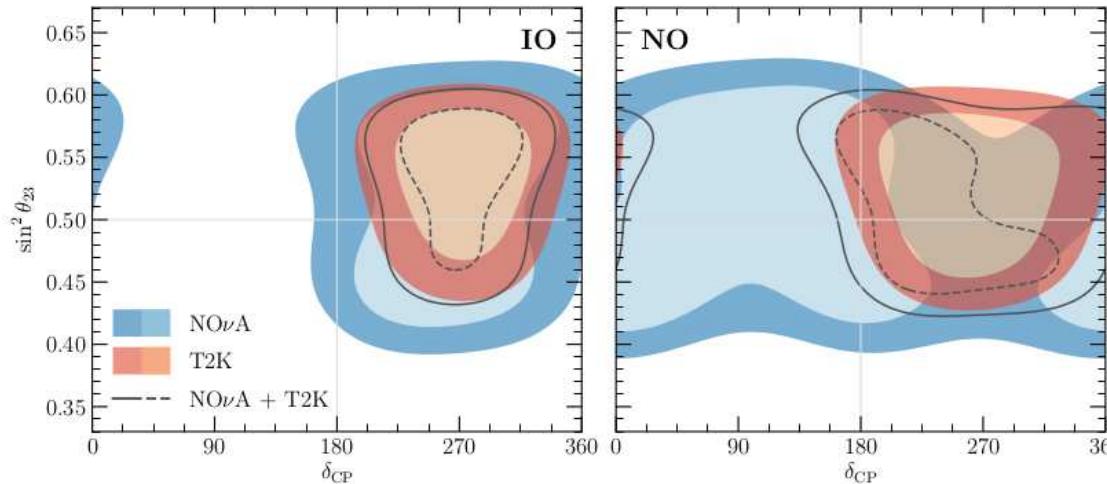
$$A_{D/N, SK4-2055} = [-3.1 \pm 1.6(\text{stat.}) \pm 1.4(\text{sys.})]\%$$

$$A_{D/N, SK4-2970} = [-2.1 \pm 1.1]\%$$

Compatibility T2K/NO ν A

Concha Gonzalez-Garcia 60

- 1 and 2 σ (2dof) allowed regions (for $s_{13}^2 = 0.0224$, marg over $|\Delta m_{3\ell}^2|$)

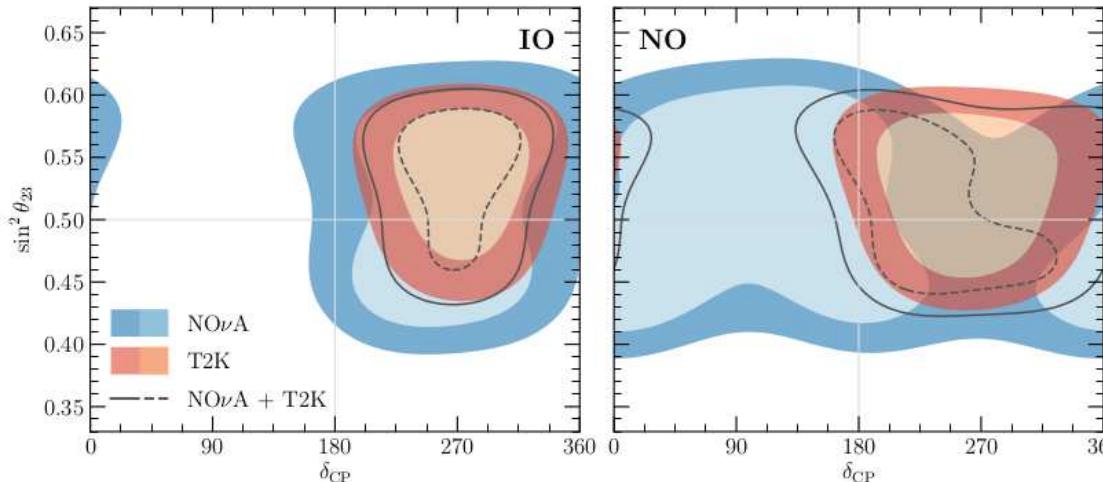


⇒ Better agreement in IO but NO 1σ regions “touch”

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oncha Gonzalez-Garcia 60-a

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- Parameter goodness-of-fit (PG) test:

	normal ordering			inverted ordering		
	χ^2_{PG}/n	p-value	# σ	χ^2_{PG}/n	p-value	# σ
T2K vs NOvA (θ_{13} free)	6.7/4	0.15	1.4 σ	3.6/4	0.46	0.7 σ
T2K vs NOvA (θ_{13} fix)	6.5/3	0.088	1.7 σ	2.8/3	0.42	0.8 σ

No significant
incompatibility

Leptonic CP Violation

- Leptonic CP $\Rightarrow P_{\nu_\alpha \rightarrow \nu_\beta} \neq P_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta}$:

$$P_{\nu_\alpha \rightarrow \nu_\beta} - P_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta} \propto J \quad \text{with} \quad J = \text{Im}(U_{\alpha 1} U_{\alpha 2}^* U_{\beta 2} U_{\beta 1}^*) = J_{\text{LEP,CP}}^{\max} \sin \delta_{\text{CP}}$$

$$J_{\text{LEP,CP}}^{\max} = \frac{1}{8} c_{13} \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 2\theta_{12}$$

