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GUTs and all that...

Proton lifetime in minimal gauge unifications

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Outline

Proton decay from the SM perspective

Proton decay in BSM physics

Experimental situation

Grand unifications as theories of proton decay

Proton lifetime estimates in GUTs

Minimal “reasonably calculable” models (?)

Proton decay from the GSW Standard model perspective

The SM lagrangian

$$\begin{aligned}
\mathcal{L}_{SM} = & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
& M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - ig c_w (\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - \\
& Z_\nu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)) - ig s_w (\partial_\nu A_\mu (W_\mu^+ W_\nu^- - \\
& W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)) - \\
& \frac{1}{2}g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\mu^+ W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\mu^0 W_\nu^+ W_\nu^-) + \\
& g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w (A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - \\
& 2 A_\mu Z_\mu^0 W_\nu^+ W_\nu^-) - \frac{1}{2}\partial_\mu H \partial_\mu H - 2M^2 \alpha_h H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \\
& \beta_h \left(\frac{2M^2}{g^2} + \frac{2M}{g} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right) + \frac{2M^4}{g^2} \alpha_h - g \alpha_h M (H^3 + H \phi^0 \phi^0 + 2H \phi^+ \phi^-) - \\
& \frac{1}{8}g^2 \alpha_h (H^4 + (\phi^0)^4 + 4(\phi^+ \phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2) - g M W_\mu^+ W_\mu^- H - \\
& \frac{1}{2}g \frac{M}{c_w} Z_\mu^0 Z_\mu^0 H - \frac{1}{2}ig (W_\mu^+ (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W_\mu^- (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0)) + \\
& \frac{1}{2}g (W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) + W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H)) + \frac{1}{2}g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) + \\
& M (\frac{1}{c_w} Z_\mu^0 \partial_\mu \phi^0 + W_\mu^+ \partial_\mu \phi^- + W_\mu^- \partial_\mu \phi^+) - ig \frac{s_w^2}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + ig s_w M A_\mu (W_\mu^+ \phi^- - \\
& W_\mu^- \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \\
& \frac{1}{4}g^2 W_\mu^+ W_\mu^- (H^2 + (\phi^0)^2 + 2\phi^+ \phi^-) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z_\mu^0 Z_\mu^0 (H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-) - \\
& \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) - \frac{1}{2}ig^2 \frac{s_w^2}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\
& W_\mu^- \phi^+) + \frac{1}{2}ig^2 s_w A_\mu H (W_\mu^+ \phi^- - W_\mu^- \phi^+) - g^2 \frac{s_w}{c_w} (2c_w^2 - 1) Z_\mu^0 A_\mu \phi^+ \phi^- - g^2 s_w^2 A_\mu A_\mu \phi^+ \phi^- + \\
& \frac{1}{2}ig_s \lambda_{ij}^a (\bar{q}_i^\sigma \gamma^\mu q_j^\sigma) g_\mu^a - \bar{e}^\lambda (\gamma \partial + m_e^\lambda) e^\lambda - \bar{\nu}^\lambda (\gamma \partial + m_\nu^\lambda) \nu^\lambda - \bar{u}_j^\lambda (\gamma \partial + m_u^\lambda) u_j^\lambda - \bar{d}_j^\lambda (\gamma \partial + m_d^\lambda) d_j^\lambda + \\
& ig s_w A_\mu \left(-(\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3}(\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda) \right) + \frac{ig}{4c_w} Z_\mu^0 \{ (\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - \\
& 1 - \gamma^5) e^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (\frac{4}{3}s_w^2 - 1 - \gamma^5) d_j^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (1 - \frac{8}{3}s_w^2 + \gamma^5) u_j^\lambda) \} + \\
& \frac{ig}{2\sqrt{2}} W_\mu^+ \left((\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) U^{lep}{}_{\lambda\kappa} e^\kappa) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa) \right) + \\
& \frac{ig}{2\sqrt{2}} W_\mu^- \left((\bar{e}^\kappa U^{lep\dagger}{}_{\kappa\lambda} \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\kappa C_{\kappa\lambda}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda) \right) + \\
& \frac{ig}{2M\sqrt{2}} \phi^+ (-m_e^\kappa (\bar{\nu}^\lambda U^{lep}{}_{\lambda\kappa} (1 - \gamma^5) e^\kappa) + m_\nu^\lambda (\bar{\nu}^\lambda U^{lep}{}_{\lambda\kappa} (1 + \gamma^5) e^\kappa) + \\
& \frac{ig}{2M\sqrt{2}} \phi^- (m_e^\lambda (\bar{e}^\lambda U^{lep\dagger}{}_{\lambda\kappa} (1 + \gamma^5) \nu^\kappa) - m_\nu^\kappa (\bar{e}^\lambda U^{lep\dagger}{}_{\lambda\kappa} (1 - \gamma^5) \nu^\kappa) - \frac{g}{2} \frac{m_e^\lambda}{M} H (\bar{\nu}^\lambda \nu^\lambda) - \\
& \frac{g}{2} \frac{m_e^\lambda}{M} H (\bar{e}^\lambda e^\lambda) + \frac{ig}{2} \frac{m_\nu^\lambda}{M} \phi^0 (\bar{\nu}^\lambda \gamma^5 \nu^\lambda) - \frac{ig}{2} \frac{m_e^\lambda}{M} \phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda) - \frac{1}{4} \bar{\nu}_\lambda M_{\lambda\kappa}^R (1 - \gamma_5) \hat{\nu}_\kappa - \\
& \frac{1}{4} \bar{\nu}_\lambda M_{\lambda\kappa}^R (1 - \gamma_5) \hat{\nu}_\kappa + \frac{ig}{2M\sqrt{2}} \phi^+ (-m_d^\kappa (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\kappa) + m_u^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \gamma^5) d_j^\kappa) + \\
& \frac{ig}{2M\sqrt{2}} \phi^- (m_d^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\kappa) - m_u^\kappa (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \gamma^5) u_j^\kappa) - \frac{g}{2} \frac{m_u^\lambda}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \frac{g}{2} \frac{m_d^\lambda}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \\
& \frac{ig}{2} \frac{m_u^\lambda}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{ig}{2} \frac{m_d^\lambda}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda)
\end{aligned}$$

