

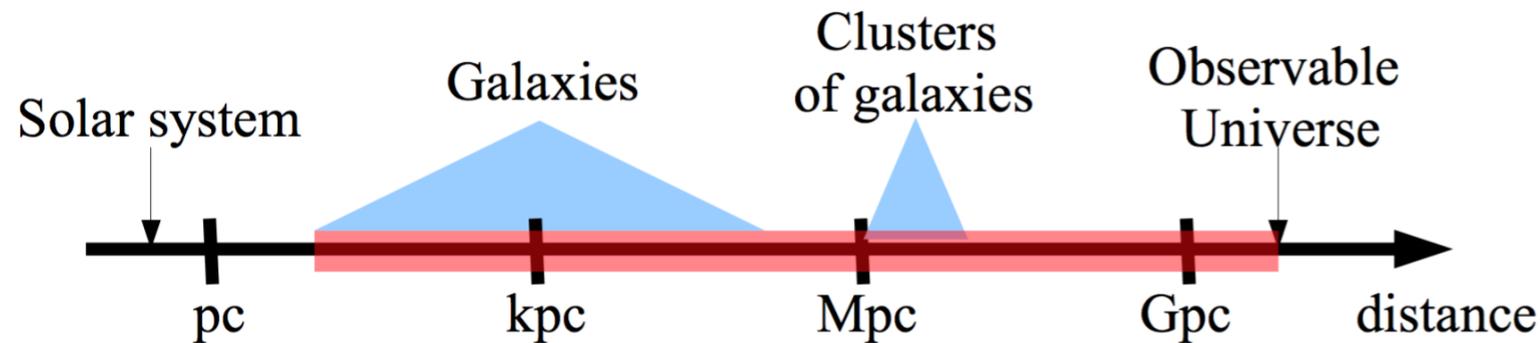
Unravelling the mysteries of dark matter

Suchita Kulkarni

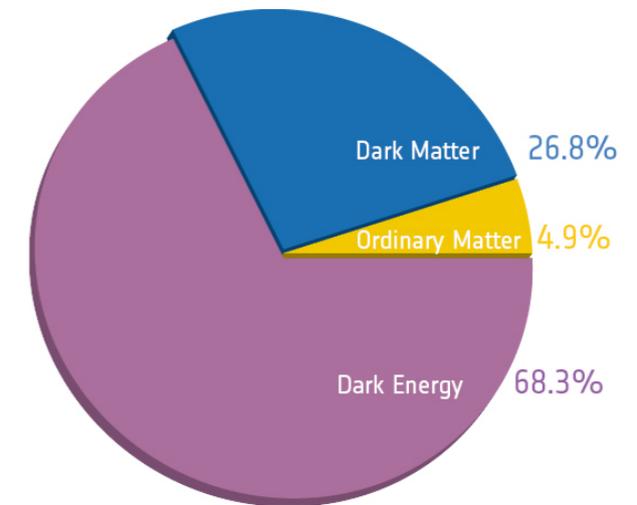
Elise - Richter Fellow
HEPHY, Vienna

 @suchi_kulkarni

- Strong evidence on all scales



- Precise measurements of relic density



After Planck

- But apart from that...

DARK MATTER

$$J = ?$$

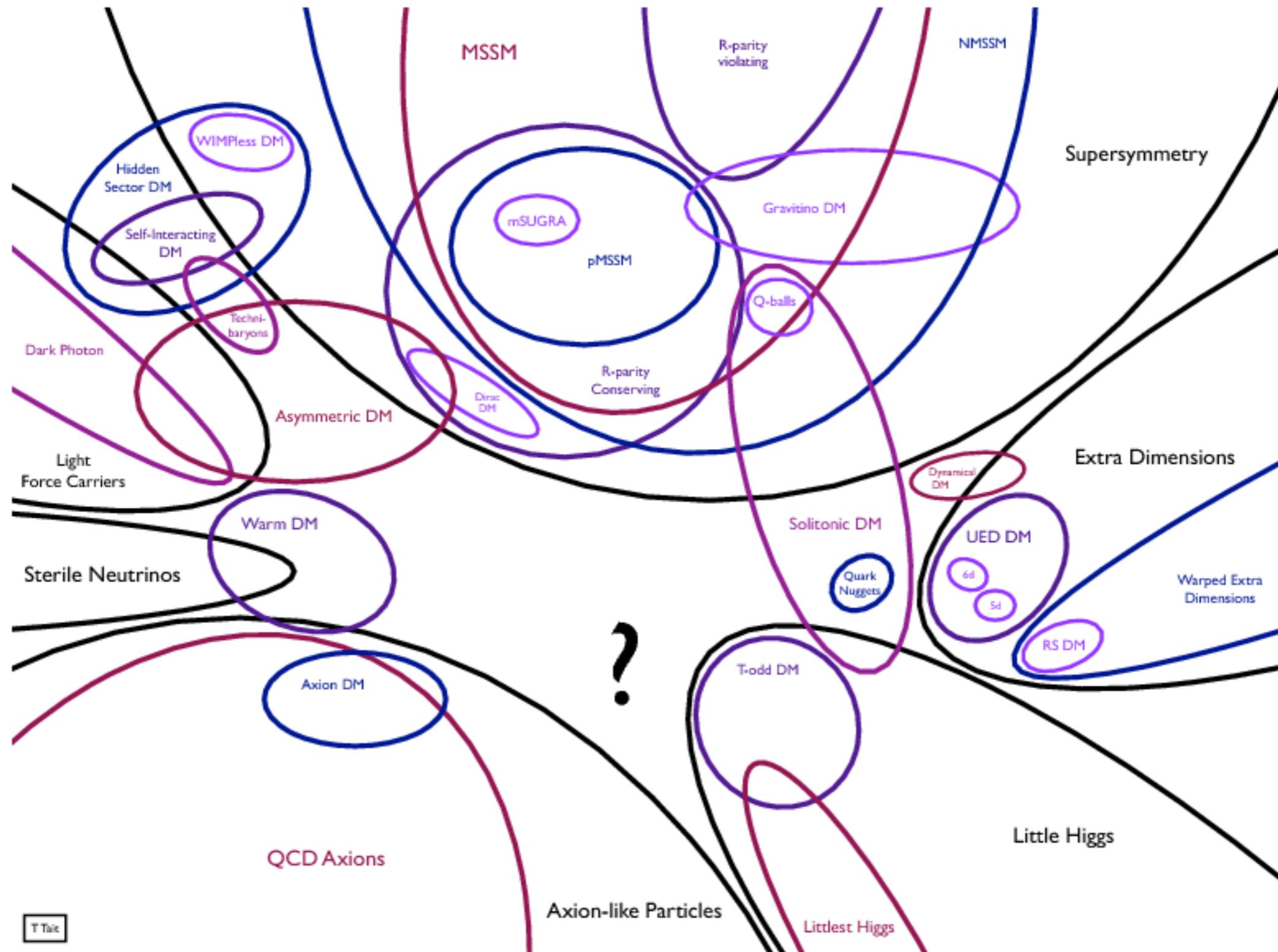
Mass $m = ?$
Mean life $\tau = ?$

| DECAY MODES | Fraction (Γ_i/Γ) | Confidence level | ρ (MeV/c) |
|-------------|--------------------------------|------------------|----------------|
| ? | ? | ? | ? |

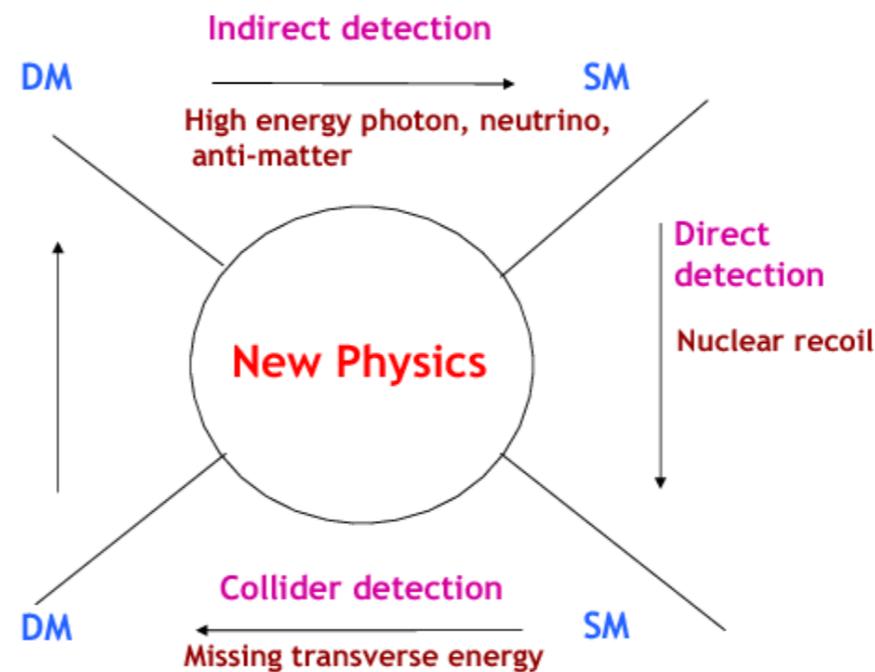
Goal for 21st century:
identify the properties of
dark matter

~85% all matter in the Universe is dark matter

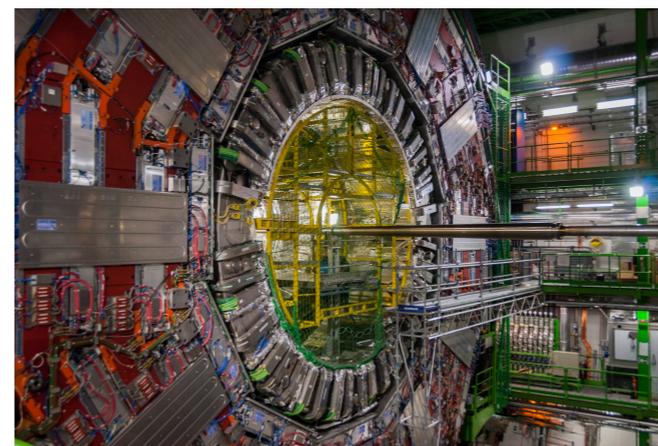
Slide inspired by A. Ibarra's talk



1. Potential signatures at multiple experiments
 - Cross-correlate signatures
 2. Future experimental searches are in pipeline
 - Demonstrate their potential
 3. Is there something we are missing?
 - Suggest new signatures
- Stay as model independent as possible



@HEPHY



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Cross-correlate signatures

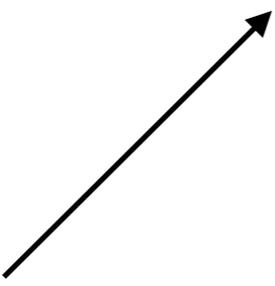
LHC master formula for searches

$$N_{events} = \mathcal{L} \times \mathcal{A} \times \epsilon \times \sigma \times BR$$

LHC master formula for searches

$$N_{evts} = \mathcal{L} \times \mathcal{A} \times \epsilon \times \sigma \times BR$$

Final observable



LHC master formula for searches

$$N_{evts} = \mathcal{L} \times \mathcal{A} \times \epsilon \times \sigma \times BR$$



Integrated luminosity

LHC master formula for searches

$$N_{evts} = \mathcal{L} \times \mathcal{A} \times \epsilon \times \sigma \times BR$$

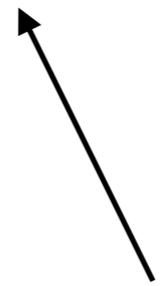


Depends on the detector geometry

LHC master formula for searches

$$N_{events} = \mathcal{L} \times \mathcal{A} \times \epsilon \times \sigma \times BR$$

Depends on the selection cuts



LHC master formula for searches

$$N_{evts} = \mathcal{L} \times \mathcal{A} \times \epsilon \times \sigma \times BR$$

Theory prediction
↑

LHC master formula for searches

$$N_{events} = \mathcal{L} \times \mathcal{A} \times \epsilon \times \sigma \times BR$$

LHC master formula for searches

$$N_{events} = \mathcal{L} \times \mathcal{A} \times \epsilon \times \sigma \times \text{BR}$$

$$\sigma \times \text{BR} = 0.1 \text{ fb}$$

$$\mathcal{L} = 30 \text{ fb}^{-1}$$

$$\mathcal{A} \times \epsilon = 0.001$$

$$\Rightarrow N_{events} = 0.003$$

LHC master formula for searches

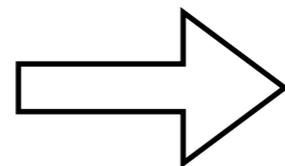
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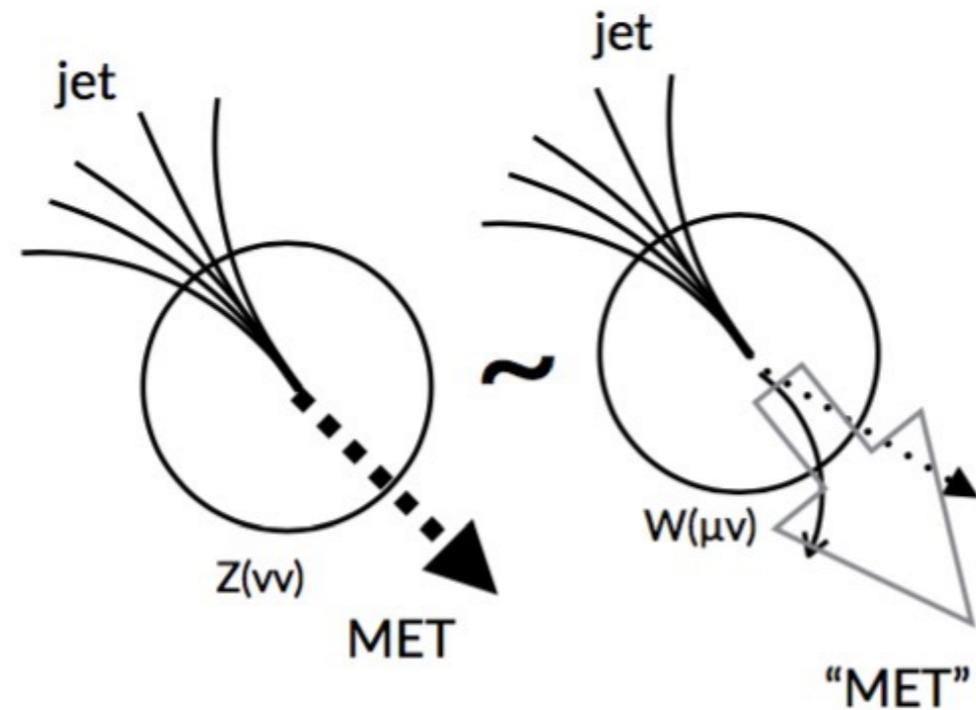
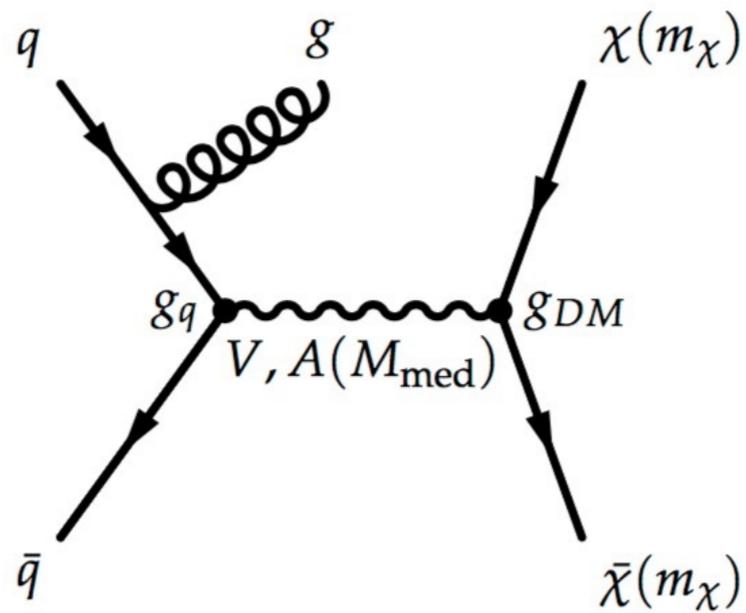
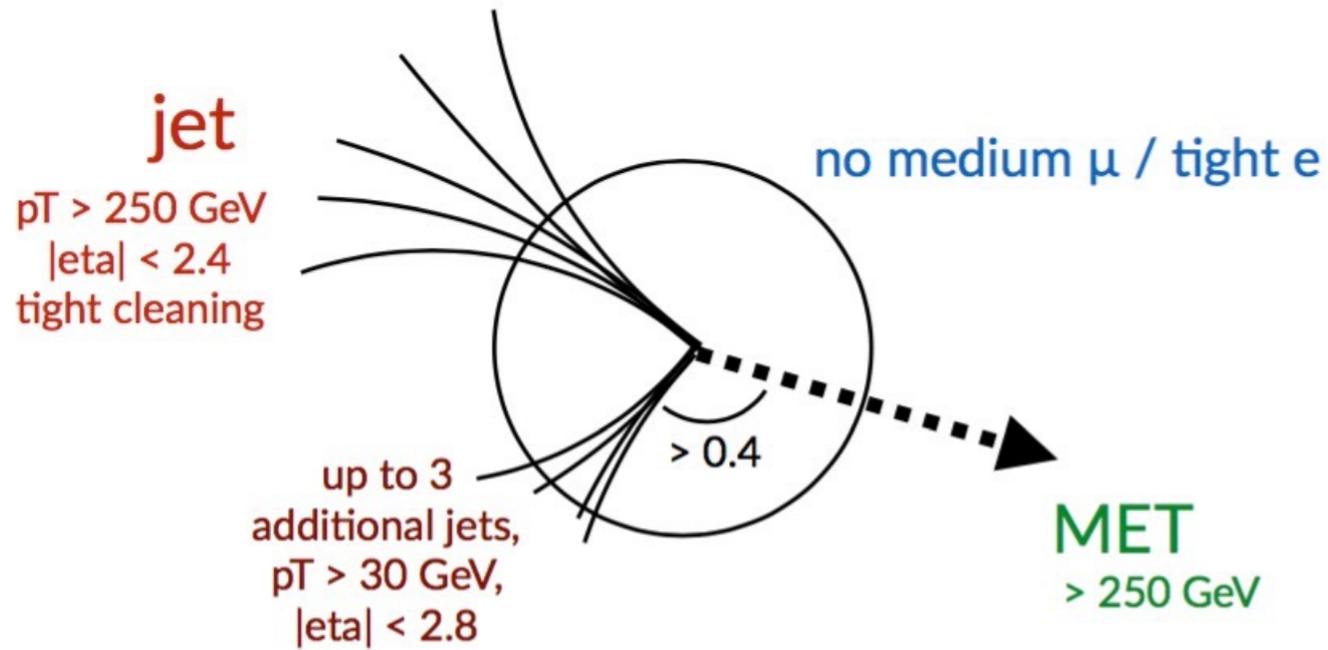
$$\Rightarrow N_{events} = 0.003$$



- For ideal detector there is some chance
- Hopeless to try to probe this cross section
- Situation better for higher luminosity