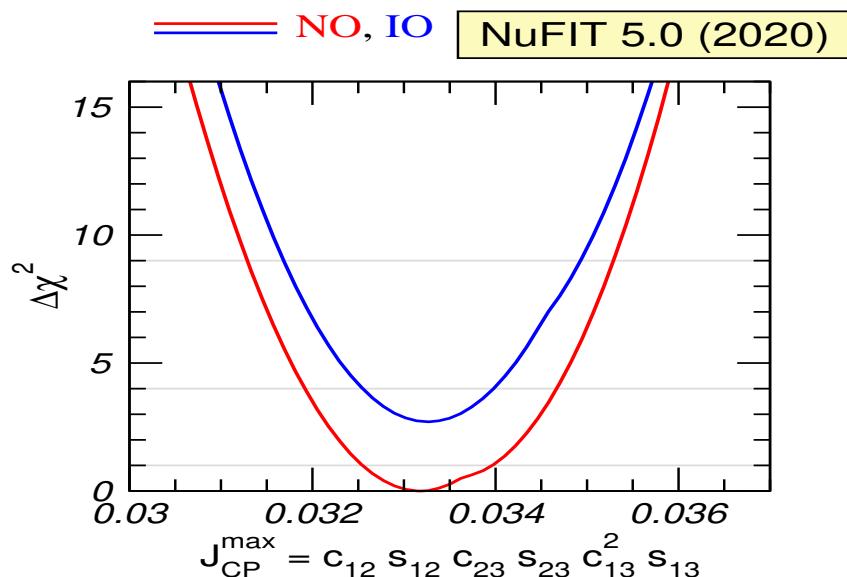
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$$J_{\text{LEP,CP}}^{\max} = \frac{1}{8} c_{13} \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 2\theta_{12}$$

- Maximum Allowed Leptonic CPV:



$$J_{\text{LEP,CP}}^{\max} = (3.29 \pm 0.07) \times 10^{-2}$$

to compare with

$$J_{\text{CKM,CP}} = (3.04 \pm 0.21) \times 10^{-5}$$

\Rightarrow Leptonic CPV may be largest CPV
in New Minimal SM

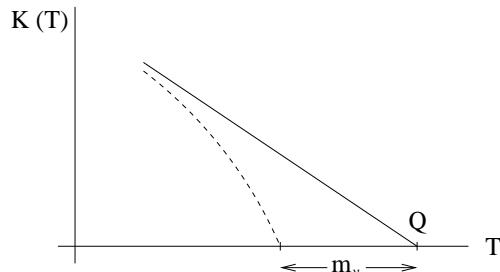
if $\sin \delta_{\text{CP}}$ not too small

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Neutrino Mass Scale: β Decay

Single β decay : Dirac or Majorana ν mass modify spectrum endpoint



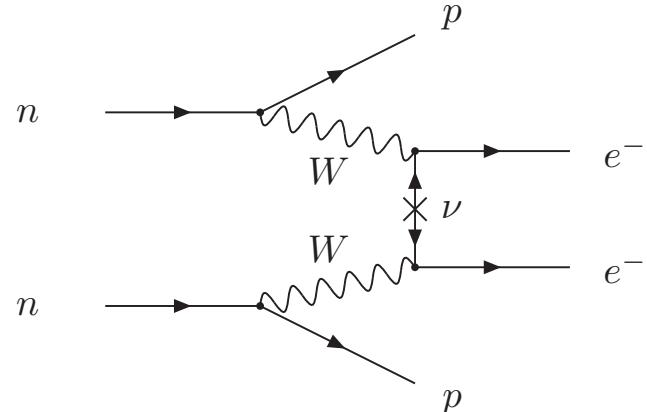
$$m_{\nu_e}^2 = \sum m_j^2 |U_{ej}|^2$$

Purely kinematics \Rightarrow Only model independent probe ν -mass scale

KATRIN: $m_{\nu_e} \leq 0.8$ eV (at 90 % CL)