The SM lagrangian

$$\begin{aligned}
\mathcal{L}_{SM} = & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
& M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - ig c_w (\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - \\
& Z_\nu^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + Z_\mu^0 (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)) - ig s_w (\partial_\nu A_\mu (W_\mu^+ W_\nu^- - \\
& W_\nu^+ W_\mu^-) - A_\nu (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + A_\mu (W_\nu^+ \partial_\nu W_\mu^- - W_\nu^- \partial_\nu W_\mu^+)) - \\
& \frac{1}{2}g^2 W_\mu^+ W_\mu^- W_\nu^+ W_\nu^- + \frac{1}{2}g^2 W_\mu^+ W_\nu^- W_\mu^+ W_\nu^- + g^2 c_w^2 (Z_\mu^0 W_\mu^+ Z_\nu^0 W_\nu^- - Z_\mu^0 Z_\mu^0 W_\nu^+ W_\nu^-) + \\
& g^2 s_w^2 (A_\mu W_\mu^+ A_\nu W_\nu^- - A_\mu A_\mu W_\nu^+ W_\nu^-) + g^2 s_w c_w (A_\mu Z_\nu^0 (W_\mu^+ W_\nu^- - W_\nu^+ W_\mu^-) - \\
& 2 A_\mu Z_\mu^0 W_\nu^+ W_\nu^-) - \frac{1}{2}\partial_\mu H \partial_\mu H - 2M^2 \alpha_h H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \\
& \beta_h \left(\frac{2M^2}{g^2} + \frac{2M}{g} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right) + \frac{2M^4}{g^2} \alpha_h - g \alpha_h M (H^3 + H \phi^0 \phi^0 + 2H \phi^+ \phi^-) - \\
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& \frac{1}{2}g (W_\mu^+ (H \partial_\mu \phi^- - \phi^- \partial_\mu H) + W_\mu^- (H \partial_\mu \phi^+ - \phi^+ \partial_\mu H)) + \frac{1}{2}g \frac{1}{c_w} (Z_\mu^0 (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) + \\
& M (\frac{1}{c_w} Z_\mu^0 \partial_\mu \phi^0 + W_\mu^+ \partial_\mu \phi^- + W_\mu^- \partial_\mu \phi^+) - ig \frac{s_w^2}{c_w} M Z_\mu^0 (W_\mu^+ \phi^- - W_\mu^- \phi^+) + ig s_w M A_\mu (W_\mu^+ \phi^- - \\
& W_\mu^- \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z_\mu^0 (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \\
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& \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z_\mu^0 \phi^0 (W_\mu^+ \phi^- + W_\mu^- \phi^+) - \frac{1}{2}ig^2 \frac{s_w^2}{c_w} Z_\mu^0 H (W_\mu^+ \phi^- - W_\mu^- \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0 (W_\mu^+ \phi^- + \\
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& \frac{1}{2}ig_s \lambda_{ij}^a (\bar{q}_i^\sigma \gamma^\mu q_j^\sigma) g_\mu^a - \bar{e}^\lambda (\gamma \partial + m_e^\lambda) e^\lambda - \bar{\nu}^\lambda (\gamma \partial + m_\nu^\lambda) \nu^\lambda - \bar{u}_j^\lambda (\gamma \partial + m_u^\lambda) u_j^\lambda - \bar{d}_j^\lambda (\gamma \partial + m_d^\lambda) d_j^\lambda + \\
& ig s_w A_\mu \left(-(\bar{e}^\lambda \gamma^\mu e^\lambda) + \frac{2}{3}(\bar{u}_j^\lambda \gamma^\mu u_j^\lambda) - \frac{1}{3}(\bar{d}_j^\lambda \gamma^\mu d_j^\lambda) \right) + \frac{ig}{4c_w} Z_\mu^0 \{ (\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{e}^\lambda \gamma^\mu (4s_w^2 - \\
& 1 - \gamma^5) e^\lambda) + (\bar{d}_j^\lambda \gamma^\mu (\frac{4}{3}s_w^2 - 1 - \gamma^5) d_j^\lambda) + (\bar{u}_j^\lambda \gamma^\mu (1 - \frac{8}{3}s_w^2 + \gamma^5) u_j^\lambda) \} + \\
& \boxed{\frac{ig}{2\sqrt{2}} W_\mu^+ \left((\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) U^{lep}{}_{\lambda\kappa} e^\kappa) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa) \right) + \\
& \frac{ig}{2\sqrt{2}} W_\mu^- \left((\bar{e}^\kappa U^{lep\dagger}{}_{\kappa\lambda} \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\kappa C_{\kappa\lambda}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda) \right) + \\
& \frac{ig}{2M\sqrt{2}} \phi^+ \left(-m_e^\kappa (\bar{\nu}^\lambda U^{lep}{}_{\lambda\kappa} (1 - \gamma^5) e^\kappa) + m_\nu^\lambda (\bar{\nu}^\lambda U^{lep}{}_{\lambda\kappa} (1 + \gamma^5) e^\kappa) \right) + \\
& \frac{ig}{2M\sqrt{2}} \phi^- \left(m_e^\lambda (\bar{e}^\lambda U^{lep\dagger}{}_{\lambda\kappa} (1 + \gamma^5) \nu^\kappa) - m_\nu^\kappa (\bar{e}^\lambda U^{lep\dagger}{}_{\lambda\kappa} (1 - \gamma^5) \nu^\kappa) \right) - \frac{g}{2} \frac{m_e^\lambda}{M} H (\bar{\nu}^\lambda \nu^\lambda) - \\
& \frac{g}{2} \frac{m_e^\lambda}{M} H (\bar{e}^\lambda e^\lambda) + \frac{ig}{2} \frac{m_\nu^\lambda}{M} \phi^0 (\bar{\nu}^\lambda \gamma^5 \nu^\lambda) - \frac{ig}{2} \frac{m_e^\lambda}{M} \phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda) - \frac{1}{4} \bar{\nu}_\lambda M_{\lambda\kappa}^R (1 - \gamma_5) \hat{\nu}_\kappa - \\
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& \frac{ig}{2M\sqrt{2}} \phi^- \left(m_d^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\kappa) - m_u^\kappa (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \gamma^5) u_j^\kappa) \right) - \frac{g}{2} \frac{m_u^\lambda}{M} H (\bar{u}_j^\lambda u_j^\lambda) - \frac{g}{2} \frac{m_d^\lambda}{M} H (\bar{d}_j^\lambda d_j^\lambda) + \\
& \frac{ig}{2} \frac{m_u^\lambda}{M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{ig}{2} \frac{m_d^\lambda}{M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda)}
\end{aligned}$$