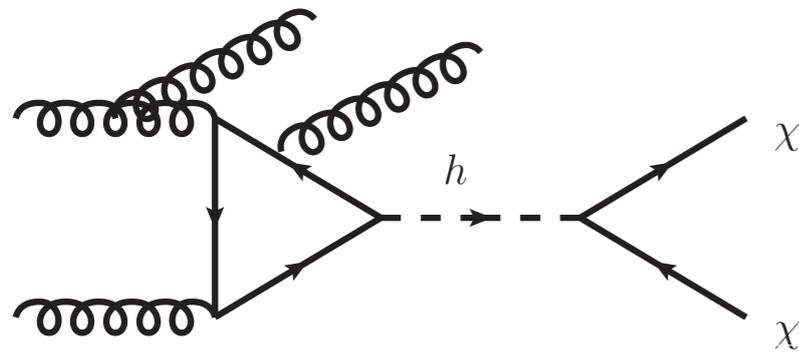
Figures courtesy A. Boveia's talk

- Signal regions with successively larger MET requirement

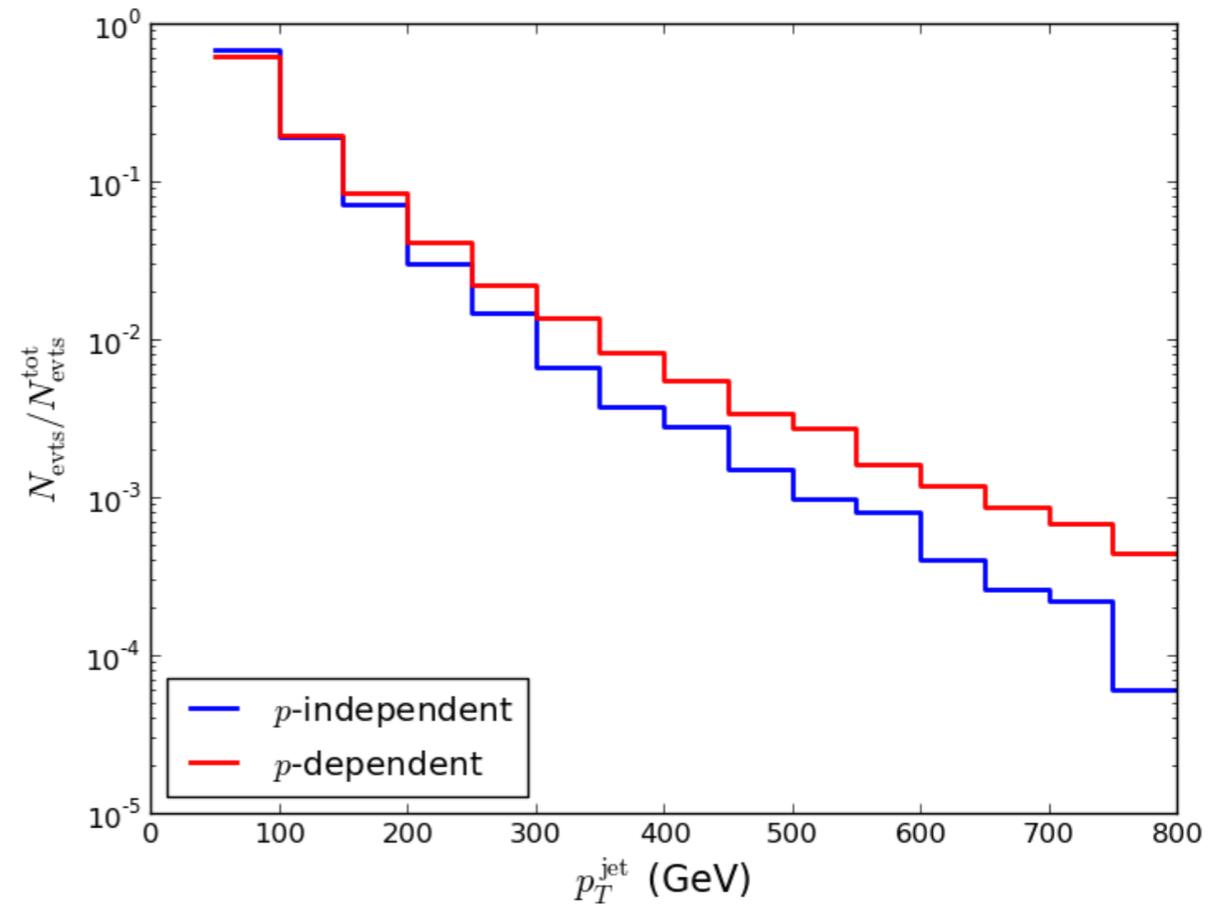


Kulkarni et al. JHEP 1701 (2017) 078

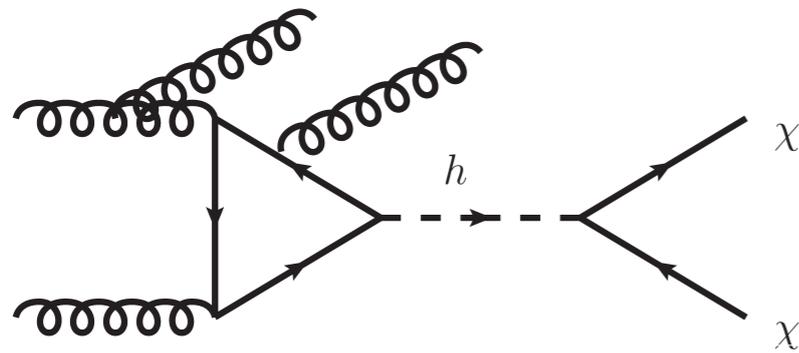
- Dark matter could be a pseudo Nambu Goldstone Boson appearing in the low energy theory as a result of the spontaneous breaking of a global symmetry by a new strong sector dynamics
- Strong sector dynamics can appear in the context of a new strongly-coupled sector above the TeV scale
- The analogy is the pion in QCD, the pions appear as Goldstone bosons of $q\bar{q}$ condensate breaking the chiral symmetry
- The shift symmetry of Goldstone bosons imply that their interactions are derivative (in the exact symmetry limit)
- What kind of phenomenological limits can be placed on such dark matter scenarios and what is the sensitivity of the LHC for these couplings?



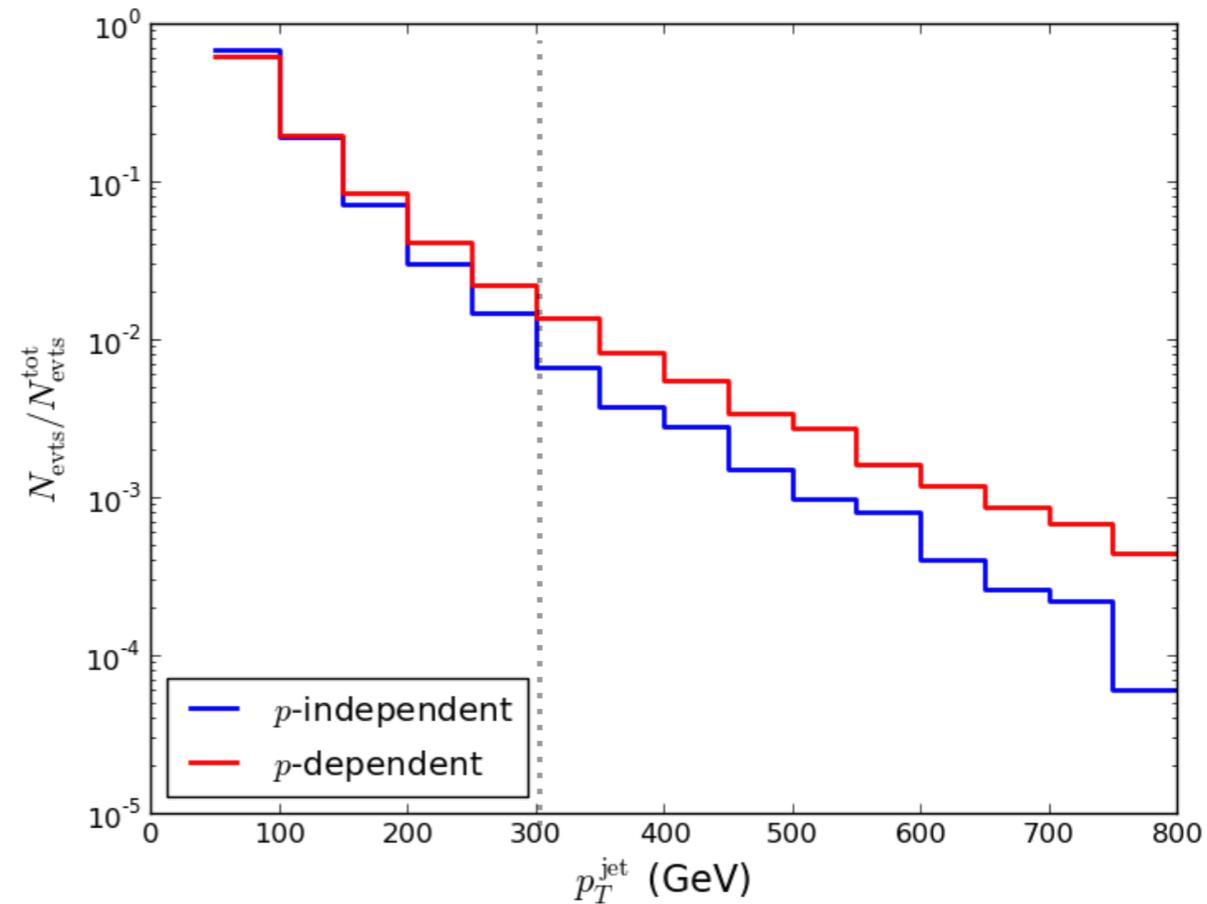
$$ig_{h\eta\eta} = 2iv \left[\lambda_{mi} + \frac{p_h^2}{f^2} \right]$$



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- Dark matter could be a pseudo Nambu Goldstone Boson appearing in the low energy theory as a result of the spontaneous breaking of a global symmetry by a new strong sector dynamics

- Extension of the Standard Model by gauge singlet real scalar field

$$\mathcal{L}_\eta = \mathcal{L}_{SM} + \frac{1}{2} \partial_\mu \eta \partial^\mu \eta - \frac{1}{2} \mu_\eta^2 \eta^2 - \frac{1}{4} \lambda_\eta \eta^4 - \frac{1}{2} \lambda \eta^2 H^\dagger H + \frac{1}{2f^2} (\partial_\mu \eta^2) \partial^\mu (H^\dagger H)$$

- After electroweak symmetry breaking

$$\mathcal{L}_\eta \supset -\frac{1}{4} (v + h)^2 \left(\lambda \eta^2 + \frac{1}{f^2} \partial_\mu \partial^\mu \eta^2 \right)$$

$$m_\eta^2 = \mu_\eta^2 + \lambda v^2 / 2$$

scale of spontaneous
symmetry breaking

Momentum dependent coupling

For mono-Higgs signature
study of similar model see e.g.
arXiv:1312.2592, arXiv:
1412.0258

- Monojet production cross section

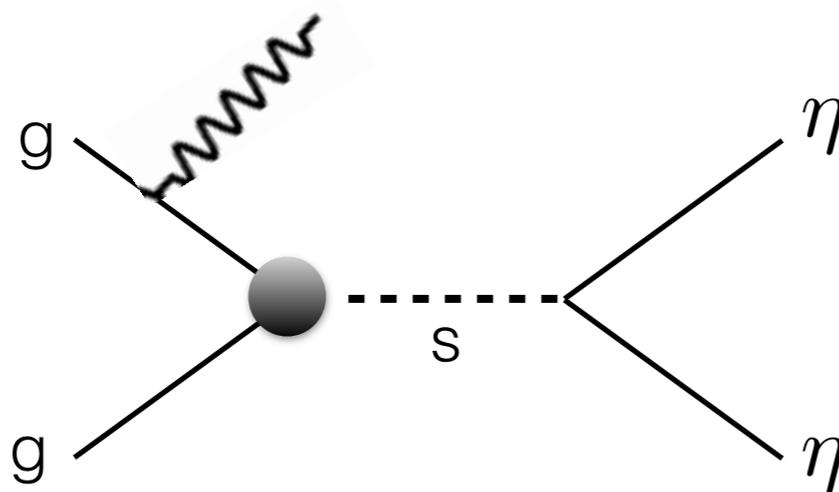
$$\hat{\sigma}(gg \rightarrow gh^* \rightarrow g\eta\eta) \propto \frac{\theta(p_h^2 - 4m_\eta^2)}{(p_h^2 - m_h^2)^2 + \Gamma_h^2 m_h^2} \left(\frac{p_h^2}{f^2} - \lambda \right)^2 \sqrt{1 - \frac{4m_\eta^2}{p_h^2}}$$

- For the onshell regime the momentum dependence vanishes
- Off-shell Higgs regime, leads to a very small cross section < 1 fb for momentum dependent and < 0.5 fb for momentum independent couplings
- Good measurements of Higgs production cross sections limit ggh couplings, decreasing the total cross section for monojet production

- Z_2 odd real singlet scalar dark matter particle couplings to the Standard Model with Z_2 even scalar singlet

$$\mathcal{L}_{\eta,s} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \partial_\mu \eta \partial^\mu \eta - \frac{1}{2} m_\eta^2 \eta \eta + \frac{1}{2} \partial_\mu s \partial^\mu s - \frac{1}{2} m_s^2 s s$$

$$+ \frac{c_{s\eta} f}{2} s \eta \eta + \frac{c_{\partial s \eta}}{f} (\partial_\mu s) (\partial^\mu \eta) \eta + \frac{\alpha_s}{16\pi} \frac{c_{sg}}{f} s G_{\mu\nu}^a G^{a\mu\nu}$$

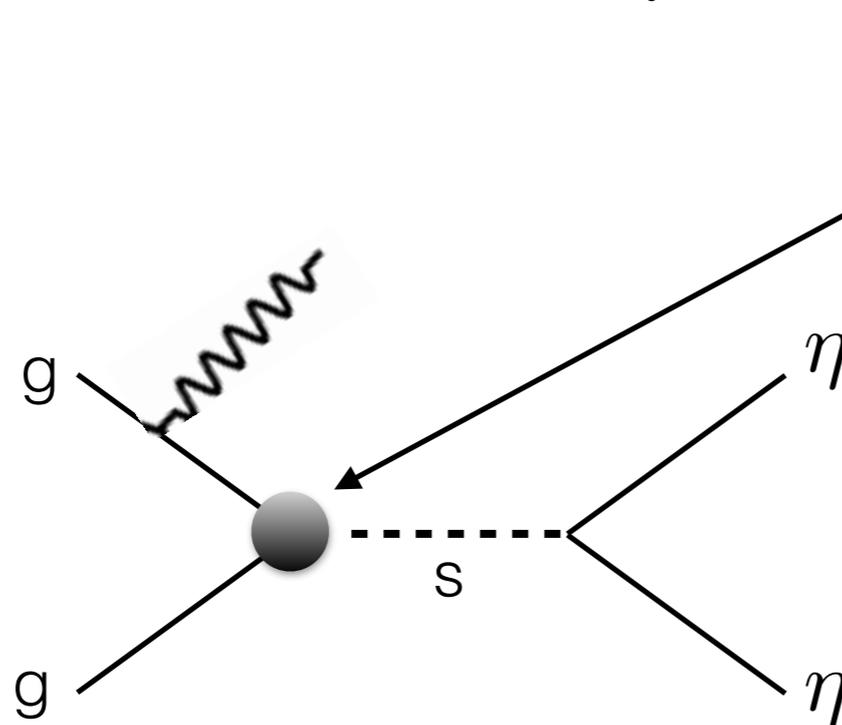


For consistent model constructions and detailed dark matter phenomenology see [arXiv:1501.05957](https://arxiv.org/abs/1501.05957)

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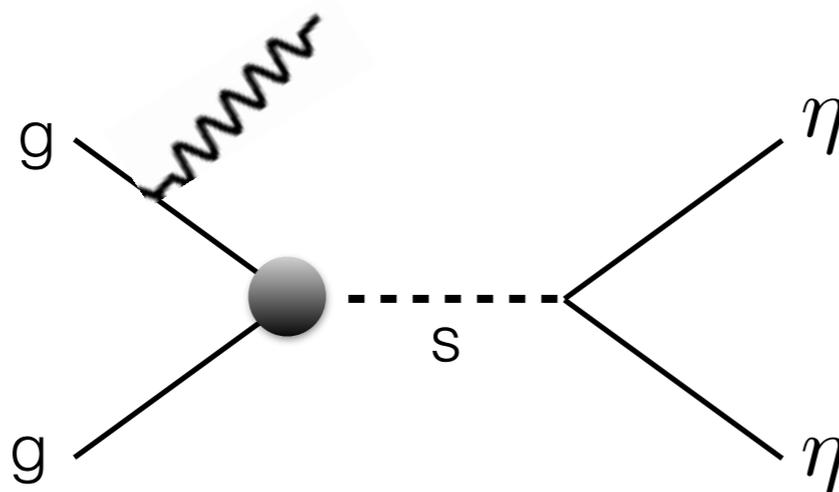


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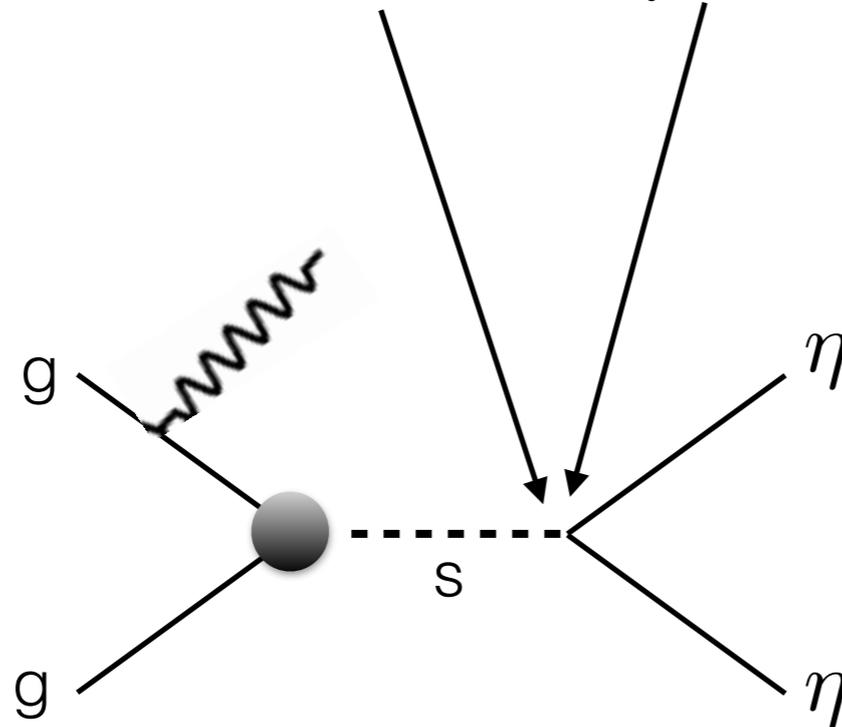