Majorana or Dirac: $0\nu\beta\beta$ Decay

$0\nu\beta\beta \Rightarrow L$ violation \Leftrightarrow Majorana ν



If m_ν only source of ΔL

$$\left(T_{1/2}^{0\nu}\right)^{-1} = G^{0\nu} M_{\text{nucl}}^2 m_{ee}^2$$

$$m_{ee} = \left| \sum U_{ej}^2 m_j \right|$$

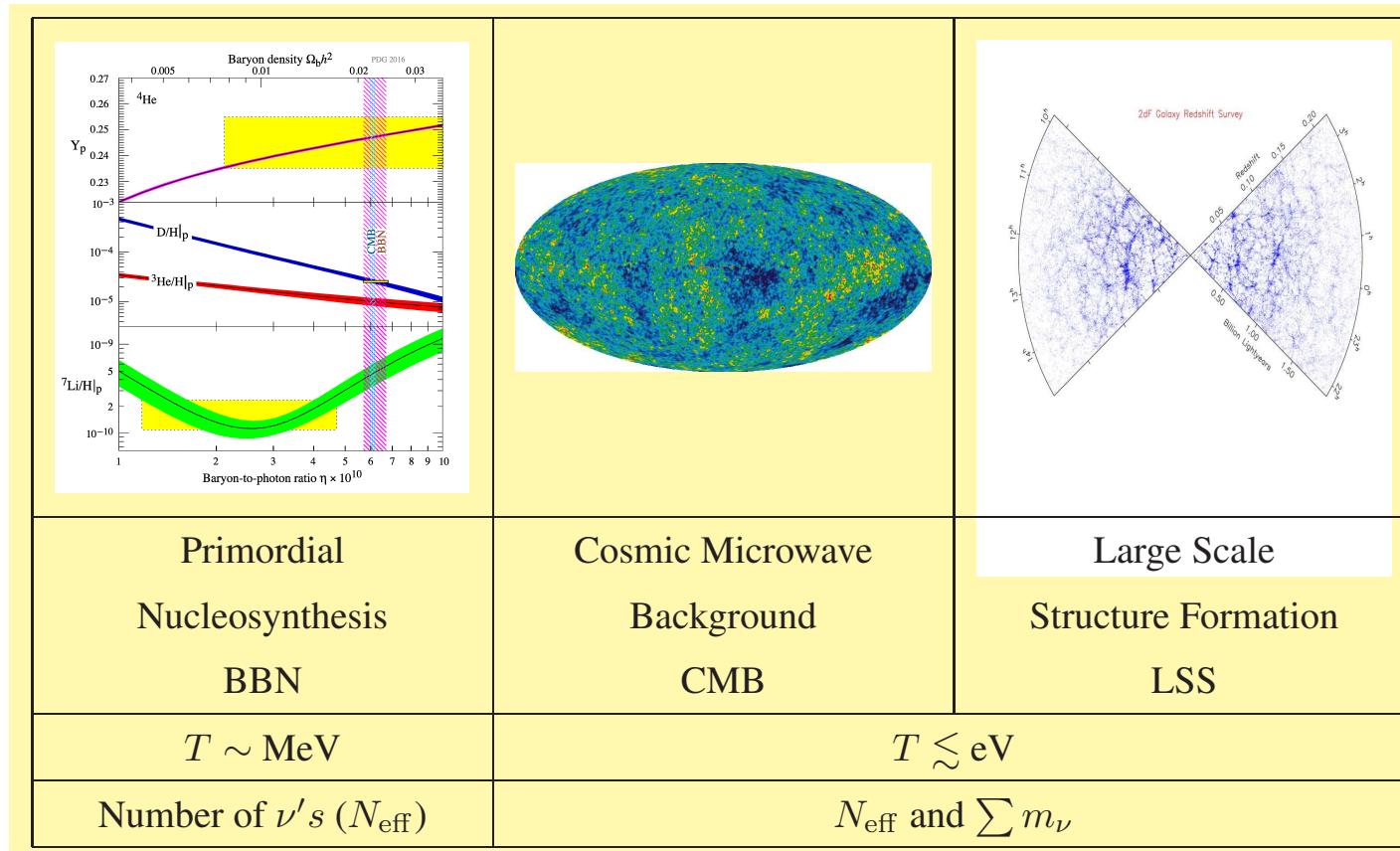
At present only bounds

Isotope	Experiment	year	$T_{1/2}$ limit (yr)	m_{ν} (meV)
^{76}Ge	GERDA	2020	1.8×10^{26}	79 – 180
^{76}Ge	MAJORANA DEMONSTRATOR	2019	2.7×10^{25}	200 – 433
^{136}Xe	KamLAND-Zen	2022	2.3×10^{26}	36 – 156
^{136}Xe	EXO-200	2019	3.5×10^{25}	93 – 286
^{130}Te	CUORE	2022	2.2×10^{25}	90 – 305

Light massive ν in Cosmology

Relic ν' s: Effects in several cosmological observations at several epochs

Mainly via two effects: $\rho_r = \left[1 + \frac{7}{8} \times \left(\frac{4}{11} \right)^{\frac{4}{3}} N_{\text{eff}} \right] \rho_\gamma$ and $\sum_i m_{\nu_i}$