The SM lagrangian

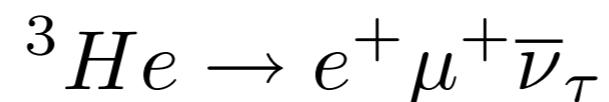
$$\begin{aligned}
& \frac{ig}{2\sqrt{2}} W_\mu^+ \left((\bar{\nu}^\lambda \gamma^\mu (1 + \gamma^5) U^{lep}{}_{\lambda\kappa} e^\kappa) + (\bar{u}_j^\lambda \gamma^\mu (1 + \gamma^5) C_{\lambda\kappa} d_j^\kappa) \right) + \\
& \frac{ig}{2\sqrt{2}} W_\mu^- \left((\bar{e}^\kappa U^{lep\dagger}{}_{\kappa\lambda} \gamma^\mu (1 + \gamma^5) \nu^\lambda) + (\bar{d}_j^\kappa C_{\kappa\lambda}^\dagger \gamma^\mu (1 + \gamma^5) u_j^\lambda) \right) + \\
& \frac{ig}{2M\sqrt{2}} \phi^+ \left(-m_e^\kappa (\bar{\nu}^\lambda U^{lep}{}_{\lambda\kappa} (1 - \gamma^5) e^\kappa) + m_\nu^\lambda (\bar{\nu}^\lambda U^{lep}{}_{\lambda\kappa} (1 + \gamma^5) e^\kappa) \right) + \\
& \frac{ig}{2M\sqrt{2}} \phi^- \left(m_e^\lambda (\bar{e}^\lambda U^{lep\dagger}{}_{\lambda\kappa} (1 + \gamma^5) \nu^\kappa) - m_\nu^\kappa (\bar{e}^\lambda U^{lep\dagger}{}_{\lambda\kappa} (1 - \gamma^5) \nu^\kappa) \right) - \frac{g m_\nu^\lambda}{2M} H (\bar{\nu}^\lambda \nu^\lambda) - \\
& \frac{g m_e^\lambda}{2M} H (\bar{e}^\lambda e^\lambda) + \frac{ig m_\nu^\lambda}{2M} \phi^0 (\bar{\nu}^\lambda \gamma^5 \nu^\lambda) - \frac{ig m_e^\lambda}{2M} \phi^0 (\bar{e}^\lambda \gamma^5 e^\lambda) - \frac{1}{4} \bar{\nu}_\lambda M_{\lambda\kappa}^R (1 - \gamma_5) \hat{\nu}_\kappa - \\
& \frac{1}{4} \bar{\nu}_\lambda M_{\lambda\kappa}^R (1 - \gamma_5) \hat{\nu}_\kappa + \frac{ig}{2M\sqrt{2}} \phi^+ \left(-m_d^\kappa (\bar{u}_j^\lambda C_{\lambda\kappa} (1 - \gamma^5) d_j^\kappa) + m_u^\lambda (\bar{u}_j^\lambda C_{\lambda\kappa} (1 + \gamma^5) d_j^\kappa) \right) + \\
& \frac{ig}{2M\sqrt{2}} \phi^- \left(m_d^\lambda (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 + \gamma^5) u_j^\kappa) - m_u^\kappa (\bar{d}_j^\lambda C_{\lambda\kappa}^\dagger (1 - \gamma^5) u_j^\kappa) \right) - \frac{g m_u^\lambda}{2M} H (\bar{u}_j^\lambda u_j^\lambda) - \frac{g m_d^\lambda}{2M} H (\bar{d}_j^\lambda d_j^\lambda) + \\
& \frac{ig m_u^\lambda}{2M} \phi^0 (\bar{u}_j^\lambda \gamma^5 u_j^\lambda) - \frac{ig m_d^\lambda}{2M} \phi^0 (\bar{d}_j^\lambda \gamma^5 d_j^\lambda)
\end{aligned}$$

always a $\overline{\Psi}\Psi$ structure - B & L perturbatively conserved

B & L violation in the SM

Only by anomalies (at the renormalizable level)