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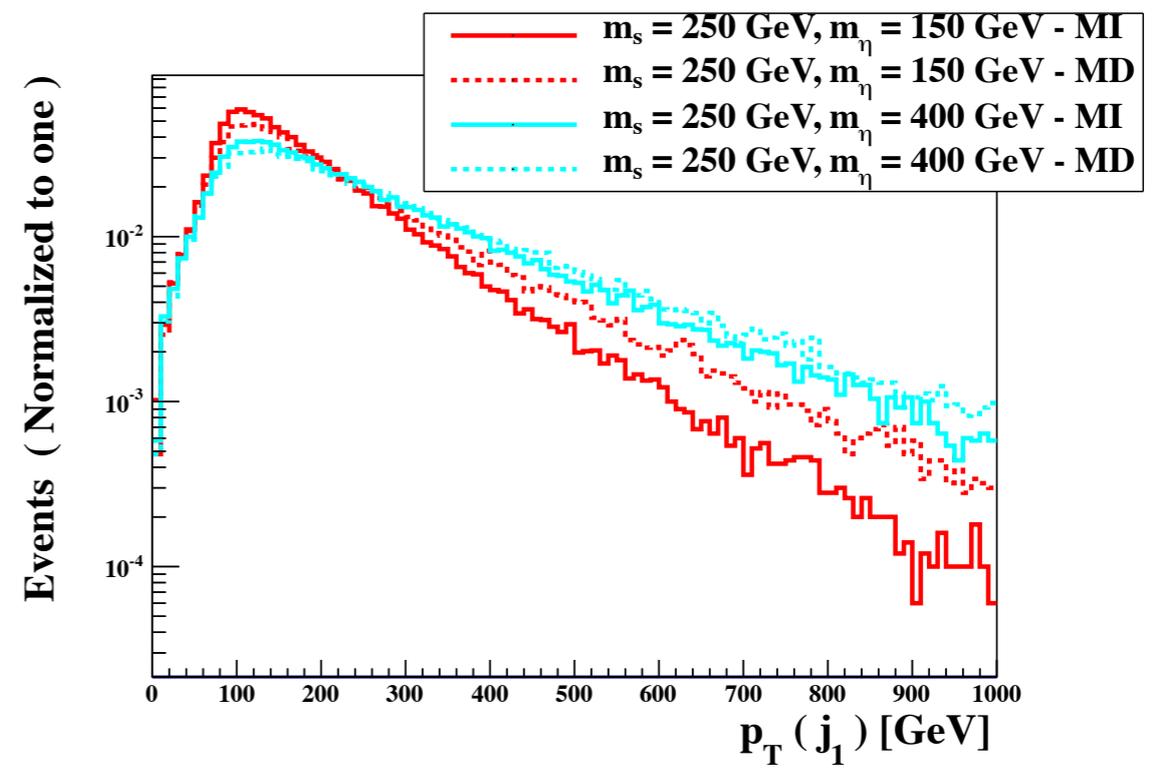
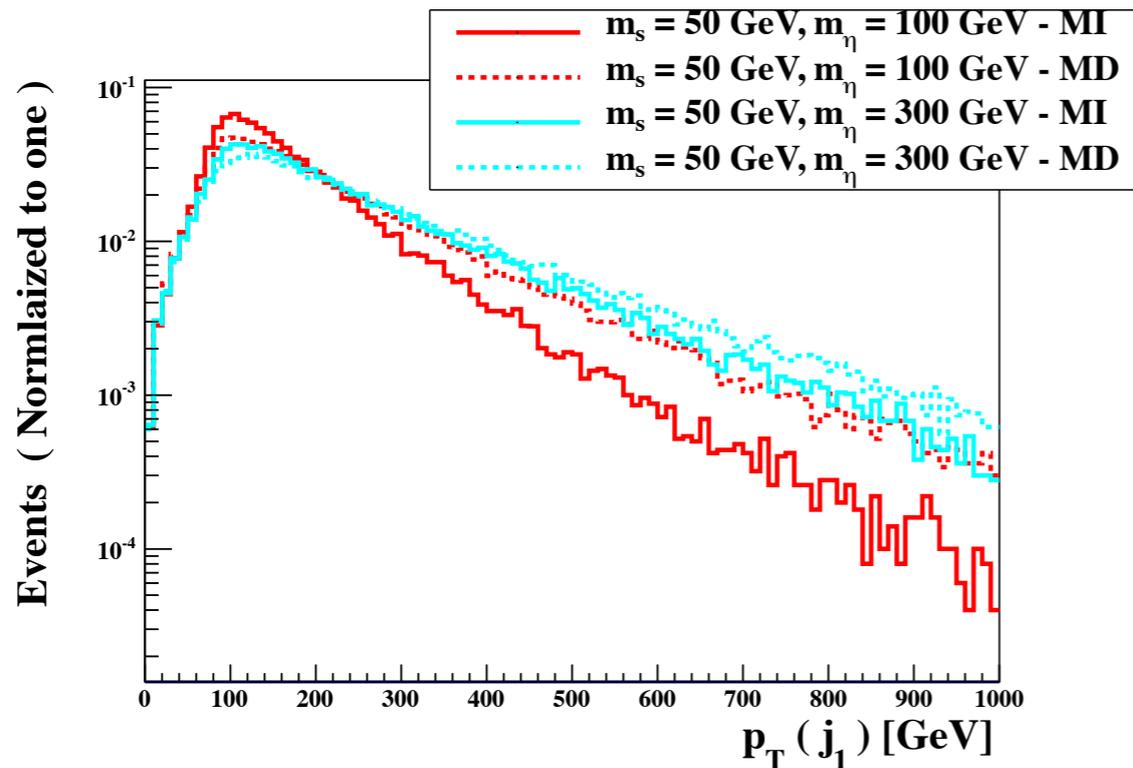
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$$c_{gs} = 100 \quad f = 1 \text{ TeV} \quad c_{\partial s\eta} = 2.5 \quad c_{s\eta} = 0.5$$

Production cross section of 2.9 pb after generator cut of jet $p_T > 80 \text{ GeV}$

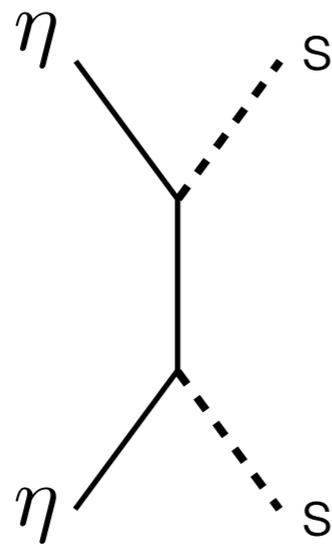
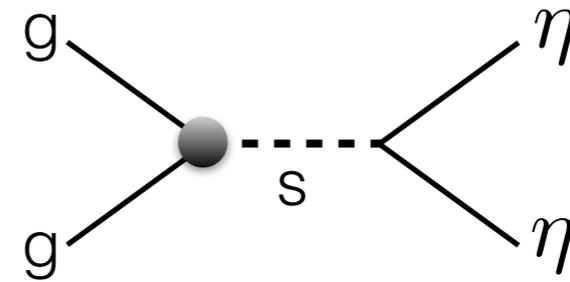
For $p_T > 300 \text{ GeV}$,
Luminosity 300 fb^{-1}

| #events MI | #events MD |
|------------|------------|
| 131300 | 196533 |

Momentum dependent
expected to yield 50%
better sensitivity

- Unlike LHC constraints, relic density depends on the propagator mass
- Two annihilation channels

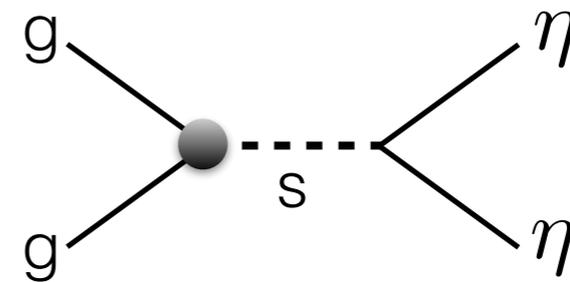
$$\langle \sigma v \rangle_{gg} \simeq \frac{\alpha_s^2 c_{sg}^2 (c_{s\eta} f^2 + 4c_{\partial s\eta} m_s^2)^2}{256\pi^3 f^4 (m_s^2 - 4m_\eta^2)^2}$$



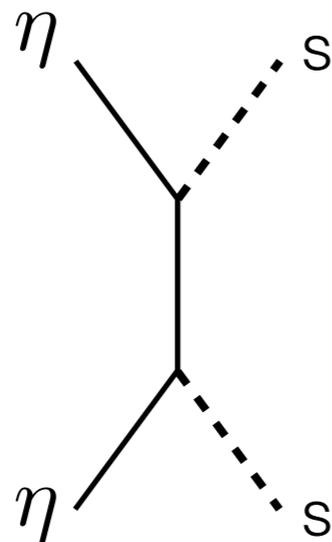
$$\langle \sigma v \rangle_{ss} \simeq \frac{\sqrt{1 - \frac{m_s^2}{m_\eta^2}} (c_{\partial s\eta} m_s^2 + c_{s\eta} f^2)^4}{16\pi f^4 m_\eta^2 (m_s^2 - 2m_\eta^2)^2}$$

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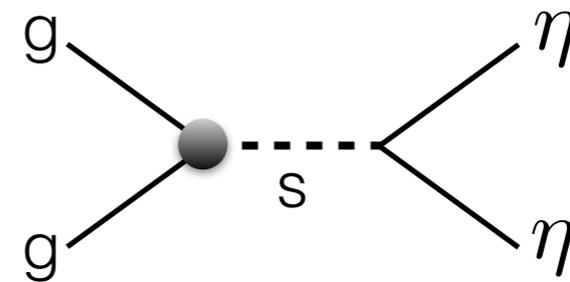
Mostly drives relic



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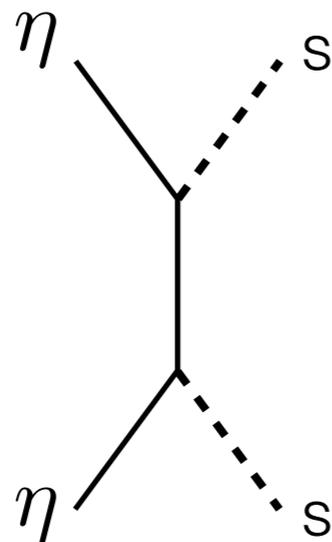
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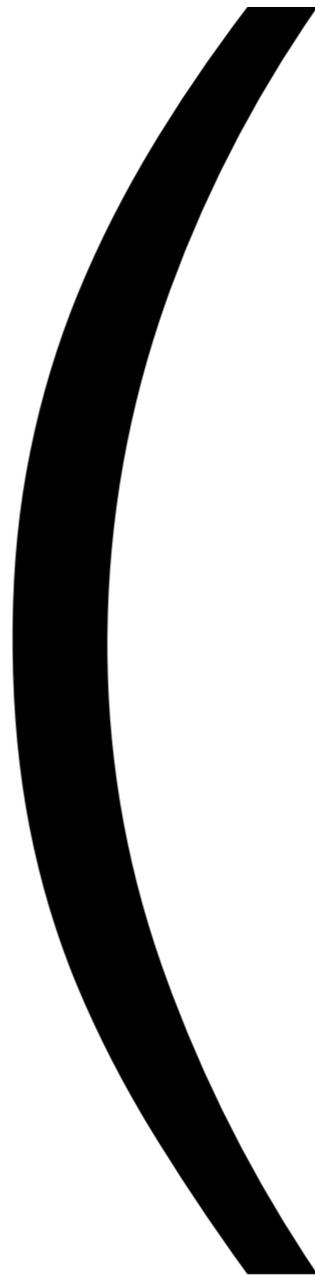


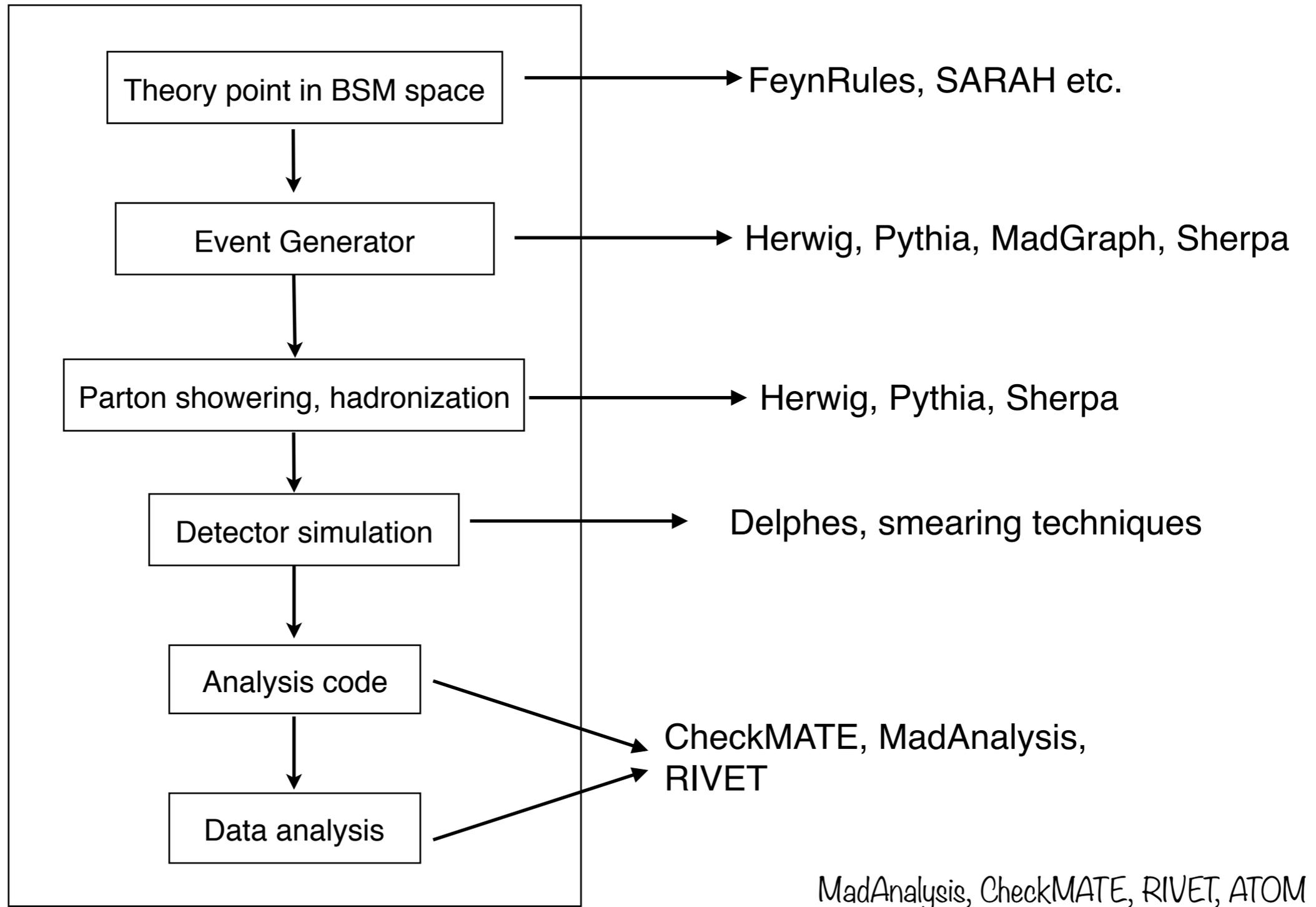
Mostly drives relic

Contributes up to 15%



$$\langle \sigma v \rangle_{ss} \simeq \frac{\sqrt{1 - \frac{m_s^2}{m_\eta^2}} (c_{\partial s\eta} m_s^2 + c_{s\eta} f^2)^4}{16\pi f^4 m_\eta^2 (m_s^2 - 2m_\eta^2)^2}$$





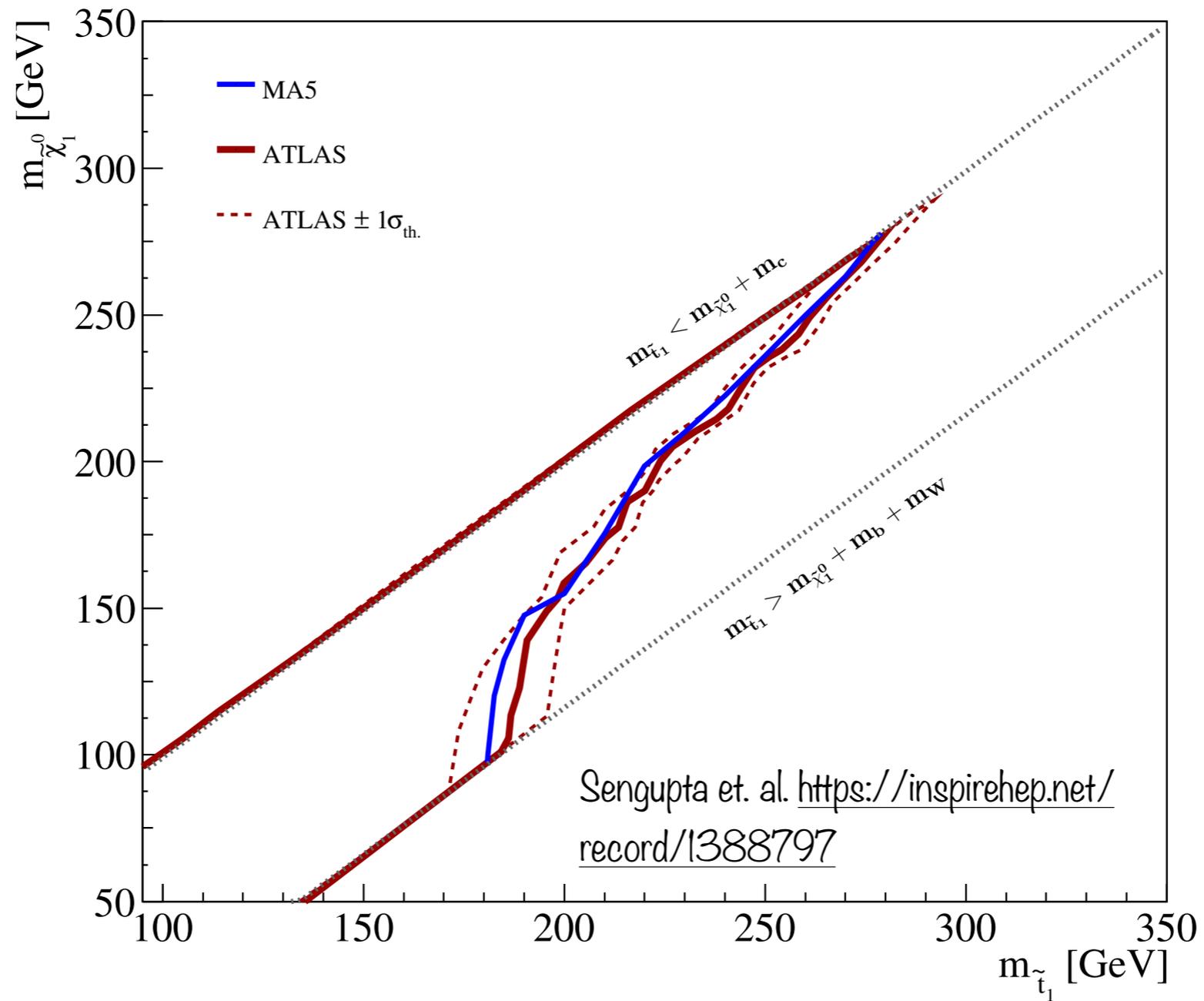
- Public framework for analysing Monte-Carlo events
- Has different levels of sophistication — partonic, hadronic, detector reconstructed
- Input formats: StdHEP, HepMC, LHE, LHCO, Delphes ROOT files
- Normal mode: Initiative commends typed in python interface
- Expert mode: C++/ROOT programmes