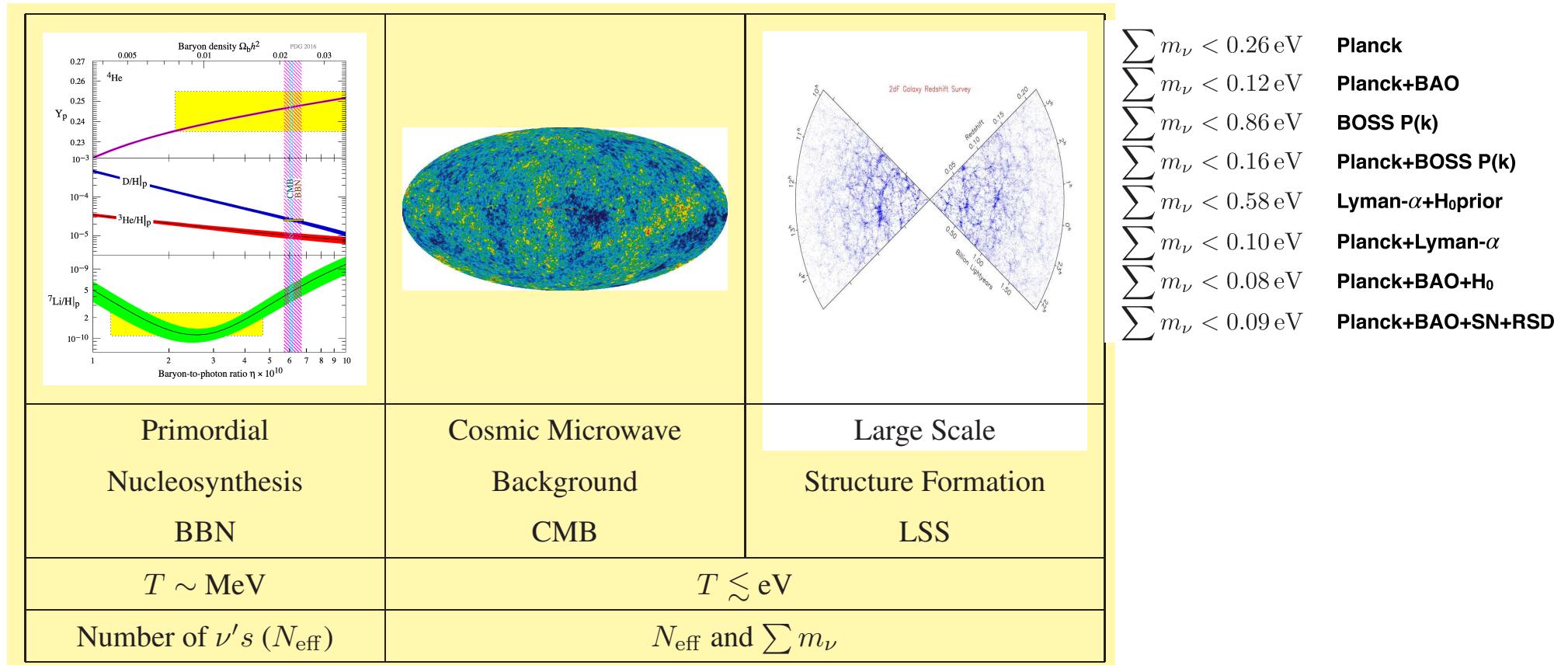


BUT: Observables also depend on all other cosmo parameters (and assumptions)

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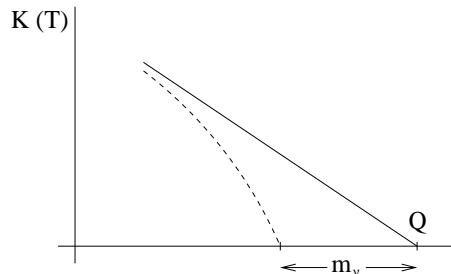
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BUT: Observables also depend on all other cosmo parameters (and assumptions)

Probes of Mass Scale in 3ν -mixing

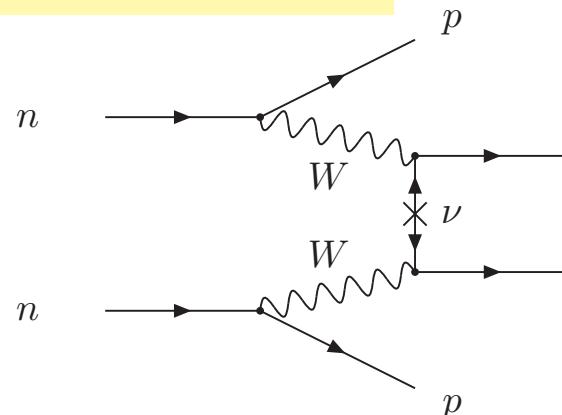
Single β decay : Pure kinematics, Dirac or Majorana ν 's, only model independent



$$m_{\nu_e}^2 = \sum m_j^2 |U_{ej}|^2 = \begin{cases} \text{NO : } m_\ell^2 + \Delta m_{21}^2 c_{13}^2 s_{12}^2 + \Delta m_{31}^2 s_{13}^2 \\ \text{IO : } m_\ell^2 + \Delta m_{21}^2 c_{13}^2 s_{12}^2 - \Delta m_{31}^2 c_{13}^2 \end{cases}$$

Present bound: $m_{\nu_e} \leq 0.8$ eV (90% CL KATRIN 2022)
^TKatrin (20XX) Sensitivity to $m_{\nu_e} \sim 0.2$ eV