- Instantons (at zero T) cause $9q + 3l \leftrightarrow \emptyset$ with immeasurably small rates



$$\mathcal{A} \sim e^{-2\pi/\alpha} \sim 10^{-\mathcal{O}(100)}$$

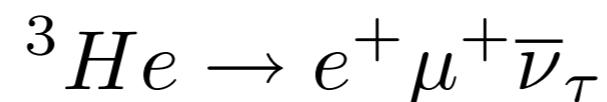
- Sphalerons (at high T) make the tunneling more efficient \Rightarrow leptogenesis

Kuzmin, V. Rubakov, M. Shaposhnikov, PLB155, 1985 Fukugita, Yanagida, PLB174, 1986

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neutrinos are massive, renormalizability may not be fundamental

Perturbative L violation in the SM with massive neutrinos

Standard model with massive neutrinos

neutron neutrality + neutrino masses

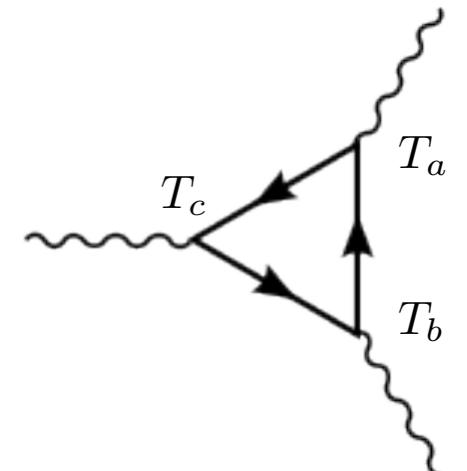
suggest

perturbative L violation

(Hyper)charge quantization in the Standard model

$SU(3) \times SU(2) \times U(1)$ gauge anomalies

$$\mathcal{A}_c \propto \frac{1}{32\pi^2} \text{Tr} (\{T_a, T_b\} T_c) \tilde{F}_{\mu\nu}^a F^{b\mu\nu}$$



(Hyper)charge quantization in the Standard model

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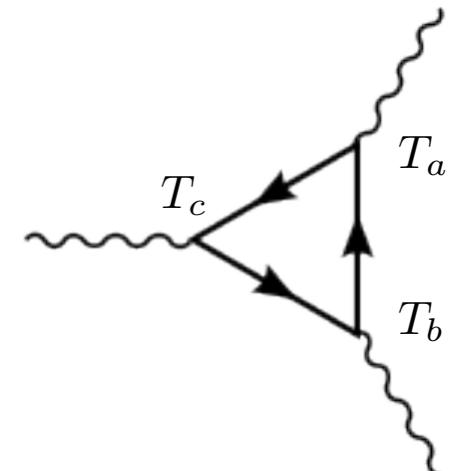
$$\mathcal{A}_c \propto \frac{1}{32\pi^2} \text{Tr} (\{T_a, T_b\} T_c) \tilde{F}_{\mu\nu}^a F^{b\mu\nu}$$

$SU(2)^2 U(1)$:

$$6Y_Q + 2Y_L = 0$$

$U(1)^3$:

$$12Y_Q^3 + 4Y_L^3 - 6Y_U^3 - 6Y_D^3 - 2Y_E^3 = 0$$



(Hyper)charge quantization in the Standard model

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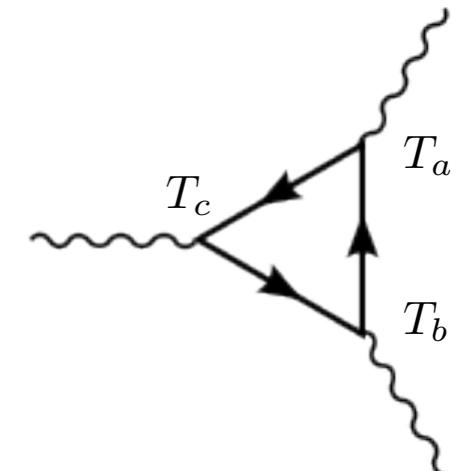
$$\mathcal{A}_c \propto \frac{1}{32\pi^2} \text{Tr} (\{T_a, T_b\} T_c) \tilde{F}_{\mu\nu}^a F^{b\mu\nu}$$