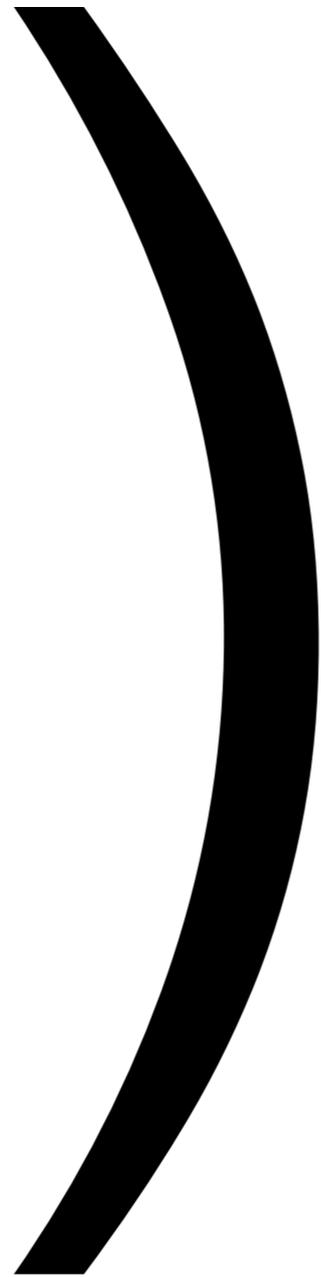
<http://madanalysis.irmp.ucl.ac.be/>,

Conte et al Eur. Phys. J. C74 (2014), no. 10 3103 ,

Dumont et al. Eur. Phys. J. C75 (2015), no. 2 56

| cut | $\tilde{t} \rightarrow c\tilde{\chi}_1^0$ (200/125) cutflow | | | |
|----------------------------------------------------|-------------------------------------------------------------|-----------------|------------------------|-------------------------------|
| | # events (scaled to σ and \mathcal{L}) | relative change | # events (official) | relative change (official) |
| Initial number of events | 376047.3 | 376047.3 | | |
| $E_T^{\text{miss}} > 80$ GeV Filter | 192812.8 | -48.7% | 181902.0 | 181902.0 |
| $E_T^{\text{miss}} > 100$ GeV | 136257.1 | -29.3% | 97217.0 | -46.6% |
| Trigger, Event cleaning... | - | - | 82131.0 | |
| Lepton veto | 134894.2 | -1.0% | 81855.0 | -15.8% |
| $N_{\text{jets}} \leq 3$ | 101653.7 | -24.6% | 59315.0 | -27.5% |
| $\Delta\phi(E_T^{\text{miss}}, \text{jets}) > 0.4$ | 95568.8 | -2.1% | 54295.0 | -8.5% |
| Leading jet $p_T > 150$ GeV | 17282.8 | -81.9% | 14220.0 | -73.8% |
| $E_T^{\text{miss}} > 150$ GeV | 10987.8 | -36.4% | 9468.0 | -33.4% |
| M1 Signal Region | | | | |
| Leading jet $p_T > 280$ GeV | 2031.2 | -81.5% | 1627.0 | -82.8% |
| $E_T^{\text{miss}} > 220$ GeV | 1517.6 | -25.3% | 1276.0 | -21.6% |
| M2 Signal Region | | | | |
| Leading jet $p_T > 340$ GeV | 858.0 | -92.2% | 721.0 | -92.4% |
| $E_T^{\text{miss}} > 340$ GeV | 344.4 | -59.9% | 282.0 | -60.9% |
| M3 Signal Region | | | | |
| Leading jet $p_T > 450$ GeV | 204.3 | -98.1% | 169.0 | -98.2% |
| $E_T^{\text{miss}} > 450$ GeV | 61.3 | -70.0% | 64.0 | -62.1% |



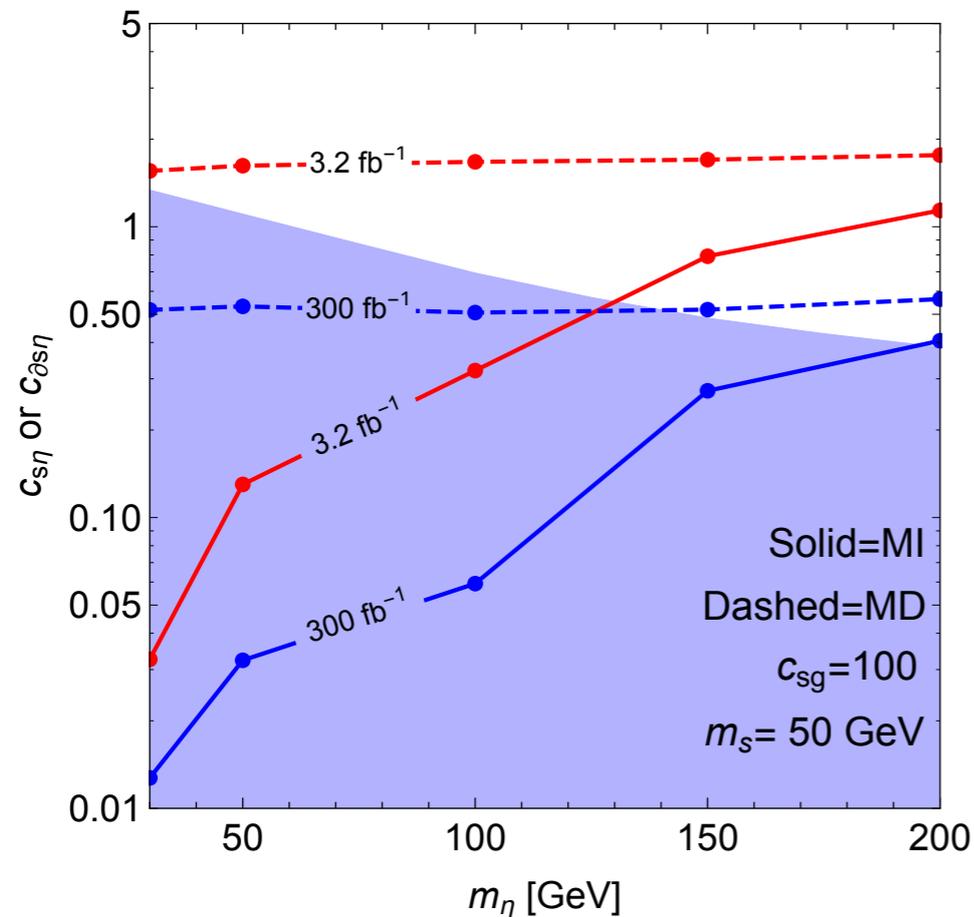


ATLAS monojet analysis at 13 TeV with 3.2 fb⁻¹ data (arXiv:1604.07773)

Reimplemented using MadAnalysis 5 by D. Sengupta

Inspire id: 10.7484/

INSPIREHEP.DATA.GTH3.RN26



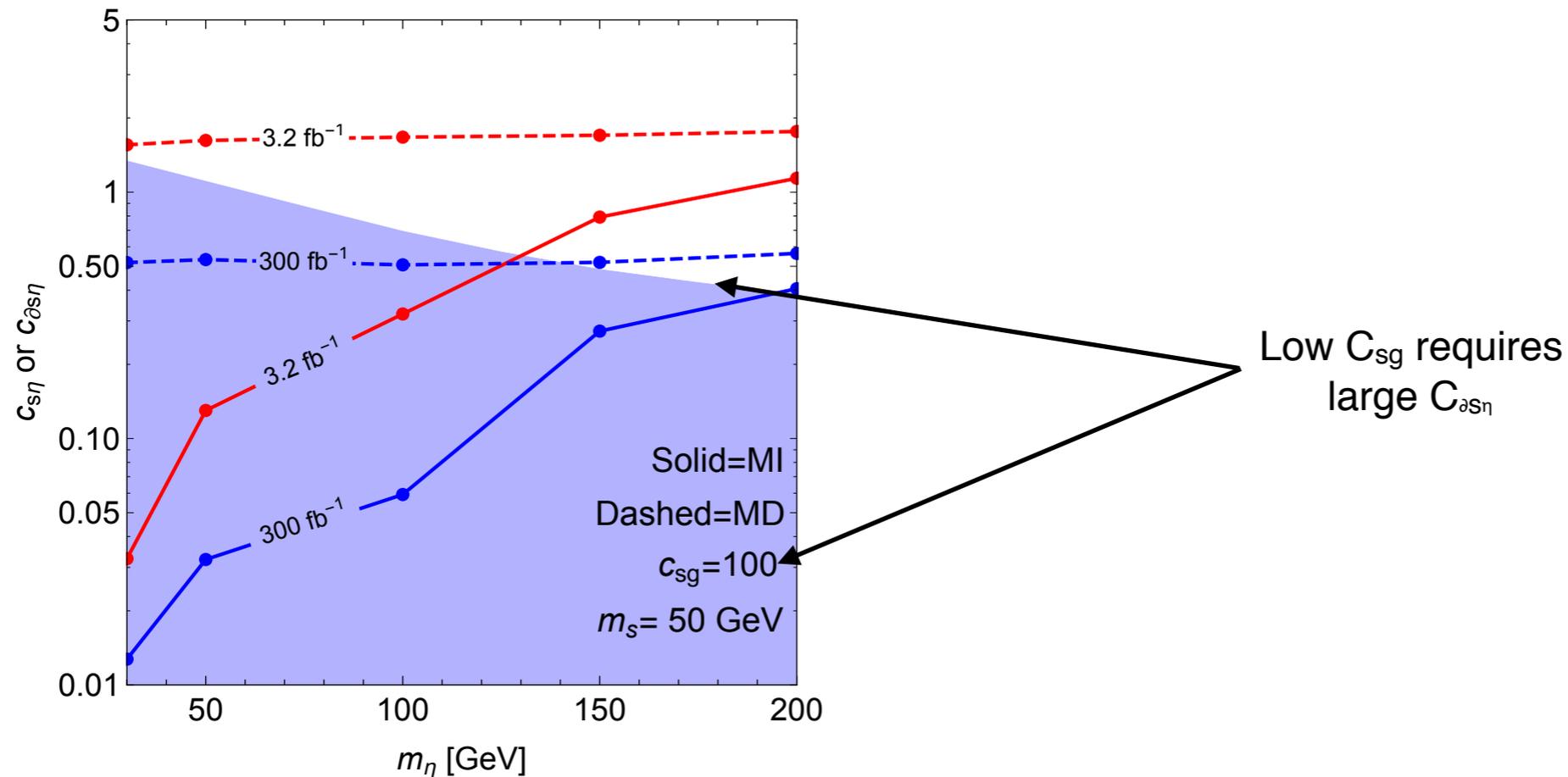
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- For light dark matter, we have better prospects at high luminosity LHC

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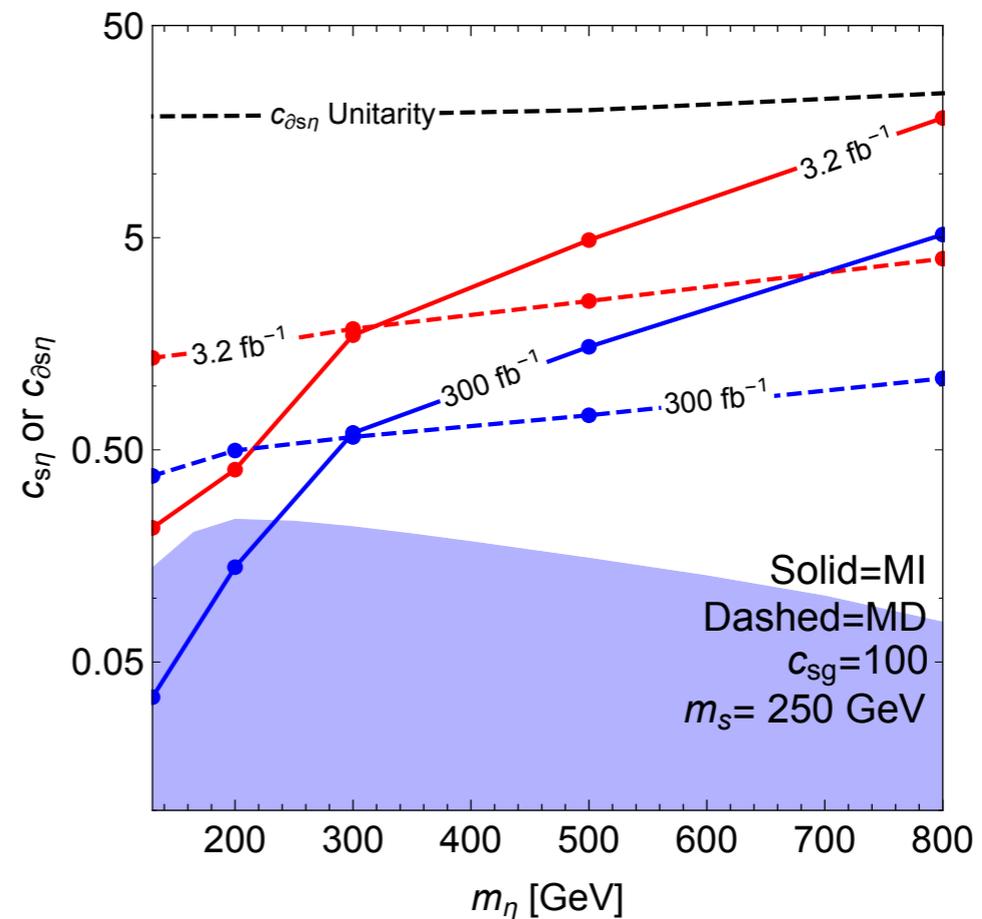
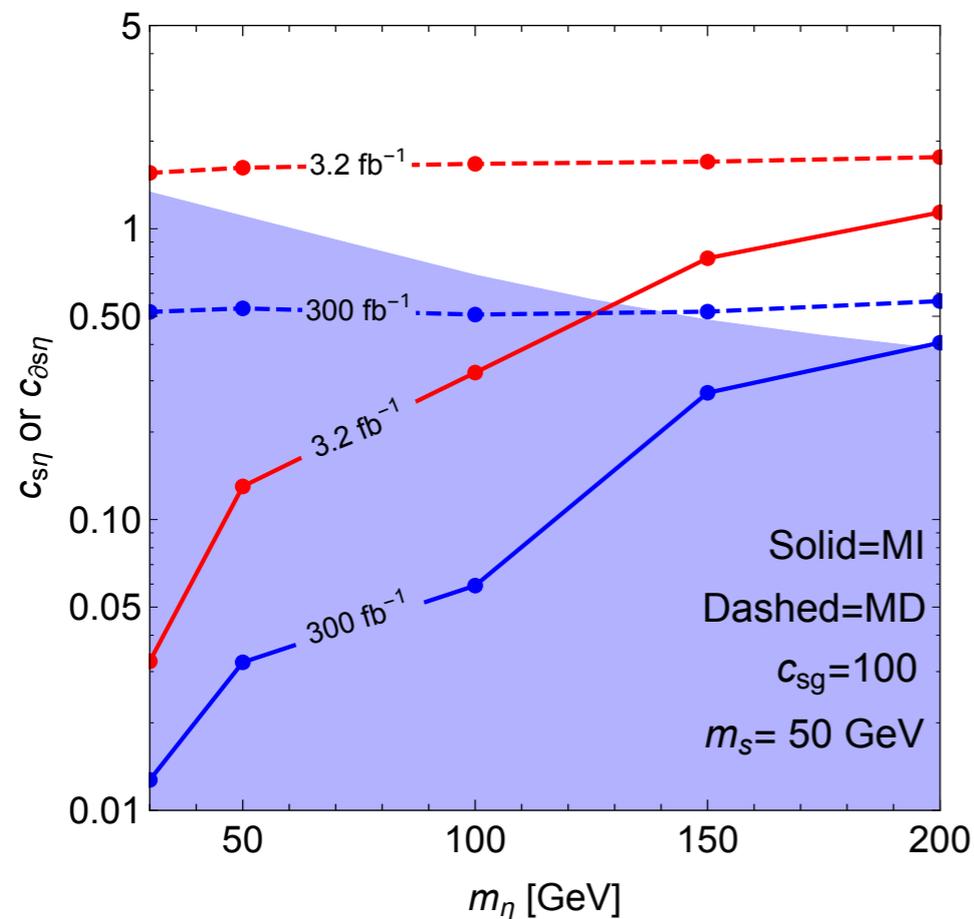
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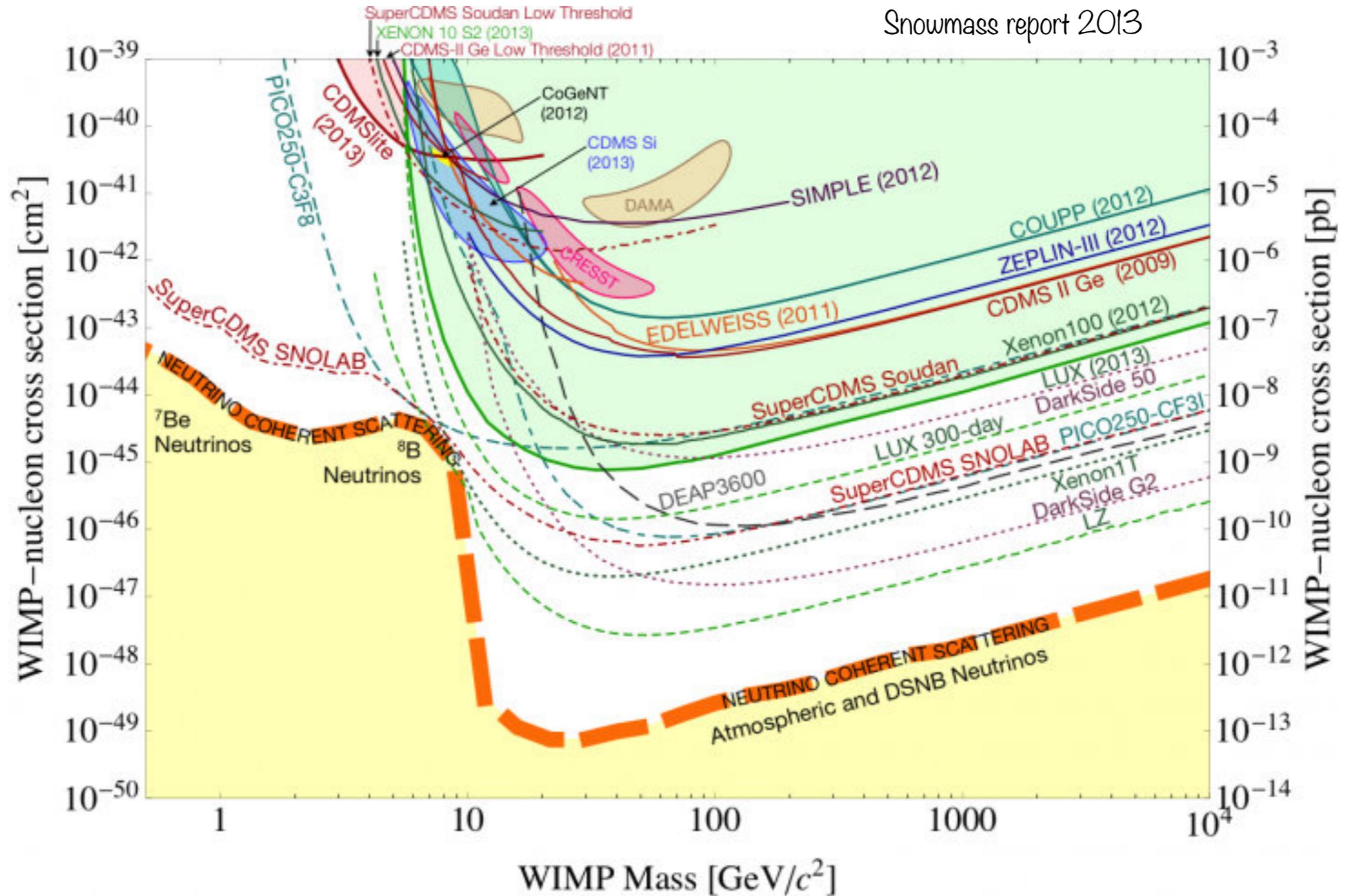
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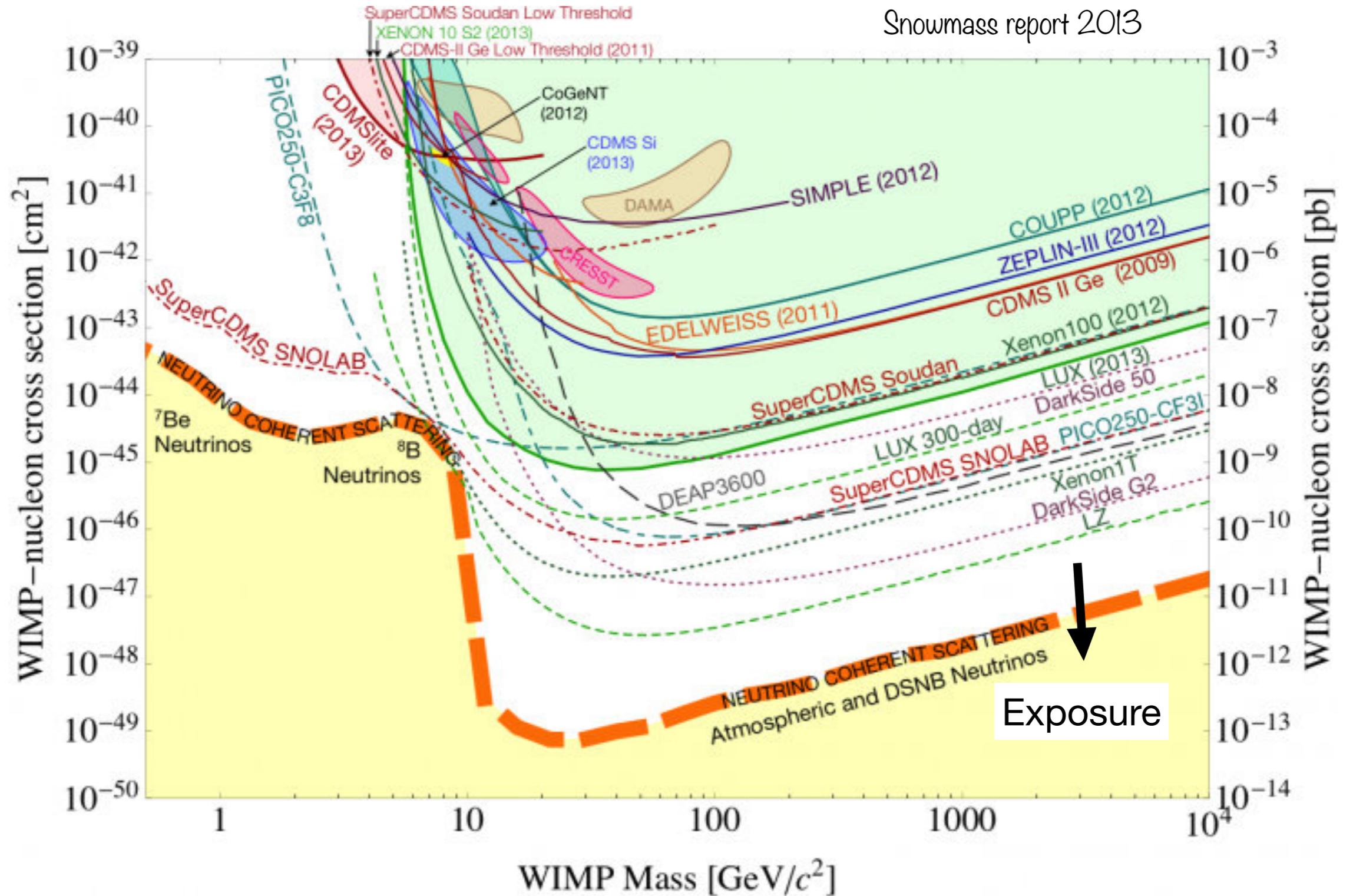