ν -less Double- β decay: \Leftrightarrow Majorana ν 's



If m_ν only source of ΔL : $(T_{1/2}^{0\nu})^{-1} = G^{0\nu} M_{\text{nucl}}^2 m_{ee}^2$

$$m_{ee} = \left| \sum U_{ej}^2 m_j \right|$$

$$\begin{aligned} &= \left| c_{13}^2 c_{12}^2 m_1 e^{i\eta_1} + c_{13}^2 s_{12}^2 m_2 e^{i\eta_2} + s_{13}^2 m_3 e^{-i\delta_{CP}} \right| \\ &= f(m_\ell, \text{order, maj phases}) \end{aligned}$$

Present Bounds: $m_{ee} < 0.04\text{--}0.5$ eV

COSMO for Dirac or Majorana
 m_ν affect growth of structures

$$\sum m_i = \begin{cases} \text{NO : } \sqrt{m_\ell^2} + \sqrt{\Delta m_{21}^2 + m_\ell^2} + \sqrt{\Delta m_{31}^2 + m_\ell^2} \\ \text{IO : } \sqrt{m_\ell^2} + \sqrt{-\Delta m_{31}^2 - \Delta m_{21}^2 - m_\ell^2} + \sqrt{-\Delta m_{31}^2 - m_\ell^2} \end{cases}$$

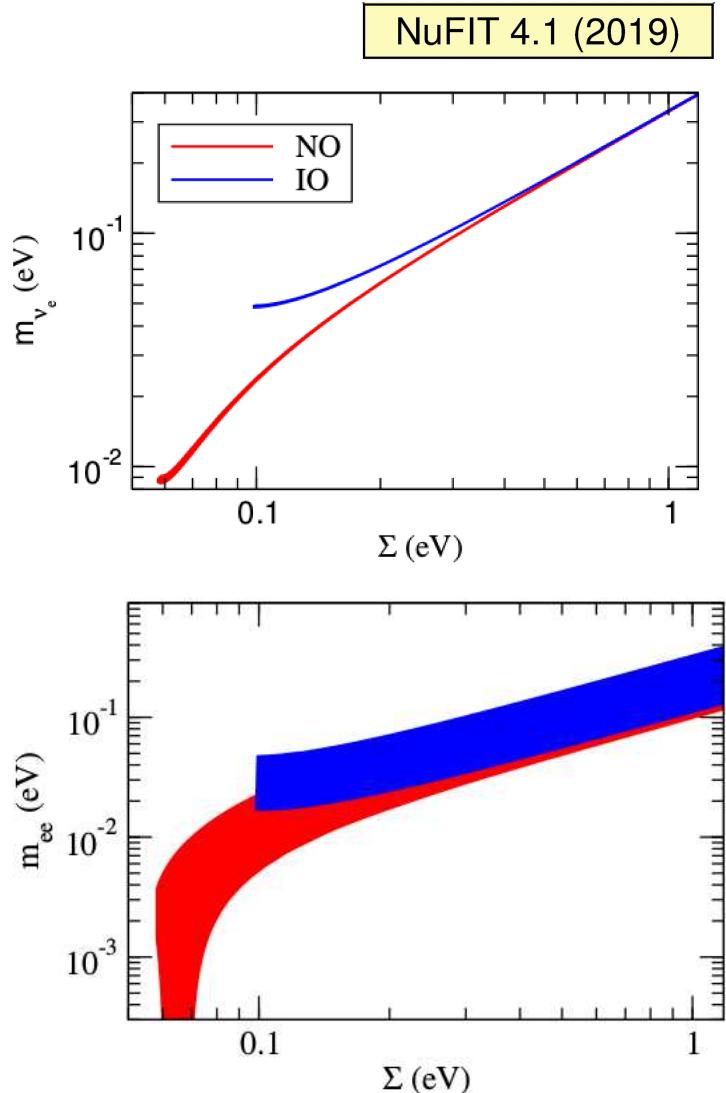
Neutrino Mass Scale: The Cosmo-Lab Connection

67

Global oscillation analysis \Rightarrow Correlations m_{ν_e} , m_{ee} and $\sum m_\nu$ (Fogli *et al* (04))