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Yukawas: $Y_{Dij} \overline{Q_L}_i \langle H \rangle D_{Rj} + Y_{Uij} \overline{Q_L}_i \langle \tilde{H} \rangle U_{Rj} + Y_{Eij} \overline{L_L}_i \langle H \rangle E_{Rj}$

$$-Y_Q + Y_D + Y_H = 0$$

$$-Y_L + Y_E + Y_H = 0$$

$$-Y_Q + Y_U - Y_H = 0$$

(Hyper)charge quantization in the Standard model

$SU(3) \times SU(2) \times U(1)$ gauge anomalies

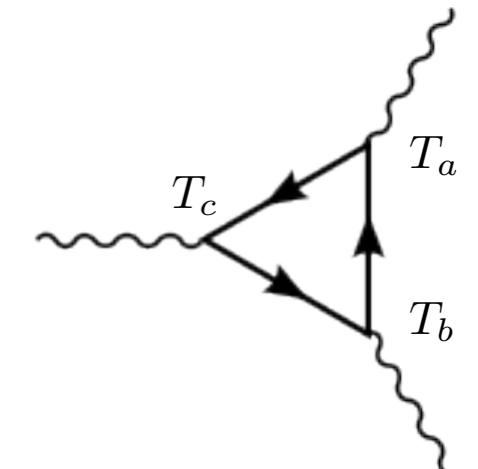
$$\mathcal{A}_c \propto \frac{1}{32\pi^2} \text{Tr} (\{T_a, T_b\} T_c) \tilde{F}_{\mu\nu}^a F^{b\mu\nu}$$

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Solution:
$$\boxed{Y_Q = +\frac{1}{6}, Y_U = +\frac{2}{3}, Y_D = -\frac{1}{3}, Y_L = -\frac{1}{2}, Y_E = -1}$$

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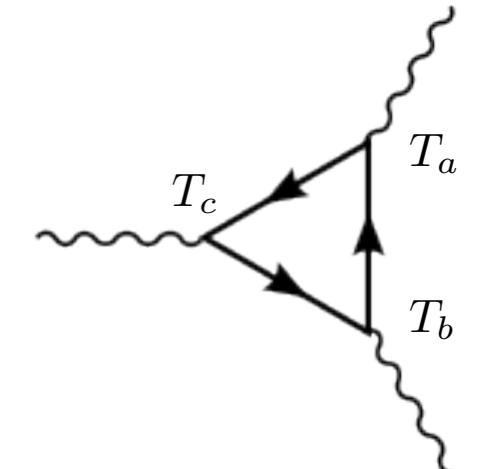
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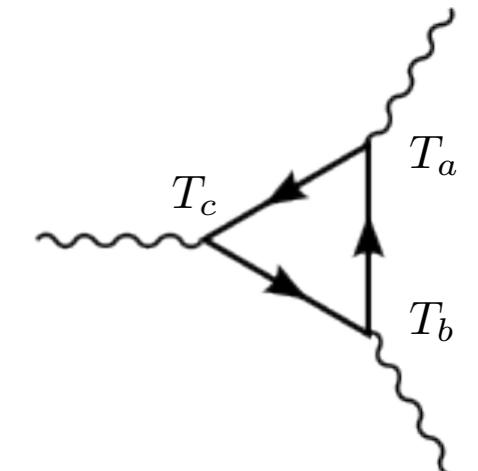
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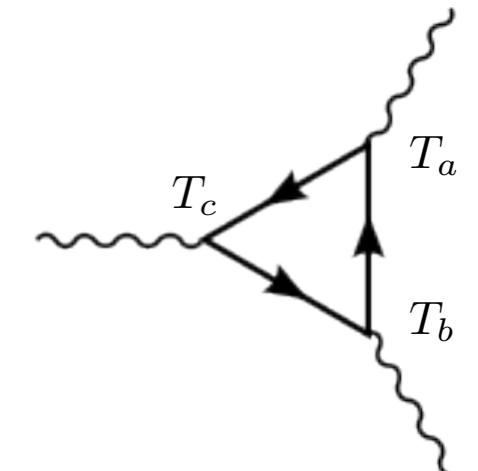
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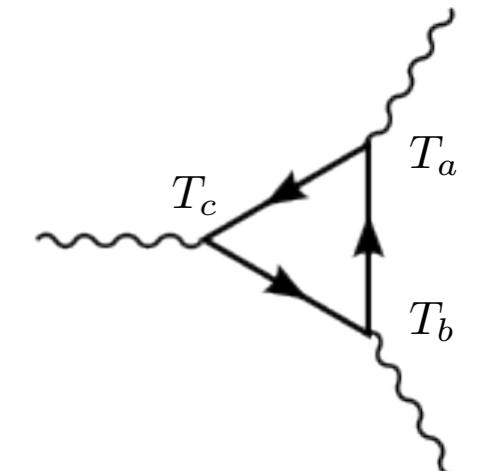
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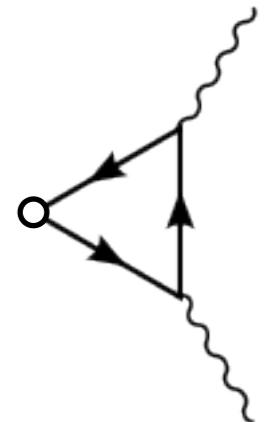
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$$\boxed{Y_Q = +\frac{1}{6} - \frac{1}{3}Y_N, Y_U = +\frac{2}{3} - \frac{1}{3}Y_N, Y_D = -\frac{1}{3} - \frac{1}{3}Y_N, \\ Y_L = -\frac{1}{2} + Y_N, Y_E = -1 + Y_N \quad Y_N \in \mathbb{R}}$$