- Current mono jet searches do not probe dark matter relic density
- For light dark matter, we have better prospects at high luminosity LHC
- For heavier dark matter, it is still difficult to probe relic density

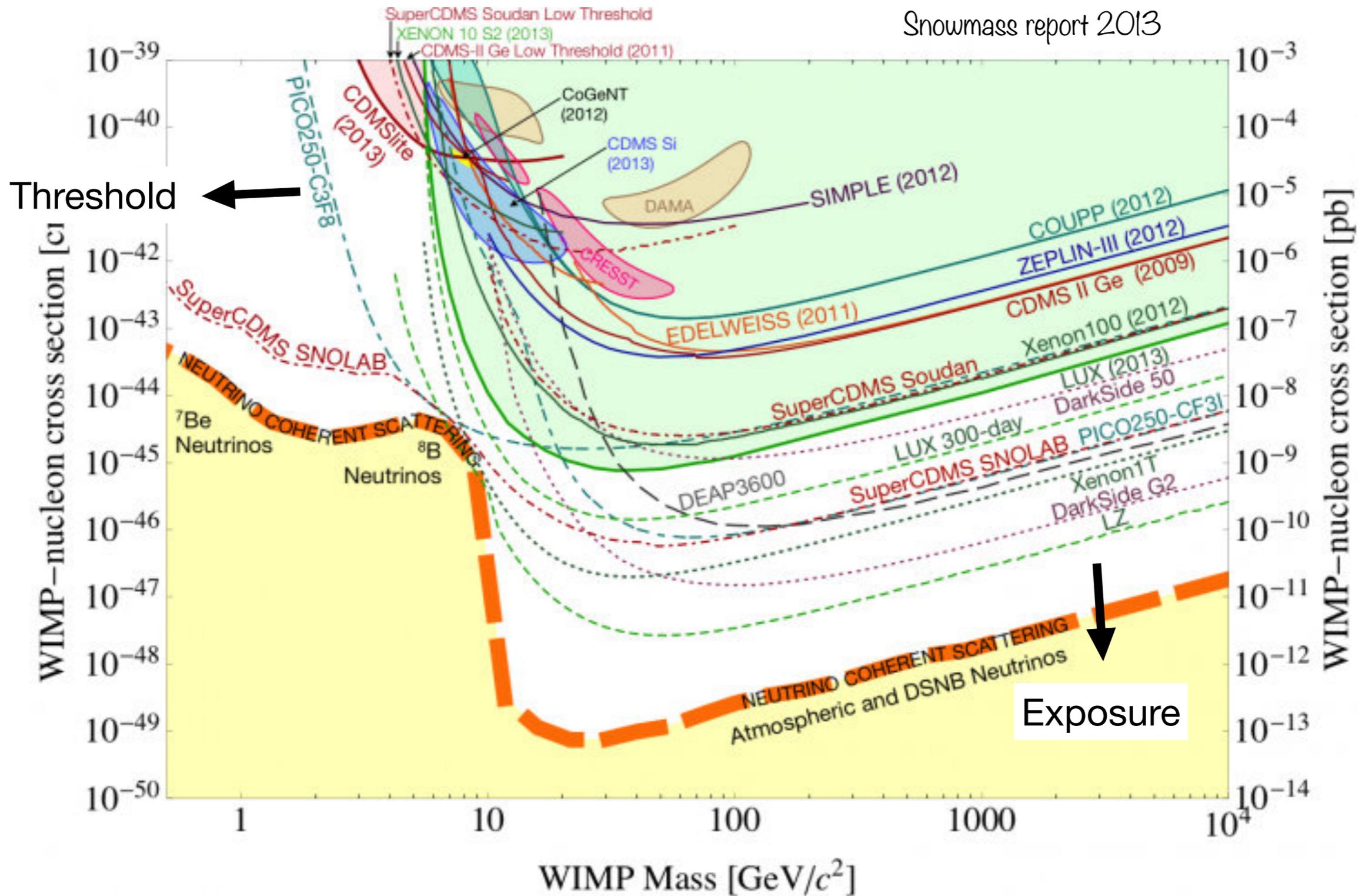
Potential of future searches

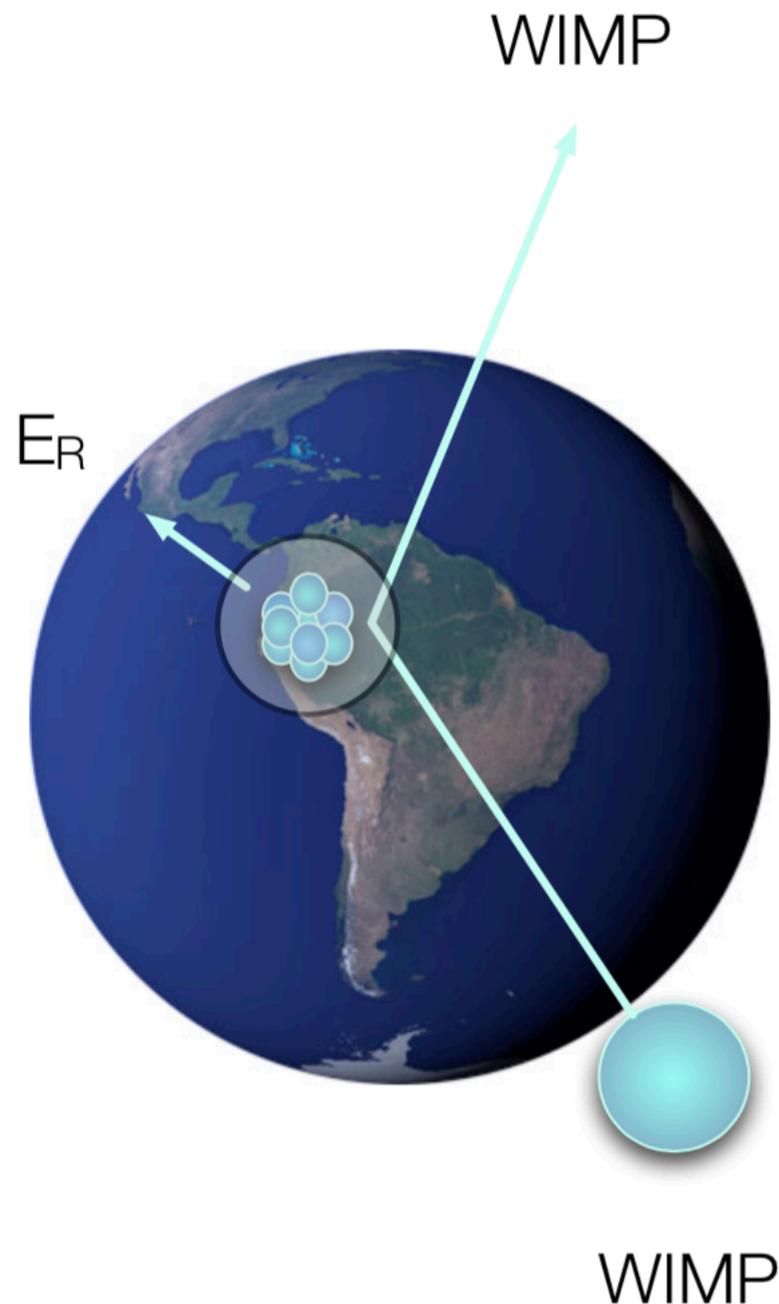
Snowmass report 2013





Snowmass report 2013



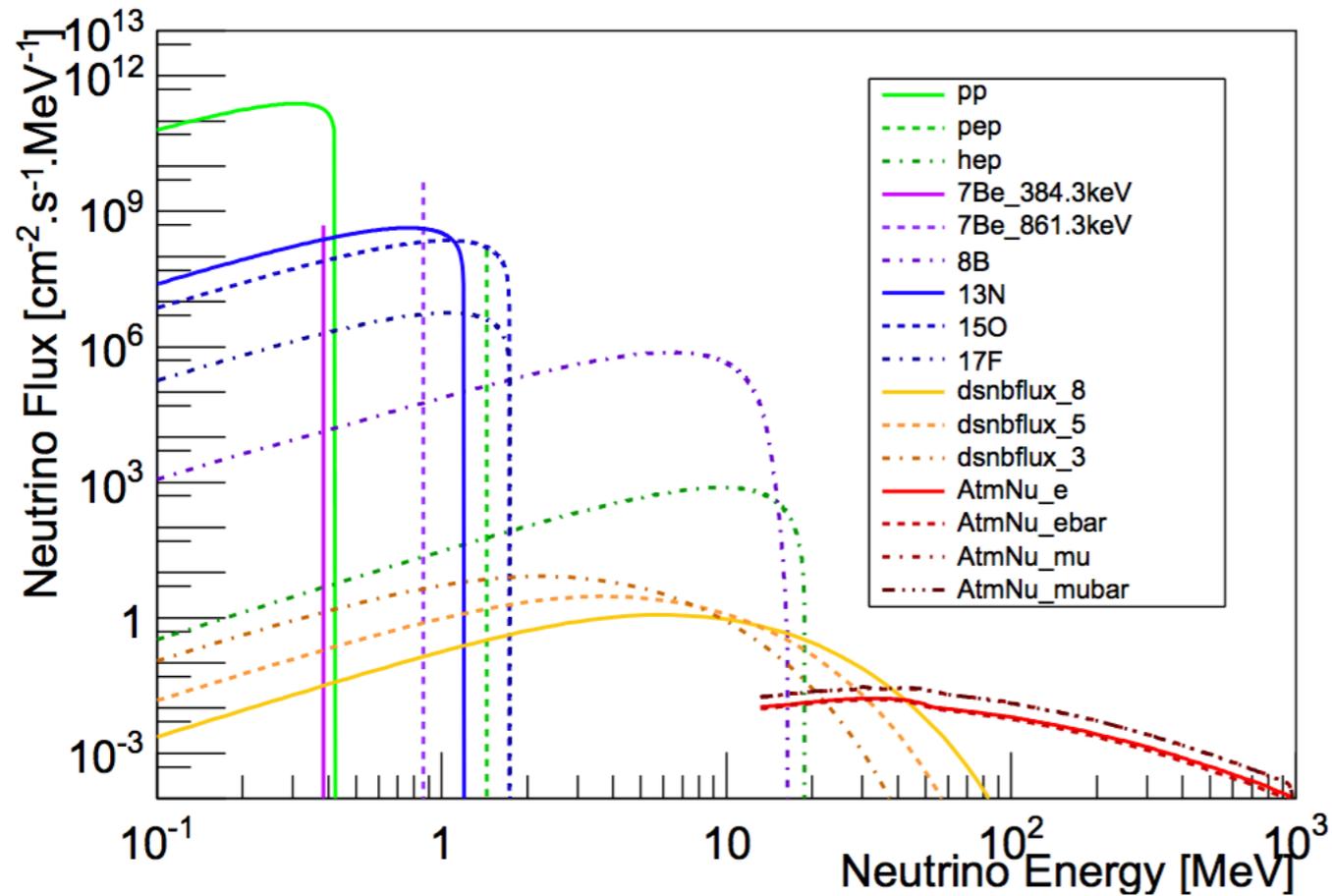


- Elastic collision between WIMPs and target nuclei

$$E_R = \frac{|\vec{q}|^2}{2m_N} = \frac{\mu^2 v^2}{m_N} (1 - \cos \theta)$$

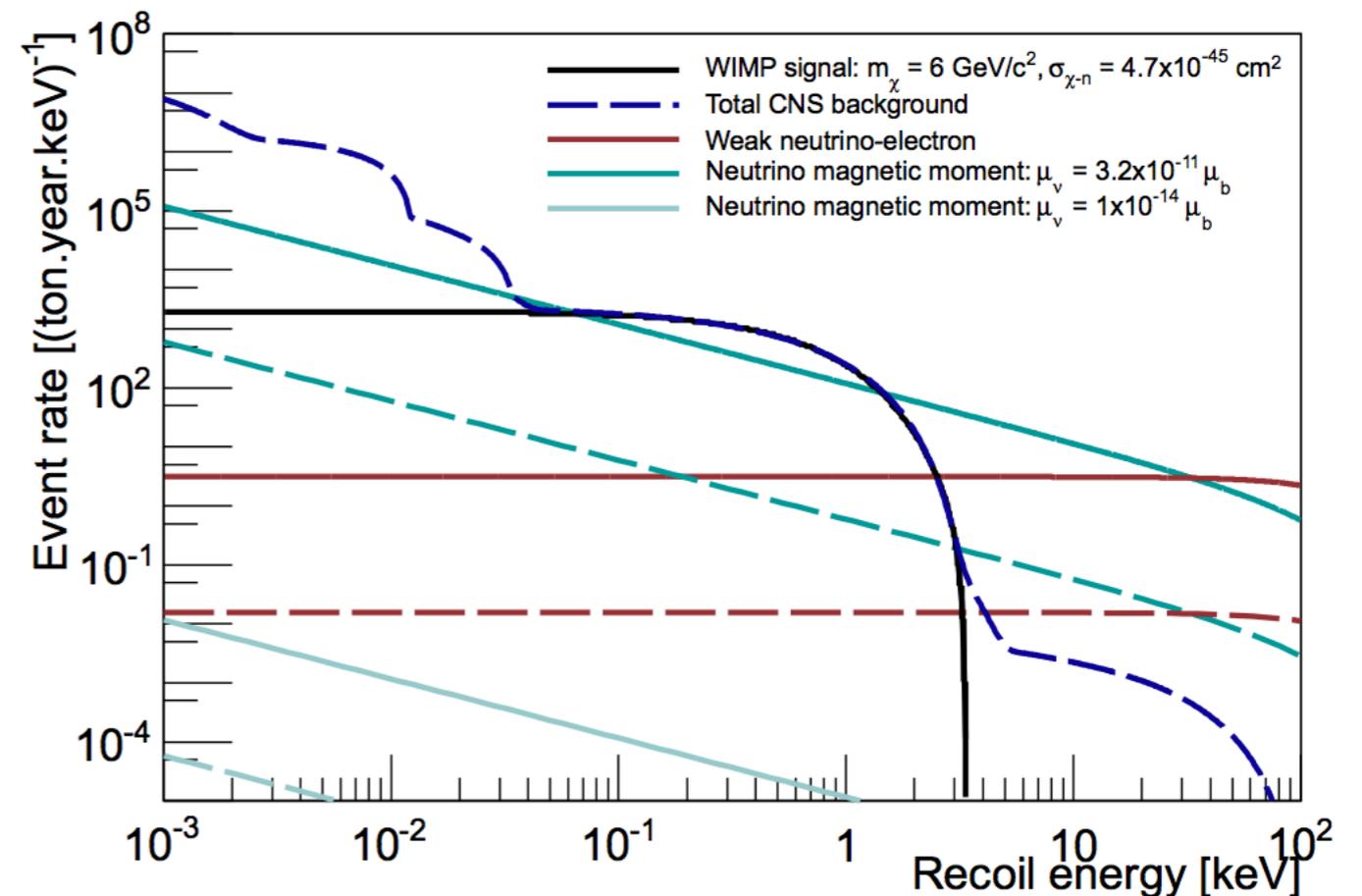
- Momentum transfer: q
- Reduced mass of nucleus: μ
- Mean WIMP velocity relative to target: v
- Scattering angle in center of mass system: θ
- WIMP recoils can be mimicked by neutrino recoils

- Neutrino fluxes are large, thankfully their cross sections are small
- Recoil energies peak at low threshold, more problem for light dark matter