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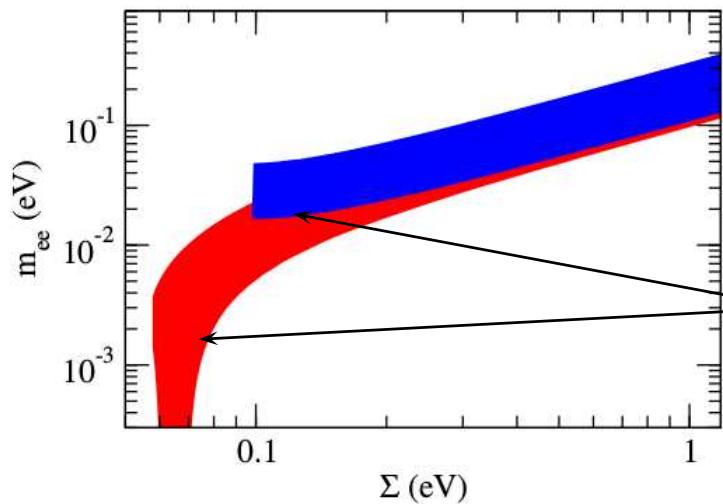
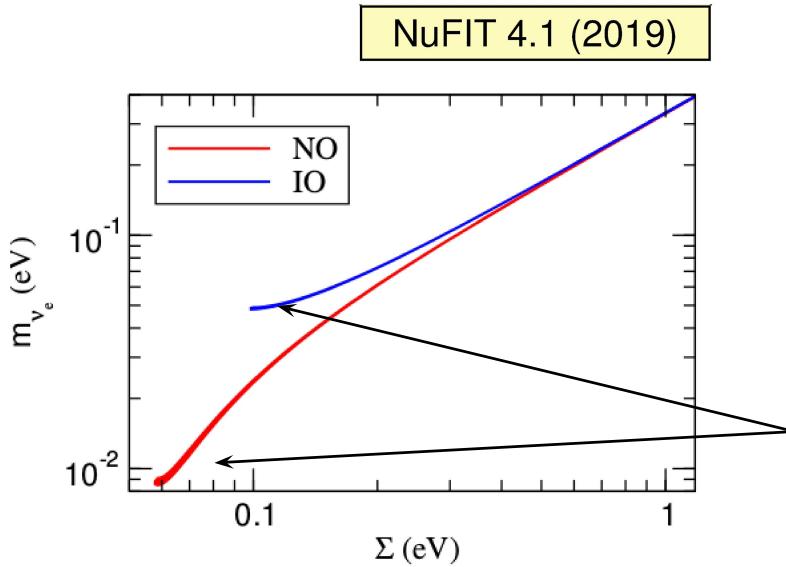
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-b

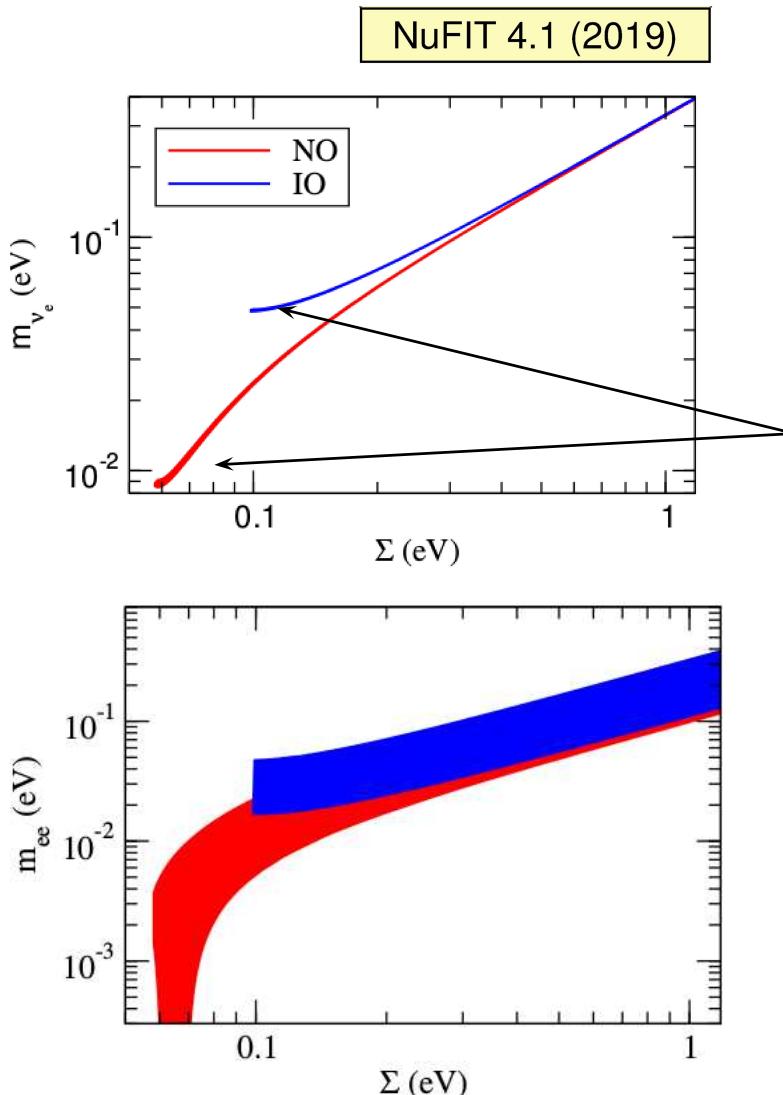
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Lower bound on $\sum m_i$ depends on ordering

Precision determination/bound of $\sum m_i$ can give information on ordering ?

Hannestad, Schwetz 1606.04691, Simpson et al 1703.03425, Capozzi et al 1703.04471 ...