A simpler symmetry argument

B and L anomalies & RH neutrino

$$\mathrm{Tr}(\{Y, Y\}(B - L)) = 0 , \mathrm{Tr}(\{T_L^3, T_L^3\}(B - L)) = 0 ,$$

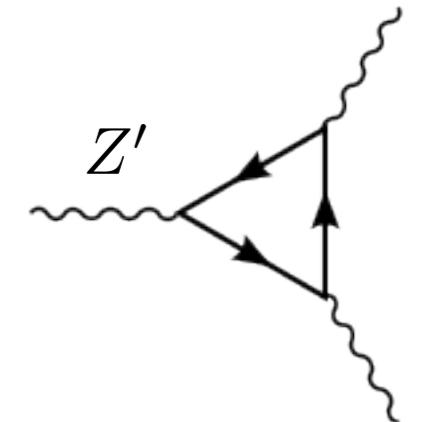


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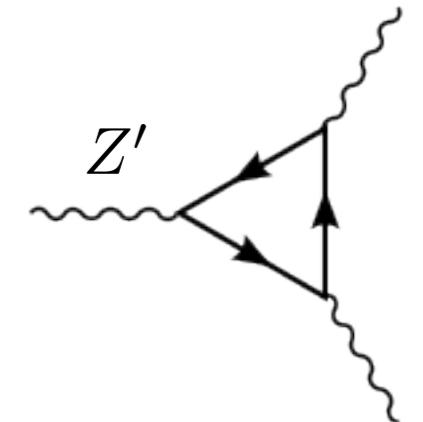


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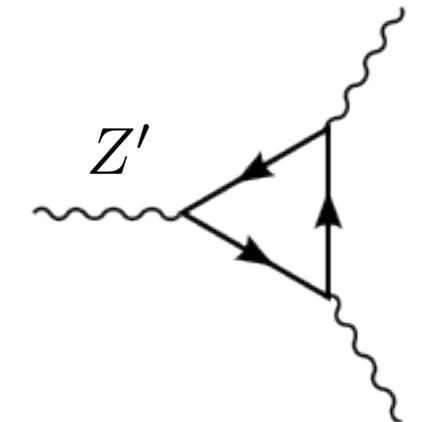
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Babu, Mohapatra, Phys.Rev. D41 (1990) 271

Experimentally (neutron neutrality): $|\varepsilon| < 10^{-21}$

Foot, Lew, Volkas 1993

SM with massive neutrinos and quantized charges

Neutrinos should better not be Dirac!

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$$+\frac{1}{2} M_{Rij} \overline{N_{Ri}^c} N_{Rj} + h.c.$$

E. Majorana 1937

Majorana neutrino mass = **perturbative L violation**

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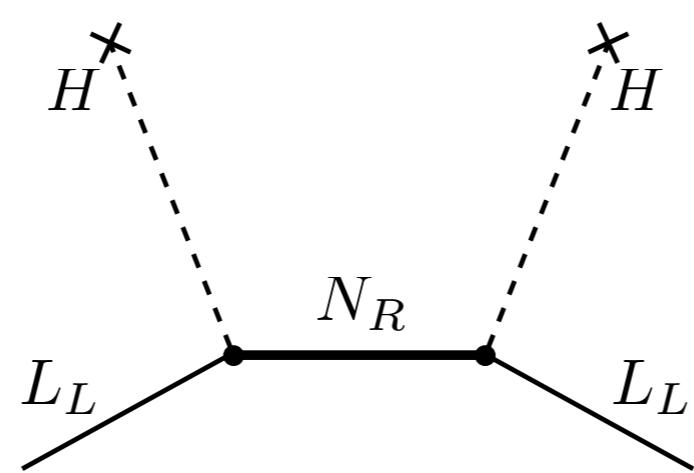
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Seesaw:



P. Minkowski, Phys. Lett. B67, 421 (1977)

Lepton number violation in oscillations

NB The first account of neutrino oscillations was indeed “L-violating”!



Kaon oscillations in 1957

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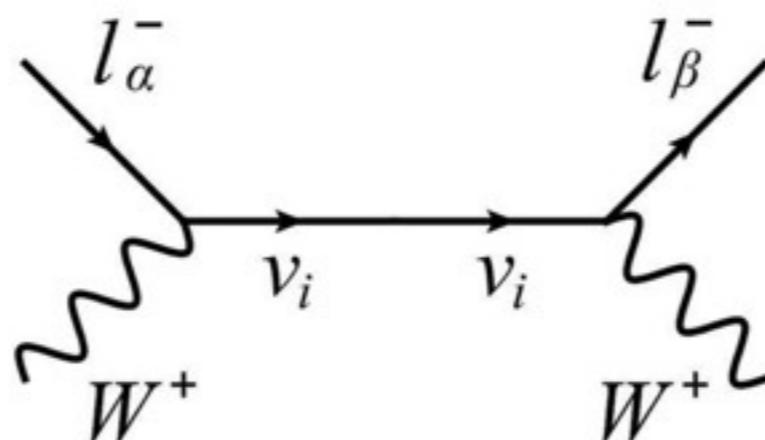
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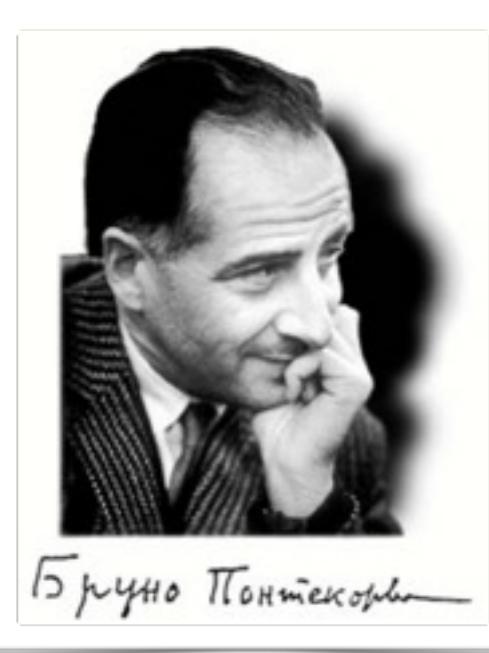
see e.g. E.Akhmedov, J. Kopp, JHEP 1004 (2010) 008