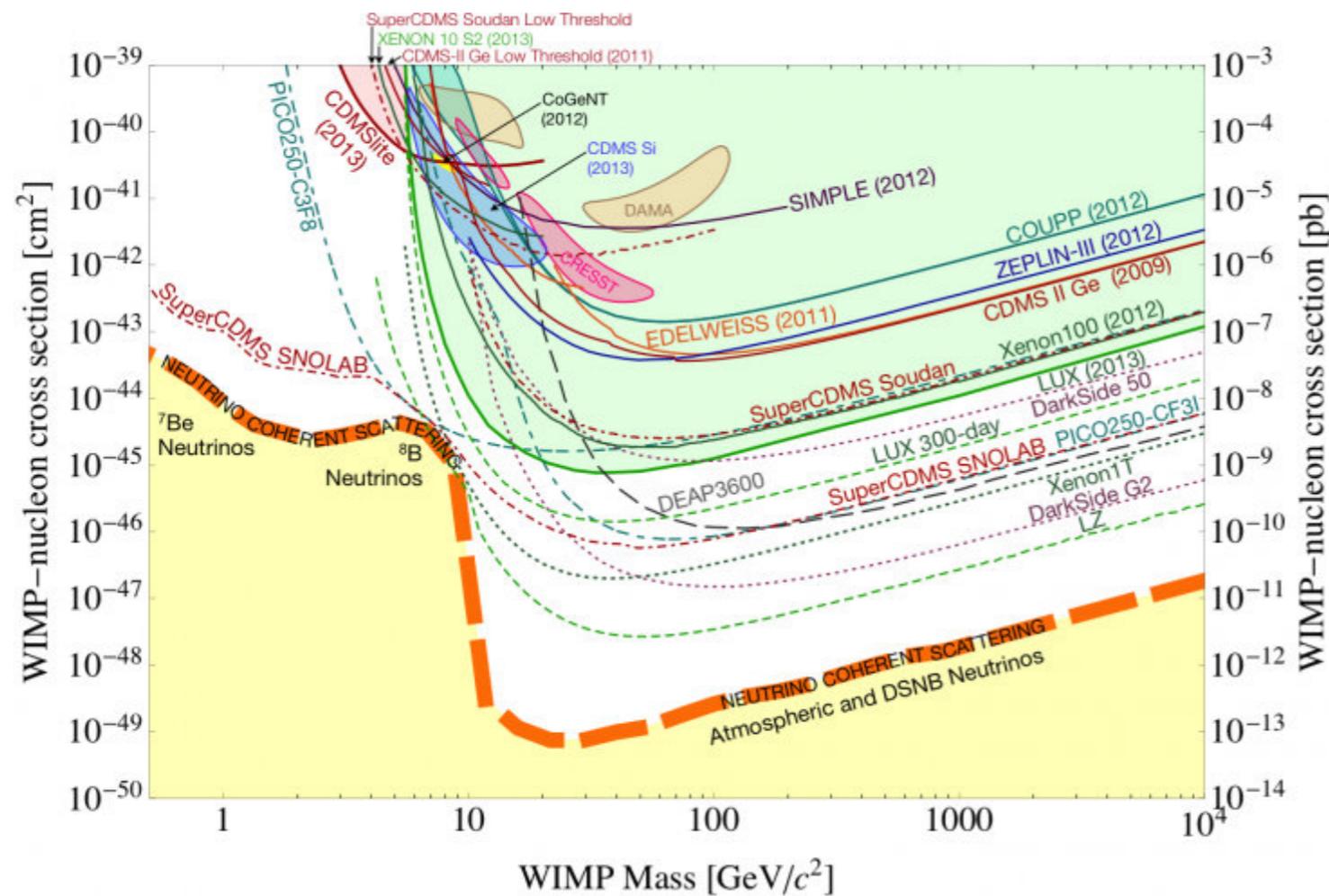


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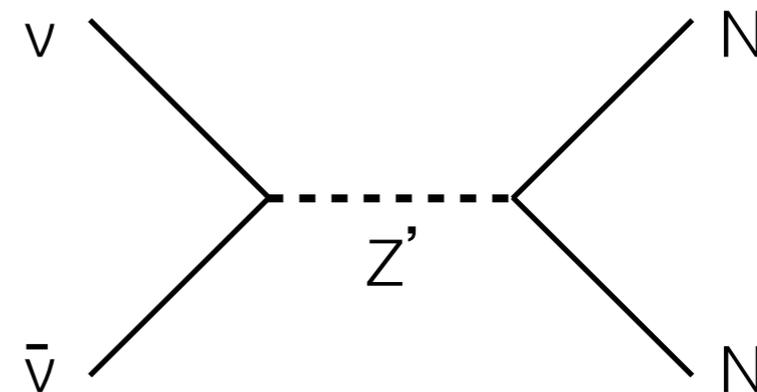
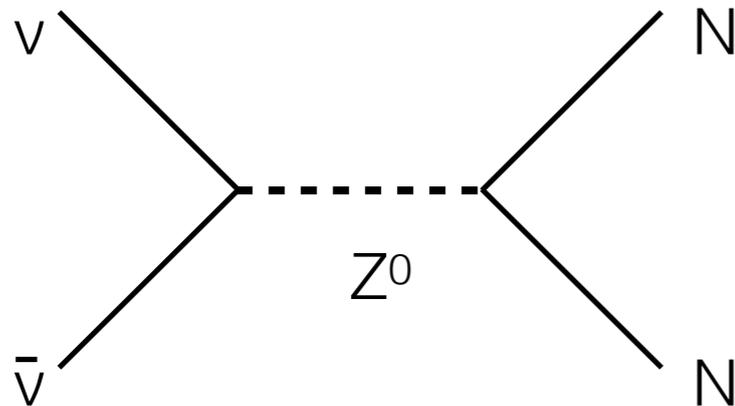


- Neutrino fluxes are large, thankfully their cross sections are small
- Recoil energies peak at low threshold, more problem for light dark matter



Kulkarni et al. JHEP 1704 (2017) 073

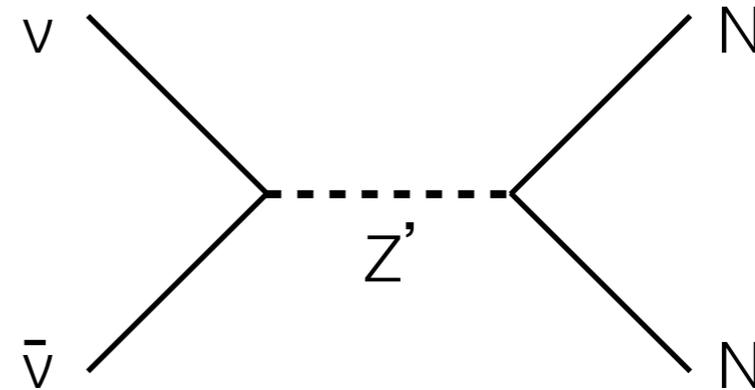
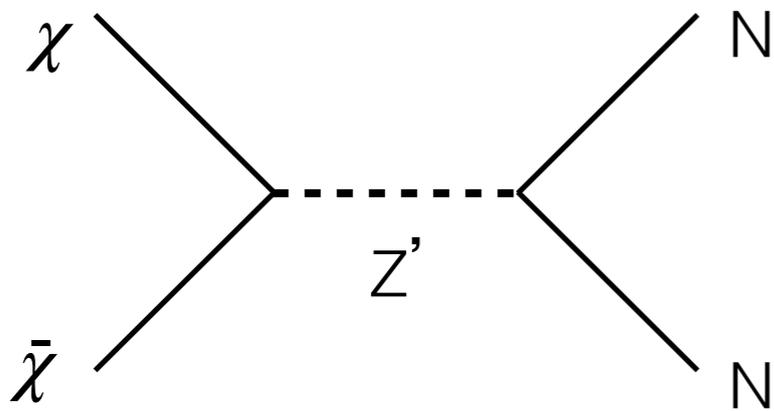
- The **coherent neutrino scattering** at the direct detection is a coherent sum of the SM and new physics scattering diagrams



$$\left. \frac{d\sigma^\nu}{dE_R} \right|_V = \mathcal{G}_V \left. \frac{d\sigma^\nu}{dE_R} \right|_{SM}, \quad \mathcal{G}_V = 1 + \left(\frac{Q_V}{Q_V^{SM}} \right)^2 \frac{4((g_V^\nu)^2)}{G_F^2 (q^2 - m_V^2)^2} - \frac{Q_V}{Q_V^{SM}} \frac{2\sqrt{2}(g_V^\nu)}{G_F (q^2 - m_V^2)}$$

- Notice the possibility of destructive interference

- The **total signal** is a sum of DM scattering and neutrino scattering rates



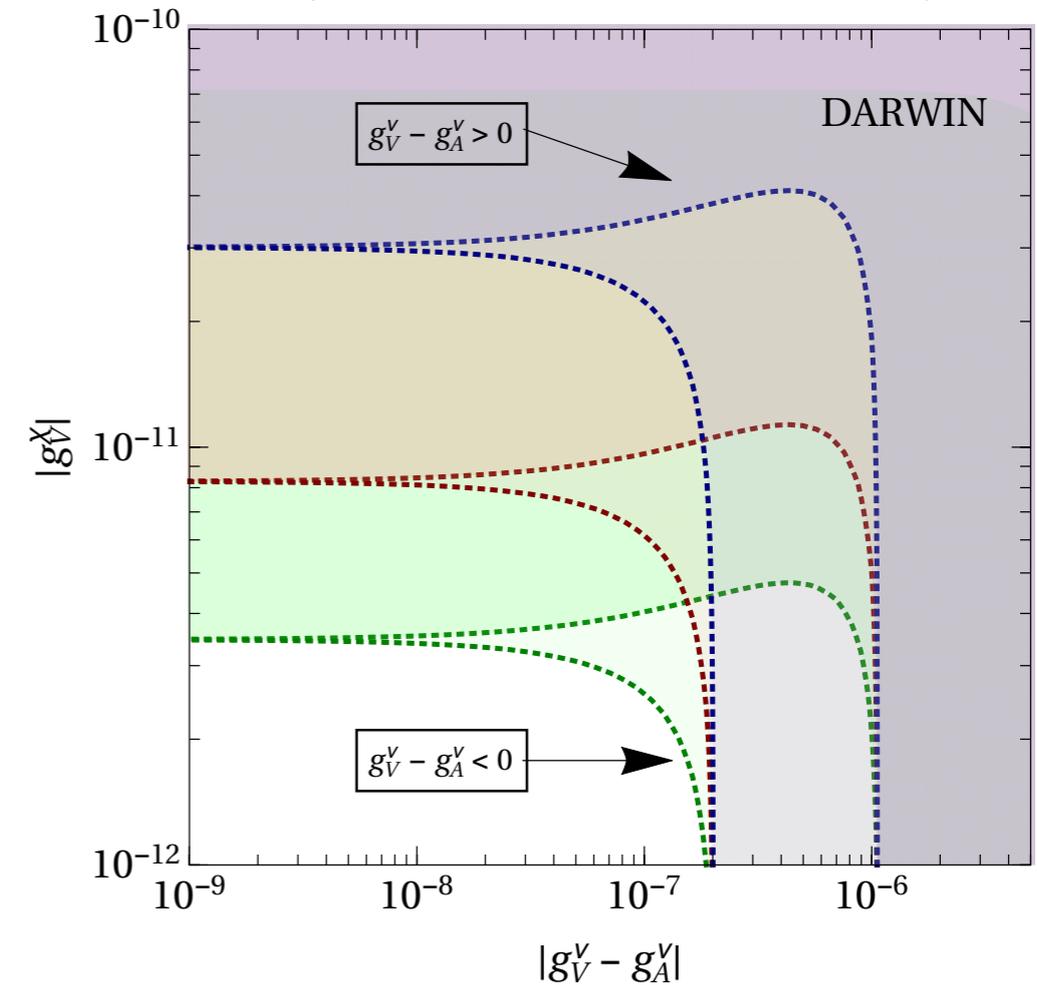
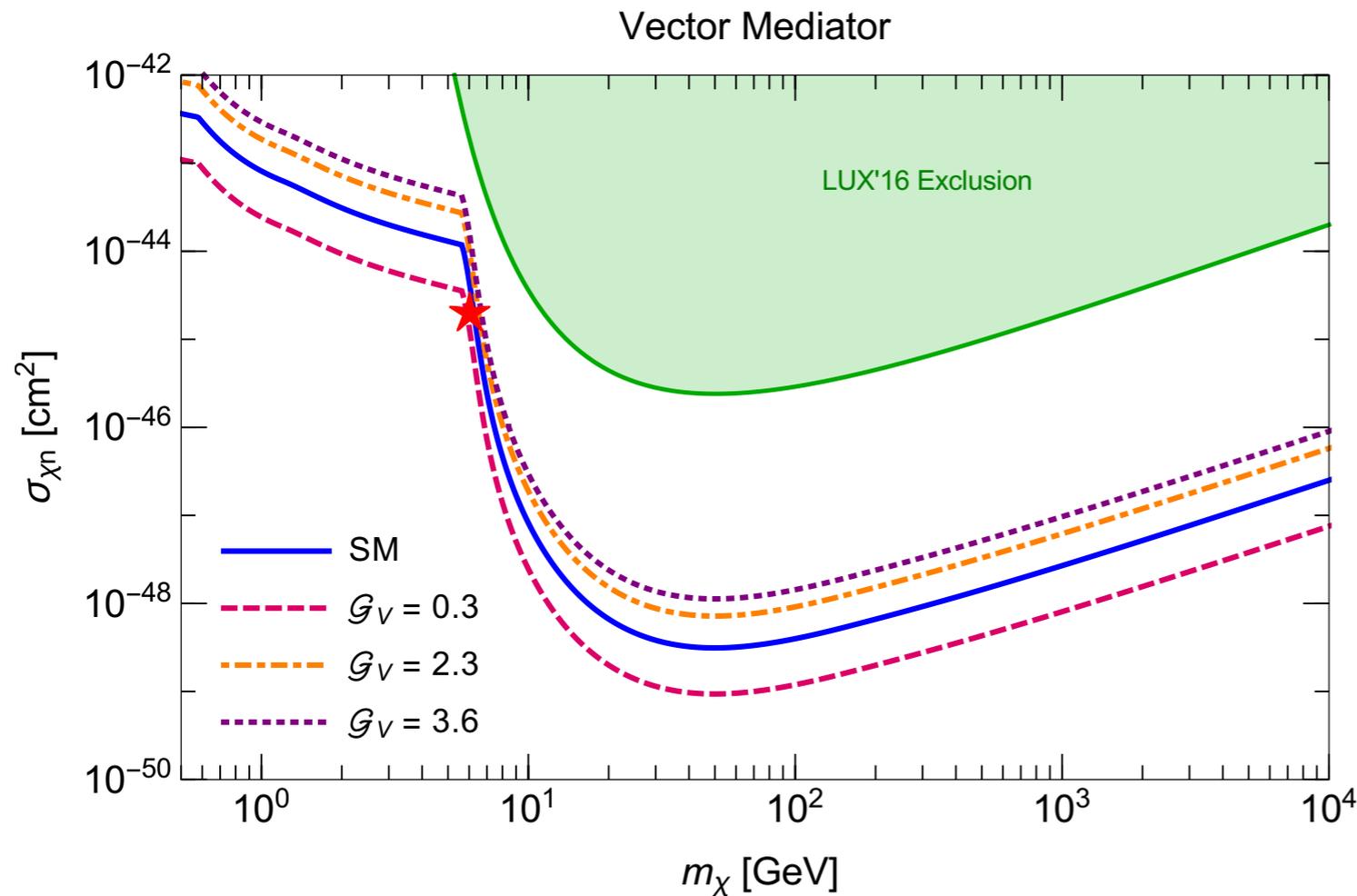
$$\left. \frac{dR}{dE_R} \right|_{\chi} = \mathcal{N} \frac{\rho_0}{m_N m_{\chi}} \int_{v_{\min}} v f(v) \frac{d\sigma_{SI}^{\chi}}{dE_R} d^3v$$

$$\left. \frac{d\sigma^{\nu}}{dE_R} \right|_V = \mathcal{G}_V \left. \frac{d\sigma^{\nu}}{dE_R} \right|_{SM}$$

- Notice the possibility of destructive interference

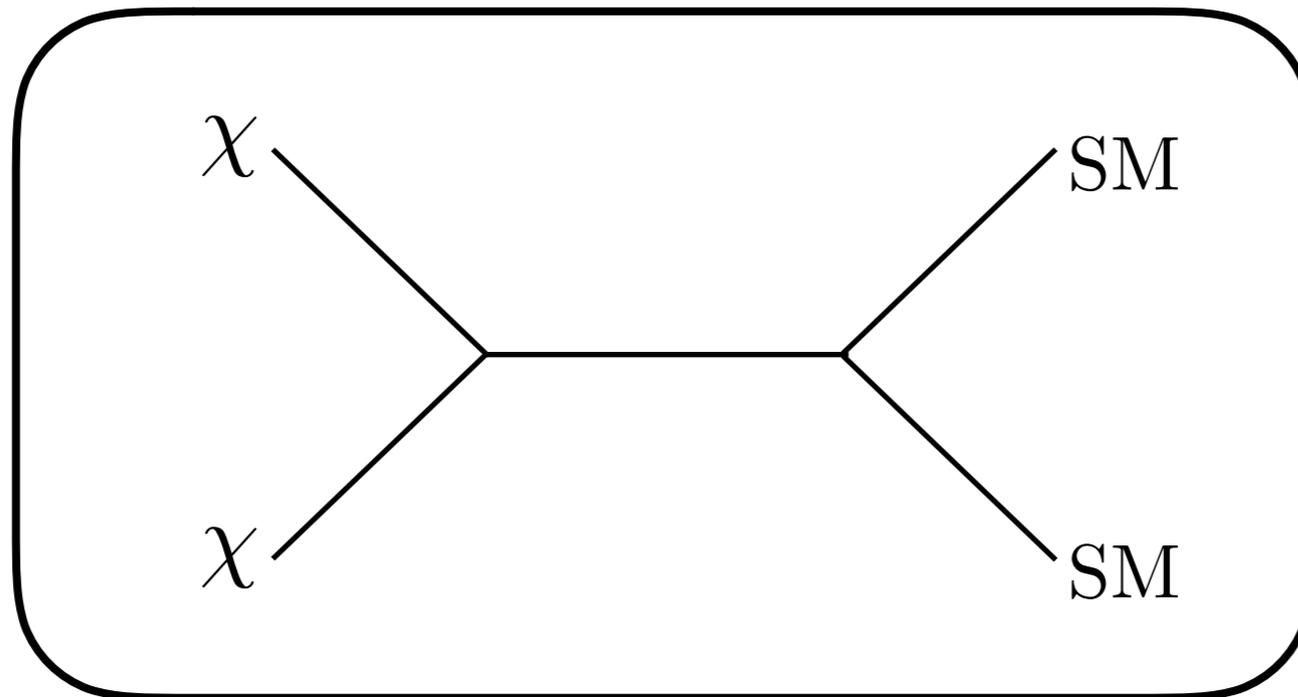
See also: Boehm et al. arXiv:1809.06385

$\Lambda_V^{-2} = \sqrt{4\pi} \text{ GeV}^{-2}$, Future Sensitivity



- Exotic neutrino interaction can lead to **measurable effects** at the direct detection experiments
- Next generation direct detection experiments can put **constraints on combined DM - SM and neutrino SM interactions**

- Previous analysis very much **valid in effective theory limit**, no longer the case if DM - SM interactions are mediated by light mediators



Kulkarni et. al. JCAP 1711 (2017) no.11, 016

- Dark matter event rate at direct detection experiment for **heavy mediators**

$$\frac{dR_T}{dE_R} = \frac{\rho_0}{m_{\text{DM}}} \eta(v_{\min}(E_R)) \frac{g^2 F_T^2(E_R)}{2\pi m_{\text{med}}^4}$$

- Dark matter event rate at direct detection experiment for **light mediators**

$$\frac{dR_T}{dE_R} = \frac{\rho_0 \xi_T}{2\pi m_{\text{DM}}} \frac{g^2 F_T^2(E_R)}{(2 m_T E_R + m_{\text{med}}^2)^2} \eta(v_{\min}(E_R))$$

- Shape of differential event rate changes as soon as mediator mass is comparable to momentum transfer
- This sensitivity might be greatly altered by experimental and astrophysical uncertainties e.g. background fluctuations and DM velocity distributions