Cosmo data will only add to N/I likelihood
when accuracy on $\sum m_\nu$ better than 0.02 eV
(to see a 2σ N/I difference between 0.06 and 0.1)

Hannestad, Schwetz 1606.04691

Alternative Oscillation Mechanisms

- Oscillations are due to:
 - Misalignment between CC-int and propagation states: Mixing \Rightarrow Amplitude
 - Difference phases of propagation states \Rightarrow Wavelength. For Δm^2 -OSC $\lambda = \frac{4\pi E}{\Delta m^2}$

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- ν masses are not the only mechanism for oscillations

Violation of Equivalence Principle (VEP): Gasperini 88, Halprin,Leung 01

Non universal coupling of neutrinos $\gamma_1 \neq \gamma_2$ to gravitational potential ϕ

Violation of Lorentz Invariance (VLI): Coleman, Glashow 97

Non universal asymptotic velocity of neutrinos $c_1 \neq c_2 \Rightarrow E_i = \frac{m_i^2}{2p} + c_i p$

Interactions with space-time torsion: Sabbata, Gasperini 81

Non universal couplings of neutrinos $k_1 \neq k_2$ to torsion strength Q

Violation of Lorentz Invariance (VLI) Colladay, Kostelecky 97; Coleman, Glashow 99

due to CPT violating terms: $\bar{\nu}_L^\alpha b_\mu^{\alpha\beta} \gamma_\mu \nu_L^\beta \Rightarrow E_i = \frac{m_i^2}{2p} \pm b_i$

$$\lambda = \frac{4\pi E}{\Delta m^2}$$

$$\lambda = \frac{\pi}{E|\phi|\delta\gamma}$$

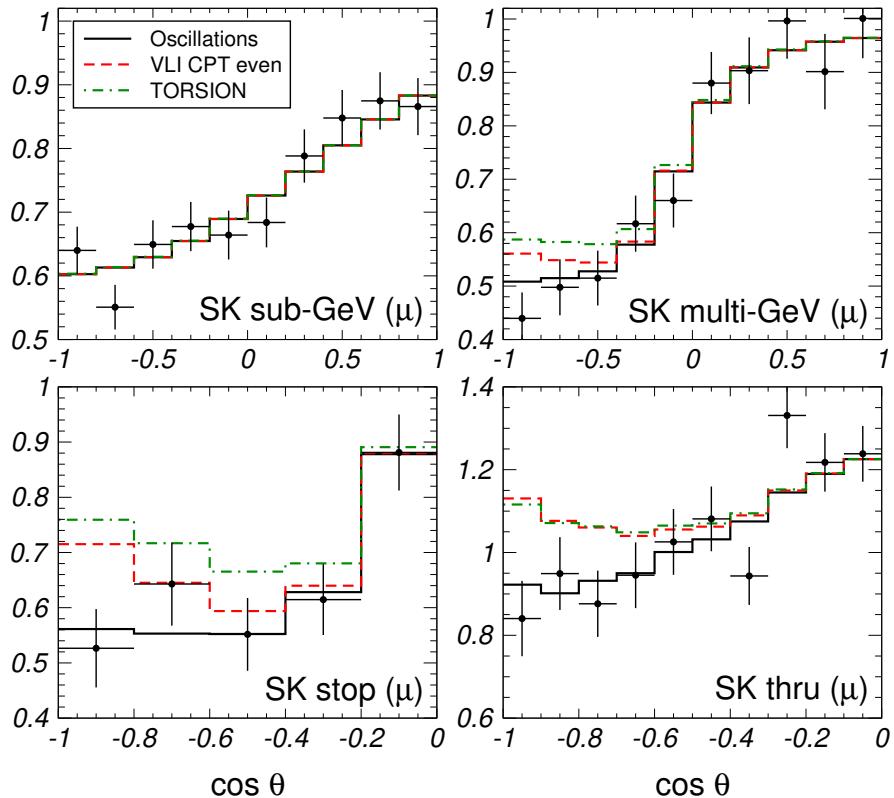
$$\lambda = \frac{2\pi}{E\Delta c}$$

$$\lambda = \frac{2\pi}{Q\Delta k}$$

$$\lambda = \pm \frac{2\pi}{\Delta b}$$

Alternative Mechanisms vs ATM ν 's

Severely constrained (MCG-G, M. Maltoni PRD 04,07)



$$\frac{|\Delta c|}{c} \leq 1.2 \times 10^{-24}$$

$$|\phi \Delta \gamma| \leq 5.9 \times 10^{-25}$$

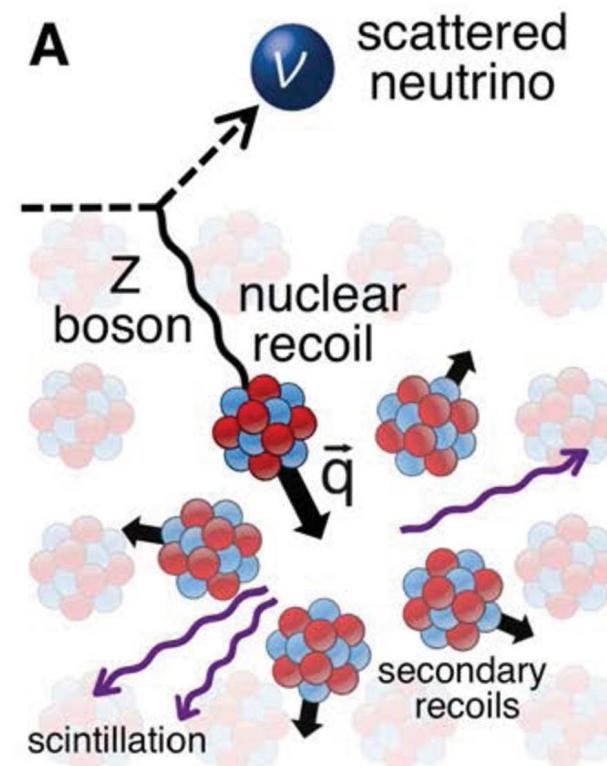
At 90% CL: $|Q \Delta k| \leq 4.8 \times 10^{-23} \text{ GeV}$