$$\mathcal{A}(\nu_\alpha \rightarrow \nu_\beta) \propto \sum_i U_{\alpha i}^* U_{\beta j}^* e^{-i \frac{m_i^2 L}{2E}}$$

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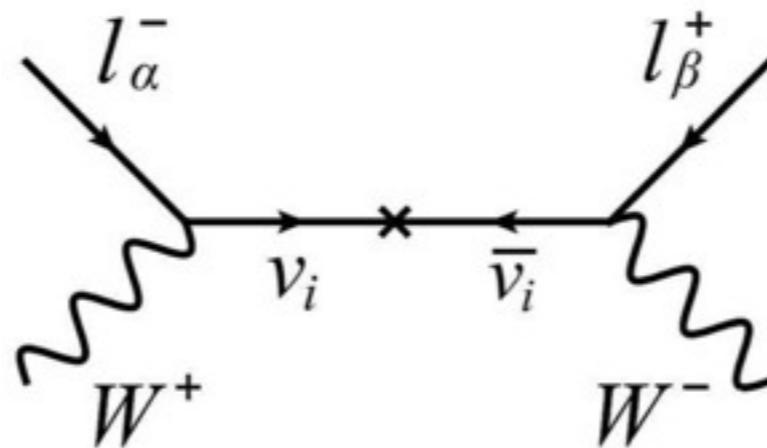
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suppressed...

see e.g. Z-z. Xing, arXiv:1301.7654v2

SM as an effective theory

LNV in the SM at d=5 level

Weinberg's d=5 operator $\mathcal{L} \ni \frac{LLHH}{\Lambda}$ S.Weinberg, PRL43, 1566 (1979)

$$\Lambda \sim (10^{12} - 10^{14}) \text{ GeV}$$

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BTW: good to have the “complete Higgs doublet” :-)
(If you prefer ABEHGHKW you rather read “HIGGS”...)

SM as an effective theory at d=6 level

X^3		φ^6 and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
Q_G	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	Q_φ	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\square}$	$(\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
Q_W	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\widetilde{W}}$	$\varepsilon^{IJK} \widetilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	Q_{eW}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	Q_{eB}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	Q_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \widetilde{W}_{\mu\nu}^I W^{I\mu\nu}$	Q_{uW}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	Q_{uB}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	Q_{dW}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \widetilde{W}_{\mu\nu}^I B^{\mu\nu}$	Q_{dB}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

B. Grzadkowski et al., JHEP 10 (2010) 085, arXiv: 1008.4884

SM as an effective theory at d=6 level

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	Q_{le}	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		B -violating			
Q_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^{\gamma j})^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	Q_{qqu}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \varepsilon_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	Q_{duu}	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		

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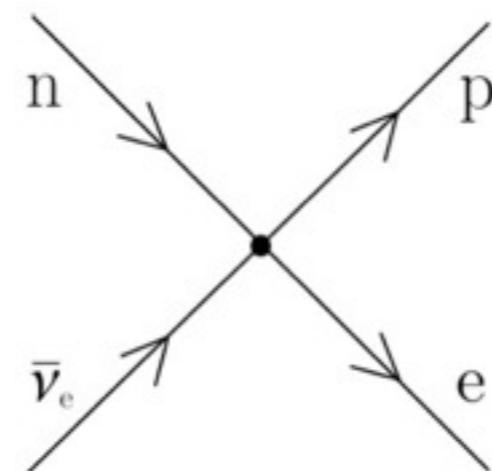
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$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		B-violating			
Q_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^{\gamma j})^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	Q_{qqu}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \varepsilon_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$	Q_{duu}	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		

B. Grzadkowski et al., JHEP 10 (2010) 085, arXiv: 1008.4884

Renormalizable dynamics behind the SM d=6 BNV?

Let's do the same trick that Schwinger & co. played with the Fermi theory:

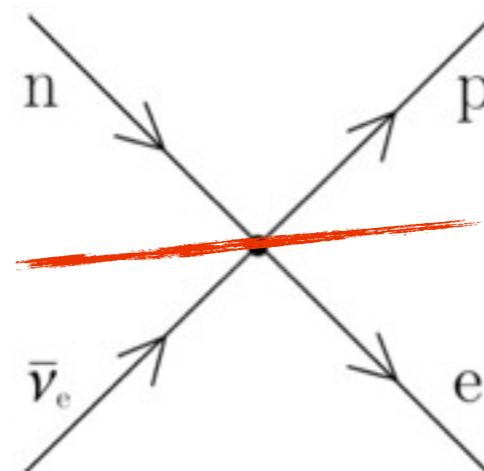
Elementary vertex:



Renormalizable dynamics behind the SM d=6 BNV?