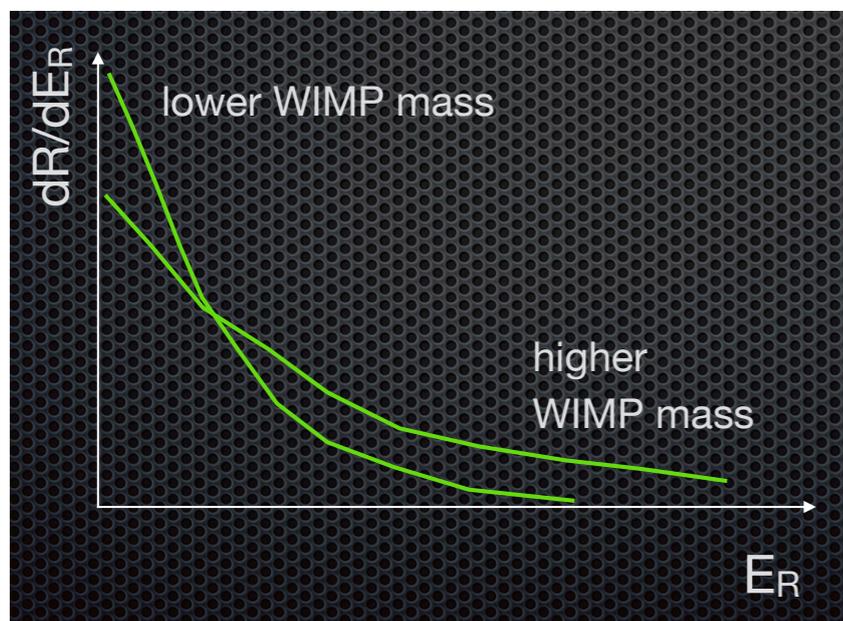
- Sharply falling recoil spectrum: need of very **low threshold**

See An et al. arxiv: 1412.8378 (PLB)

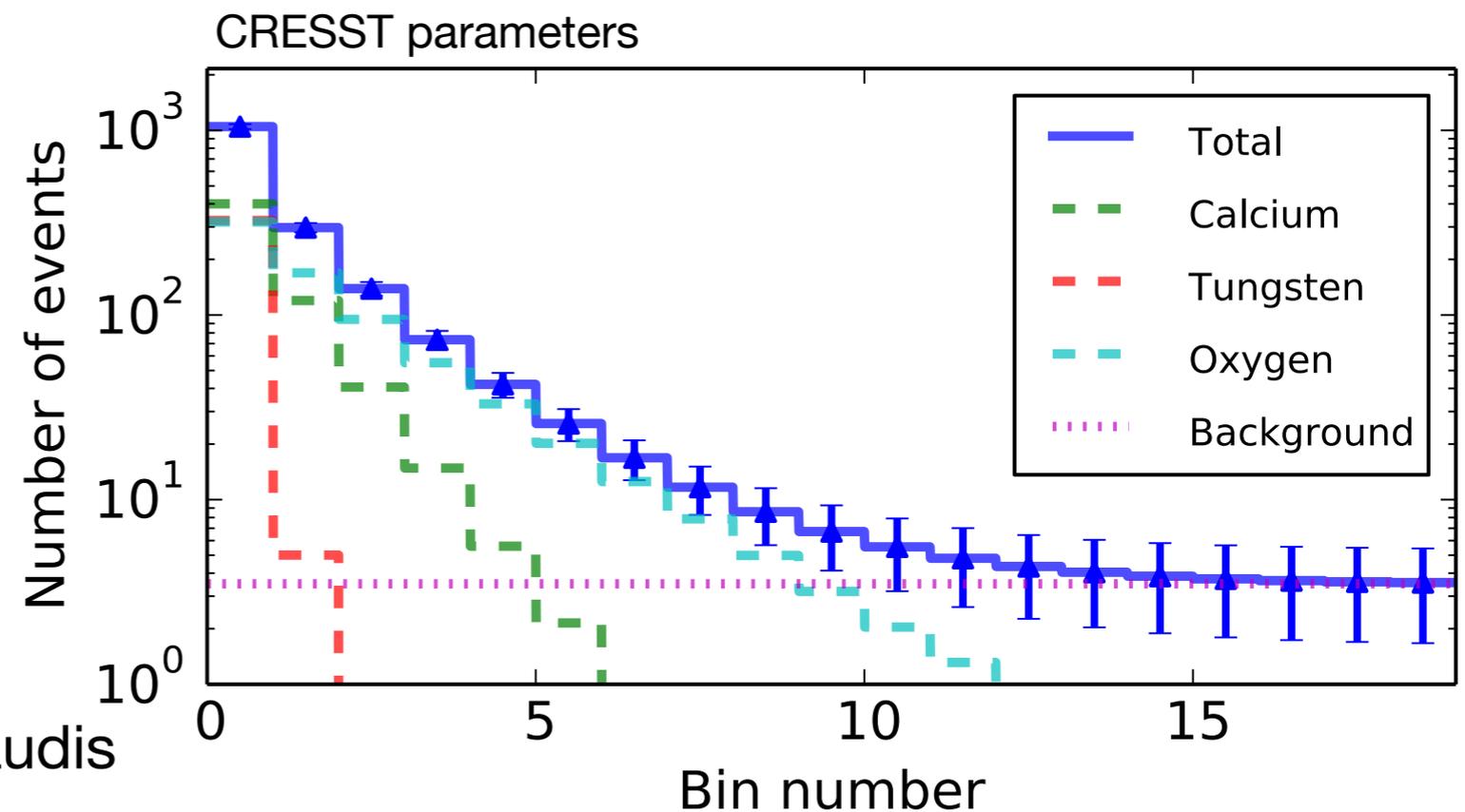
- Recoil spectrum shape important: need **good energy resolution**

See Gelmini et al. arxiv:1612.09137

- Cryogenic detectors are ideal for this!

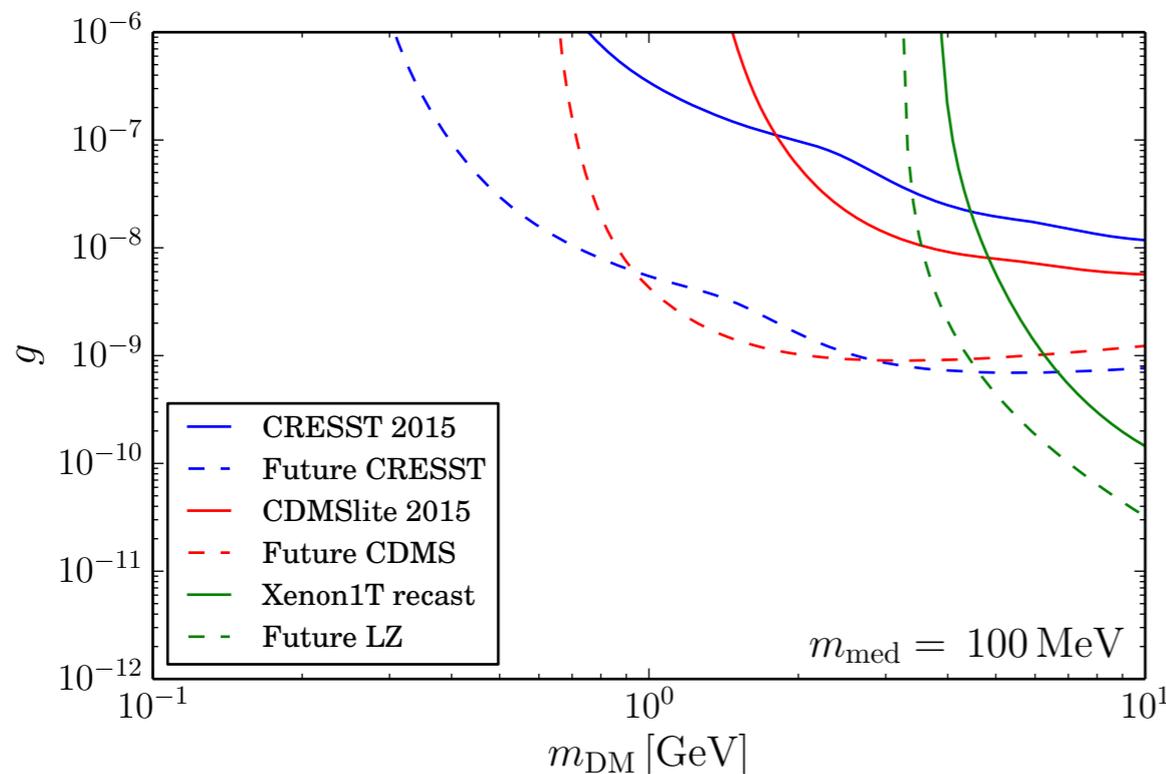


Shamelessly stolen from talk by L. Baudis

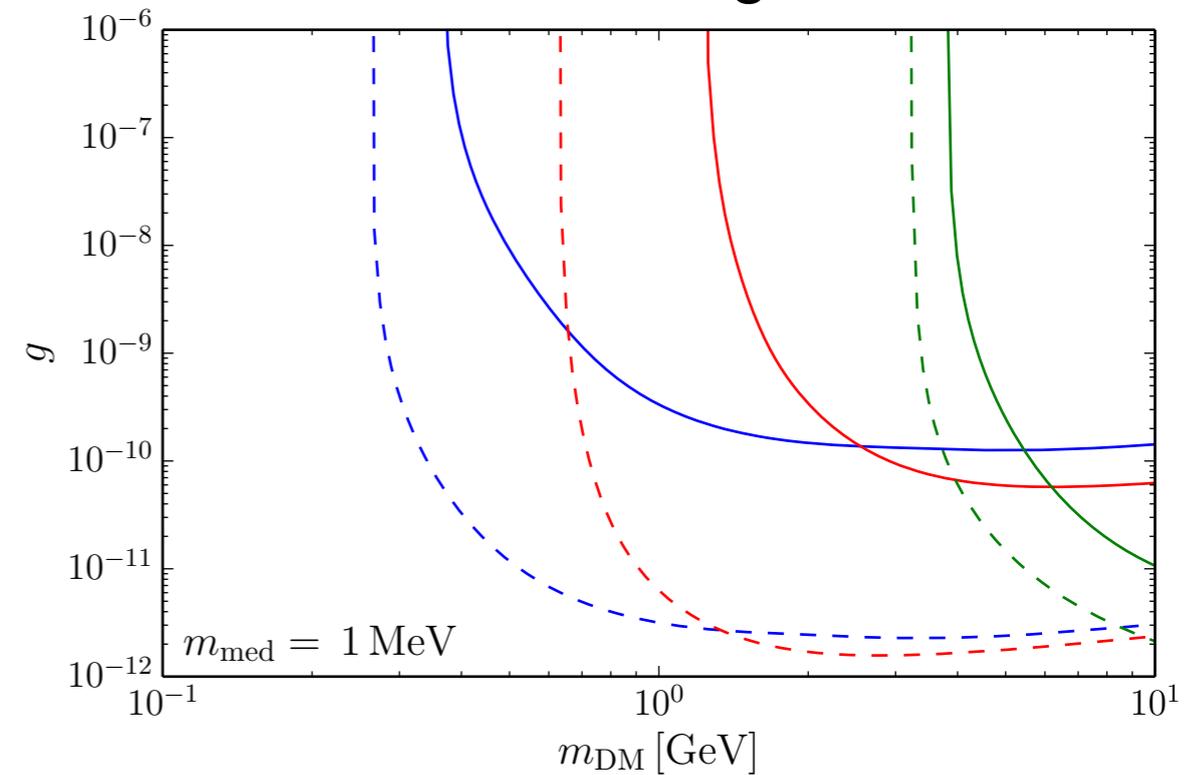


Kulkarni et. al. JCAP 1711 (2017) no.11, 016

Traditional limits on DM space

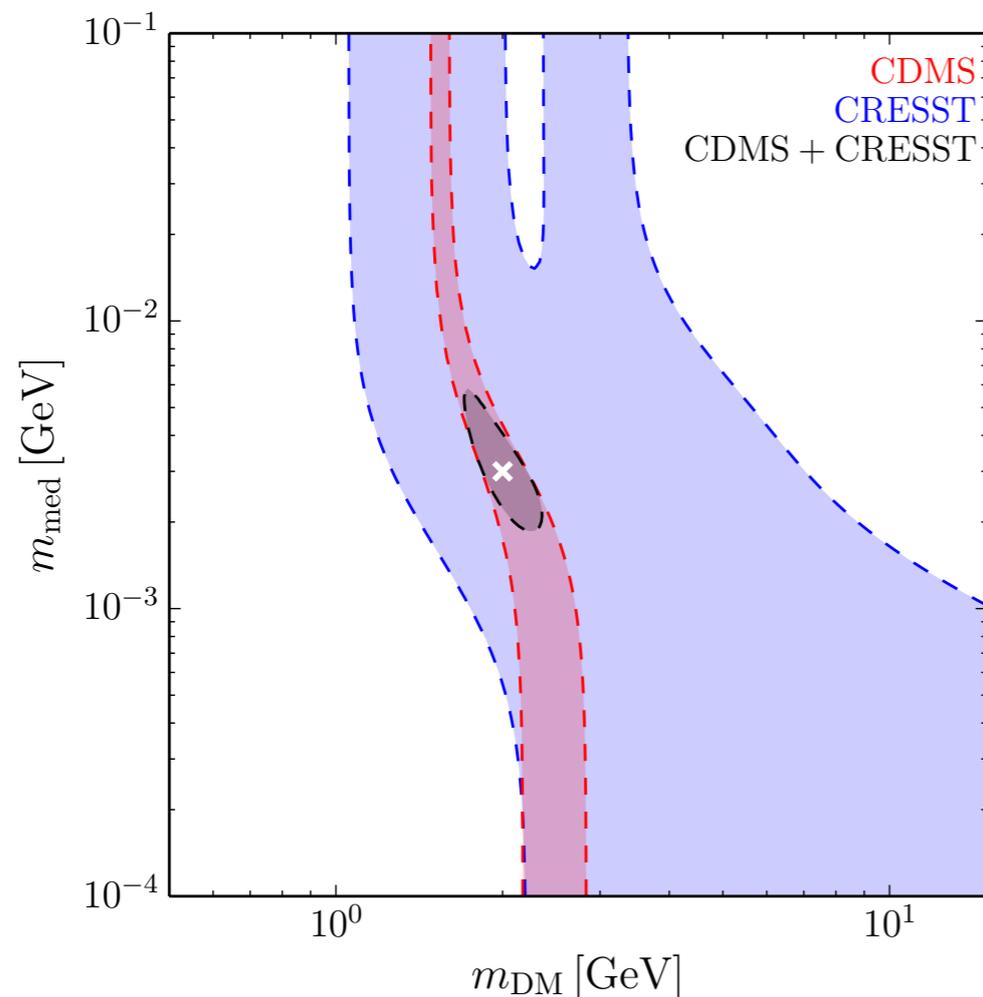


Limits on models with light mediators

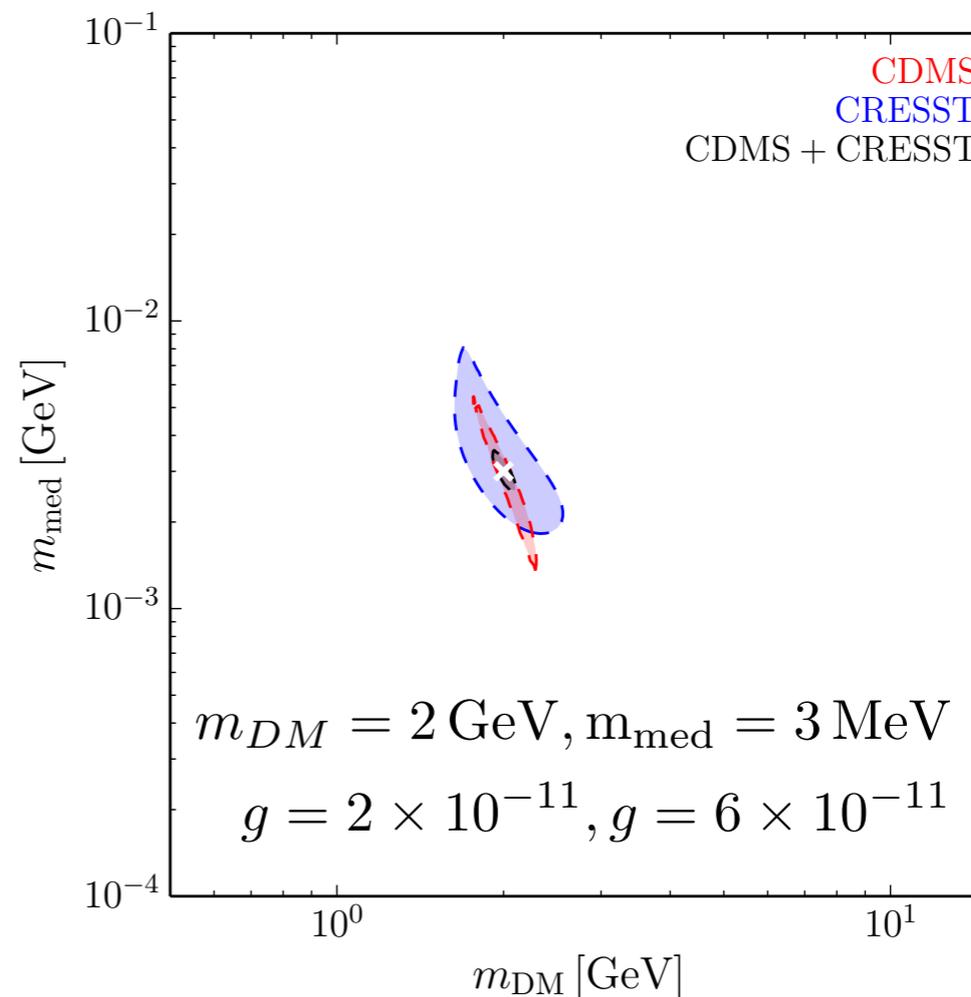


- g = product of SM - mediator and DM - mediator coupling
- Best sensitivity of cryogenic experiments for DM masses with light mediators ~ 10 GeV
- **Two orders of magnitude** improvement for effective coupling g , corresponds to up to **four orders of magnitude** in terms of the scattering rate.
- **Thousands of events** can be observed!!