$$|\Delta b| \leq 3.0 \times 10^{-23} \text{ GeV}$$

COHERENT EXPERIMENT

Science 2017 [ArXiv:1708.01294]

- observation of coherent neutrino-nucleus scattering at 6.7σ at CsI[Na] detector
- neutrinos from stopped pion source at Oak Ridge NL
- 142 events observed, in agreement with Standard Model



NSI: Combination with COHERENT data

Coloma, MCGG, Maltoni,Schwetz ArXiv:1708.02899

- COHERENT has detected for first time Coherent νN scattering [1708.01294](#):
 142($1 \pm 0.28(\text{sys})$) observed events over a steady bck of 405
 136(SM) + 6($1 \pm 0.25(\text{sys})$) beam-on bck) expected
- In presence of NSI: $N_{\text{NSI}}(\varepsilon) = \gamma [f_{\nu_e} Q_{we}^2(\varepsilon) + (f_{\nu_\mu} + f_{\bar{\nu}_\mu}) Q_{w\mu}^2(\varepsilon)]$

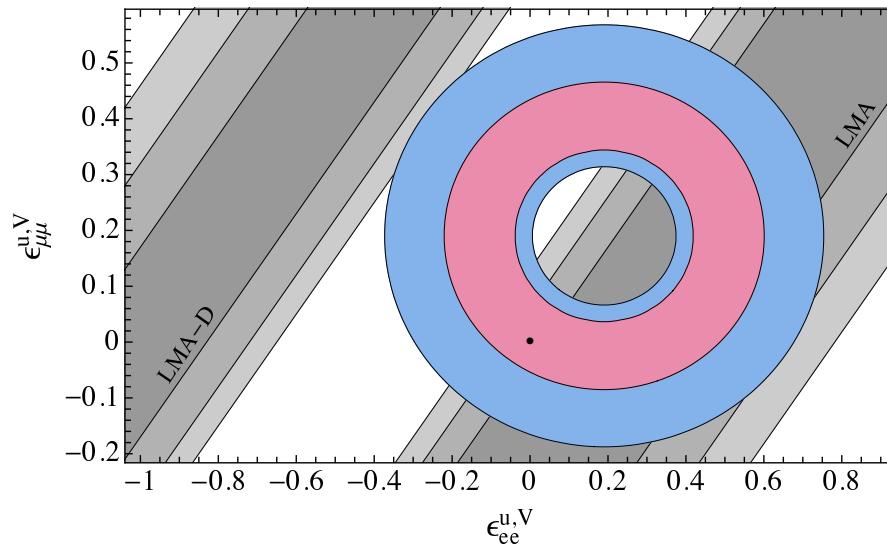
$$Q_{w\alpha}^2 \propto [Z(g_p^V + 2\varepsilon_{\alpha\alpha}^{u,V} + \varepsilon_{\alpha\alpha}^{d,V}) + N(g_n^V + \varepsilon_{\alpha\alpha}^{u,V} + 2\varepsilon_{\alpha\alpha}^{d,V})]^2 + \sum_{\beta \neq \alpha} [Z(2\varepsilon_{\alpha\beta}^{u,V} + \varepsilon_{\alpha\beta}^{d,V}) + N(\varepsilon_{\alpha\beta}^{u,V} + 2\varepsilon_{\alpha\beta}^{d,V})]^2$$

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- Impact on LMA-D: Allowed COHERENT region vs LMA-D required range



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- OSCILLATION + COHERENT \Rightarrow LMA-D excluded at more than 3.1σ

All NSI's constrained

	$f = u$	$f = d$
$\epsilon_{ee}^{f,V}$	[0.028, 0.60]	[0.030, 0.55]
$\epsilon_{\mu\mu}^{f,V}$	[-0.088, 0.37]	[-0.075, 0.33]
$\epsilon_{\tau\tau}^{f,V}$	[-0.090, 0.38]	[-0.075, 0.33]
$\epsilon_{e\mu}^{f,V}$	[-0.073, 0.044]	[-0.07, 0.04]
$\epsilon_{e\tau}^{f,V}$	[-0.15, 0.13]	[-0.13, 0.12]
$\epsilon_{\mu\tau}^{f,V}$	[-0.01, 0.009]	[-0.009, 0.008]