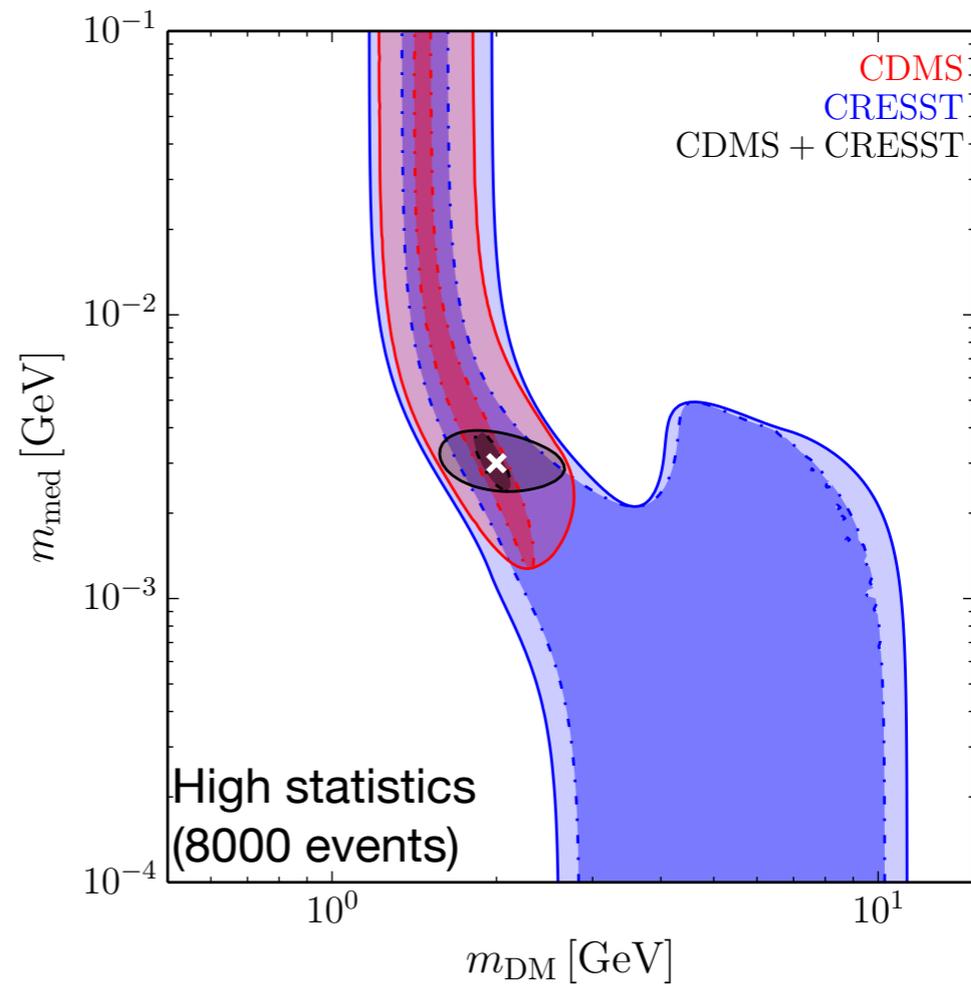
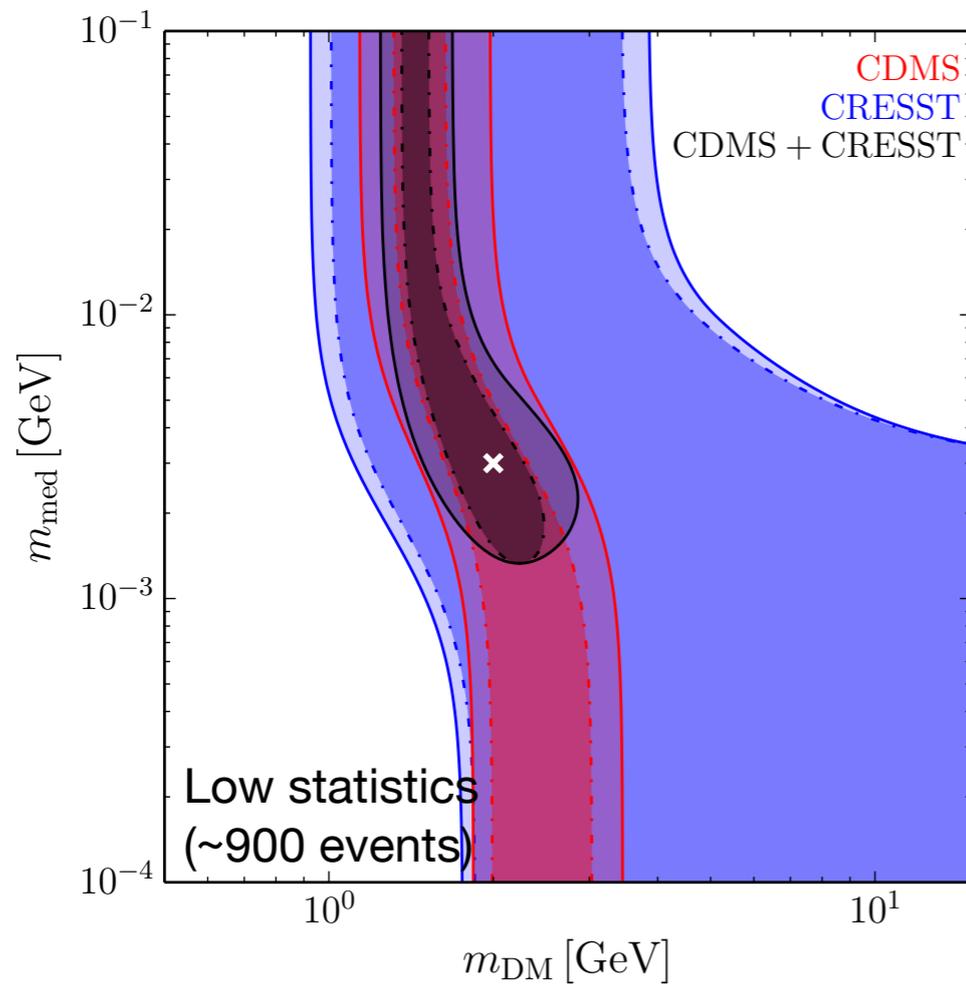
Low statistics (~900 events)



High statistics (8000 events total)

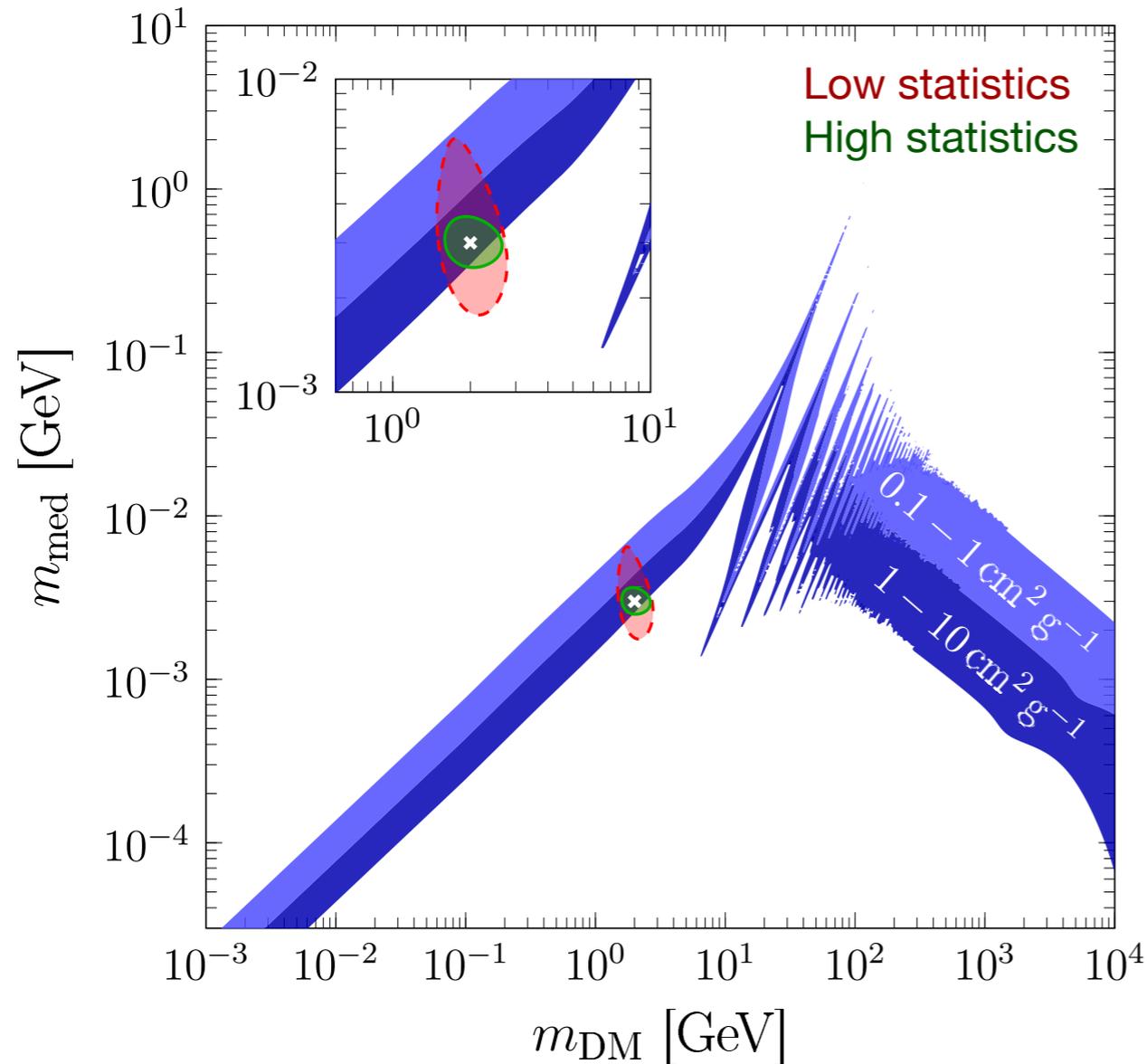


- Let us assume, we **know the backgrounds**, there are **no astrophysical uncertainties**, also let's assume DM couples to protons only
- Realistic treatment including detector resolution and background events
- Coupling g a nuisance parameter for reconstruction (fixed at max likelihood)



Solid curve = astrophysical uncertainties

- Even with astrophysical uncertainties, it is possible to reconstruct particle physics parameters
- Combination of data from different experiments better than single experiment



See also

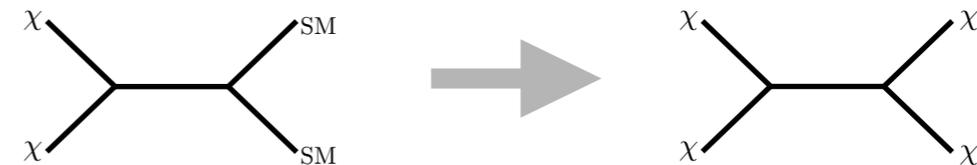
Vogelsberger et al. arXiv:1211.1377

Chen et al. arXiv:1505.03781

Del Nobile et al. arXiv:1507.04007

For plot:

Tulin et. al. arXiv:1302.3898

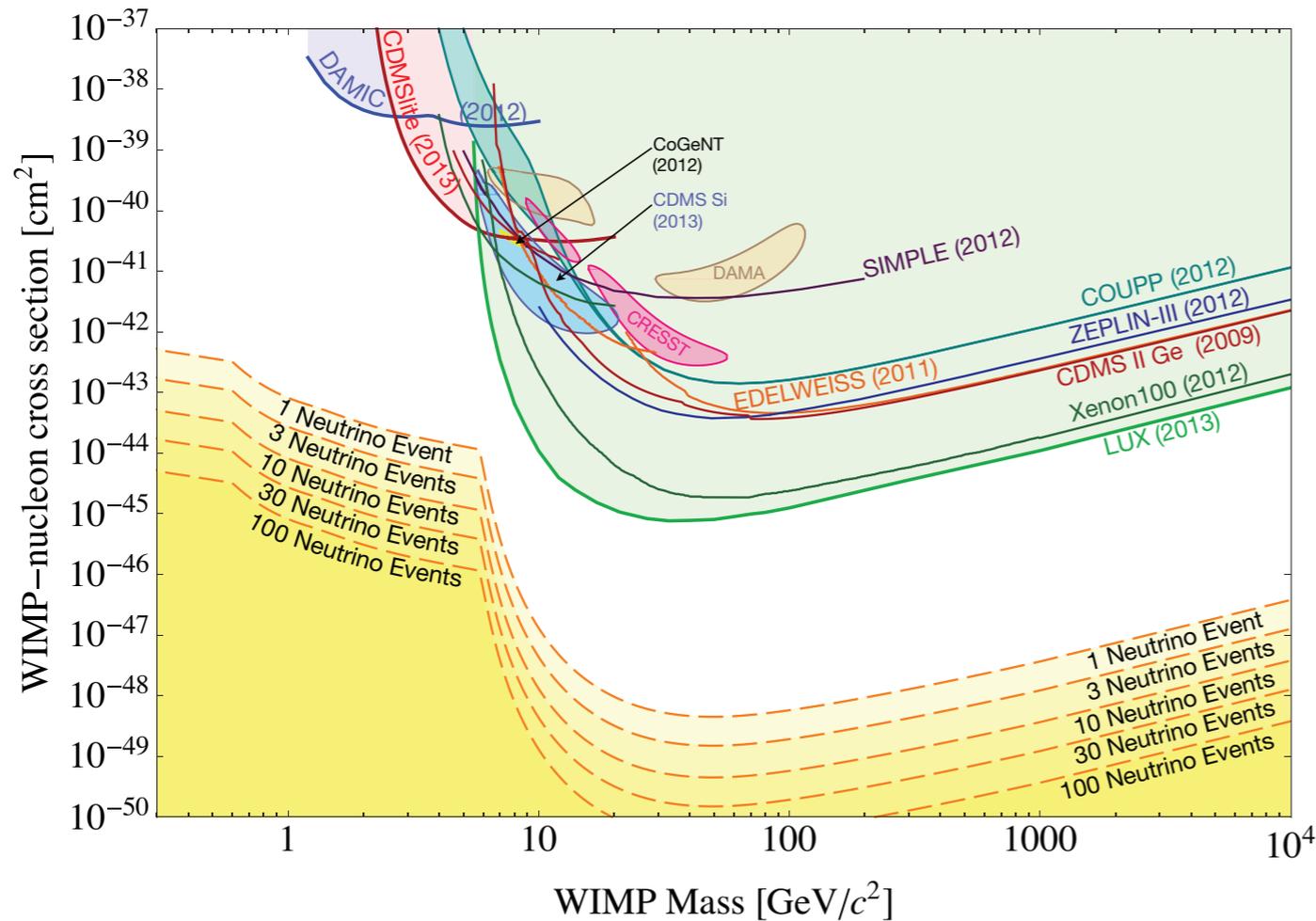


- Within **specific model** (not a general conclusion)
- Fermionic DM, scalar mediator
 - Relic via dark sector freeze out and mediator decay via Higgs mixing

- Investigating particle nature of dark matter is a crucial avenue for fundamental physics
- Plenty of new ideas for dark matter theories and a plethora of experimental searches ongoing
- Experiments and theory are no longer two separate fields but have to make progress hand in hand
- Multiple possibilities for progress however each possibility should be realistically evaluated
- Example 1: monojet is a powerful search for dark matter at the LHC, however the interpretation of these searches depends on the underlying theory scenario. The limits get stronger shall there be momentum dependence in DM - SM couplings
- Example 2: Direct detection experiments perfectly complement this quest at the LHC. While preparing for the end game at direct detection experiments, it will be important to consider complete BSM models rather than just one interaction
- Example 3: Having two direct detection low threshold experiments is better than having one for reconstructing parameters



- Two different setups: current and future LUX experiment
- Target Xenon
- Current setup
 - Take into account the efficiencies of the LUX experiment as given in LUXCalc
 - Exposure: 1.4×10^4 kg day (2013 results)
 - Number of observed events: 2, estimated background: 1.9 per ton year
- Future setup: similar to LZ
 - Keep the efficiencies the same
 - Exposure: 15 ton - year
 - background: 0.64 (including SM contribution)



$$\mathcal{L}(\sigma_{\chi-n}, \vec{\phi}) = \frac{e^{-(\mu_{\chi} + \sum_{j=1}^{n_{\nu}} \mu_{\nu}^j)}}{N!}$$

$$\times \prod_{i=1}^N \left[\mu_{\chi} f_{\chi}(E_{r_i}) + \sum_{j=1}^{n_{\nu}} \mu_{\nu}^j f_{\nu}^j(E_{r_i}) \right]$$

$$\times \prod_{i=1}^{n_{\nu}} \mathcal{L}_i(\phi_i),$$

$$\lambda(0) = \frac{\mathcal{L}(\sigma_{\chi-n} = 0, \vec{\phi})}{\mathcal{L}(\hat{\sigma}_{\chi-n}, \vec{\phi})}$$

- For a given target, consider one threshold, adjust exposure to attain N neutrino events
- Test the discrimination power between neutrino only and dark matter plus neutrino hypothesis by means of hypothesis testing

- **CRESST III**

See CRESST arXiv:1503.08065.

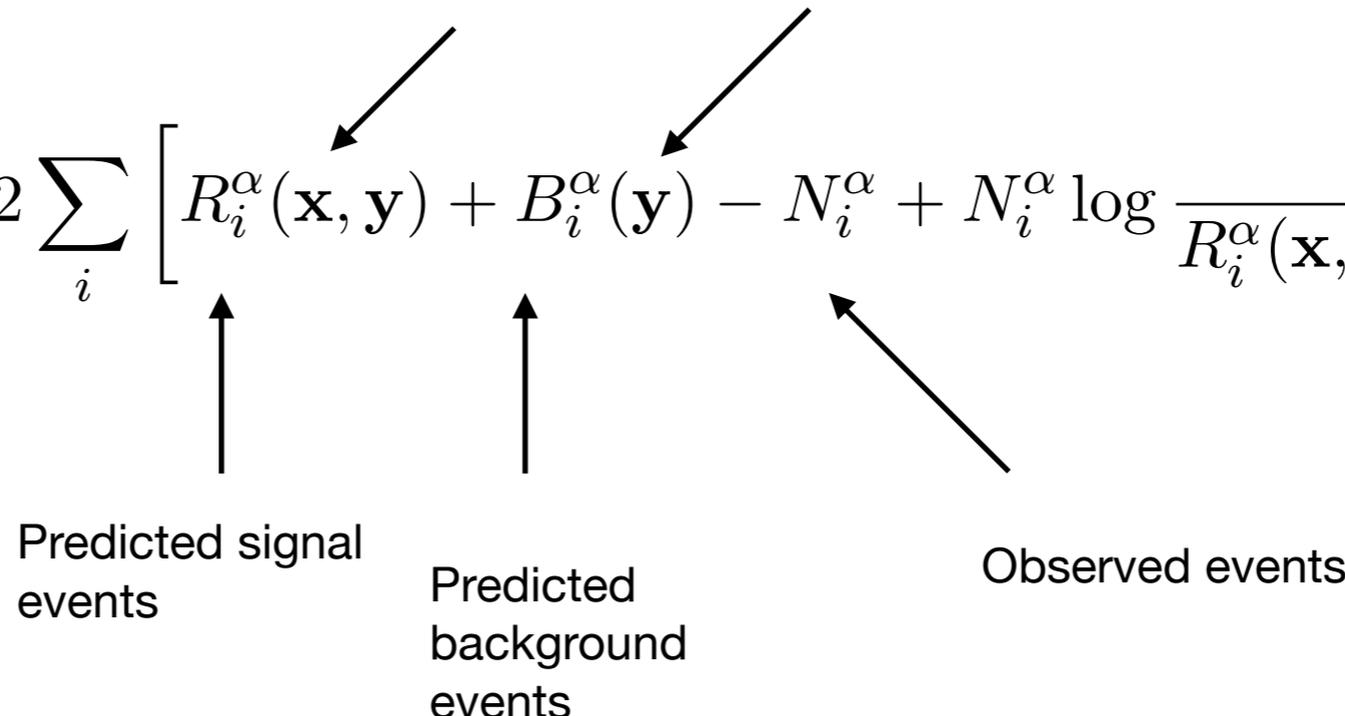
- Molecular experiment: target CaWO_4 , exposure: 1000 kg days
- Energy threshold: 100 eV
- Background level: $3.5 \times 10^{-2} \text{ keV}^{-1} \text{ kg}^{-1} \text{ day}^{-1} = 3.5 \text{ events each bin}$
- Flat efficiency and Gaussian energy resolution of 20 eV

- **SuperCDMS**

See SuperCDM arXiv:1610.00006

- High voltage Germanium, exposure $1.6 \times 10^4 \text{ kg days}$
- Energy threshold 100 eV (conservative)
- Background level: $10 \text{ keV}^{-1} \text{ kg}^{-1} \text{ year}^{-1}$
- Flat signal efficiency, energy resolution of 10 eV

- Generate mock data and attempt reconstruction
- Likelihood function

$$-2 \log \mathcal{L}^\alpha(\mathbf{x}, \mathbf{y}) = 2 \sum_i \left[R_i^\alpha(\mathbf{x}, \mathbf{y}) + B_i^\alpha(\mathbf{y}) - N_i^\alpha + N_i^\alpha \log \frac{N_i^\alpha}{R_i^\alpha(\mathbf{x}, \mathbf{y}) + B_i^\alpha(\mathbf{y})} \right]$$


Particle physics parameters

Nuisance parameters

Predicted signal events

Predicted background events

Observed events

- Construct likelihood ratio (\mathcal{R}), log likelihood follows a chi-square
- Exclude parameters, for two free parameter model if:

$$-2 \log \mathcal{R} < 5.99$$