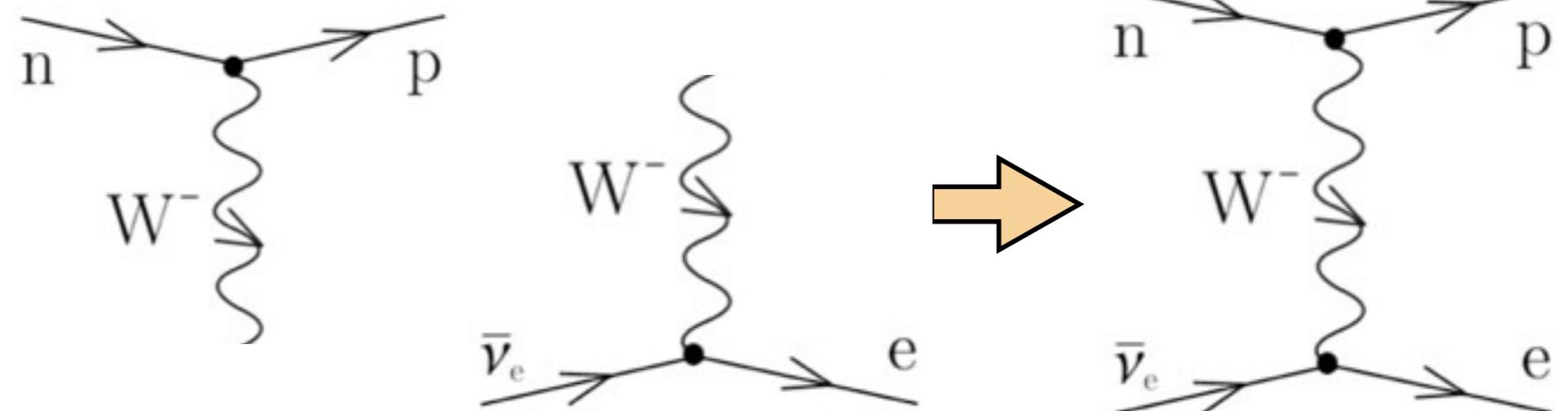
Let's do the same trick that Schwinger & co. played with the Fermi theory:

Elementary vertex:



QED-like seed of
a renormalizable theory

Elementary vertices:



Renormalizable dynamics behind the SM d=6 BNV?

Example: $(d_R^T C u_R)(Q_L^T C L_L)$

Renormalizable dynamics behind the SM d=6 BNV?

Example: $(d_R^T C u_R) / (Q_L^T C L_L)$

Scalar exchange

$$(3, 1, -\frac{1}{3}) \oplus (\bar{3}, 1, +\frac{1}{3})$$



Renormalizable dynamics behind the SM d=6 BNV?

Example: $(d_R^T C u_R) / \cancel{(Q_L^T C L_L)} = [(\overline{u_R})^c \gamma_\mu Q] [(\overline{d_R})^c \gamma_\mu L]$

Fierz
↓
Scalar exchange

$$(3, 1, -\frac{1}{3}) \oplus (\bar{3}, 1, +\frac{1}{3})$$



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Example: $(d_R^T C u_R) \cancel{(Q_L^T C L_L)} = \cancel{[(u_R)^c \gamma_\mu Q]} \cancel{[(d_R)^c \gamma_\mu L]}$

Fierz

Scalar exchange **Vector exchange**

$(3, 1, -\frac{1}{3}) \oplus (\bar{3}, 1, +\frac{1}{3})$ $(3, 2, -\frac{5}{6}) \oplus (\bar{3}, 2, +\frac{5}{6})$

Δ X^μ

Renormalizable dynamics behind the SM d=6 BNV?

Example: $(d_R^T C u_R)(Q_L^T C L_L) \xrightarrow{\text{Fierz}} [(\overline{u}_R)^c \gamma_\mu Q] [(\overline{d}_R)^c \gamma_\mu L]$

Scalar exchange $(3, 1, -\frac{1}{3}) \oplus (\bar{3}, 1, +\frac{1}{3})$

Vector exchange $(3, 2, -\frac{5}{6}) \oplus (\bar{3}, 2, +\frac{5}{6})$

Proton instability:

new Yukawa interactions

$p^+ \left\{ \begin{array}{c} d \\ u \\ u \end{array} \right\} \Delta \rightarrow e^+ + \pi^0 + \left\{ \begin{array}{c} \bar{u} \\ u \end{array} \right\}$

new gauge interaction

$p^+ \left\{ \begin{array}{c} d \\ u \\ u \end{array} \right\} X^\mu \rightarrow e^+ + \pi^0 + \left\{ \begin{array}{c} \bar{u} \\ u \end{array} \right\}$

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new gauge interaction

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Useless without further info on the mediator masses and couplings...

Proton lifetime experimental constraints I

First limits on proton lifetime

1950's - M. Goldhaber

$$\tau(p^+) > 10^{18} y$$



“Tickle in the bones” argument...

NB. Lethal dose about 10^{14-15} MeV/y

First experiments

1954 - F. Reines, C.L. Cowan, M. Goldhaber

Reines, Cowan, Goldhaber, Phys. Rev. 96, 1157 (1954)

Experiment in Savannah River, SC

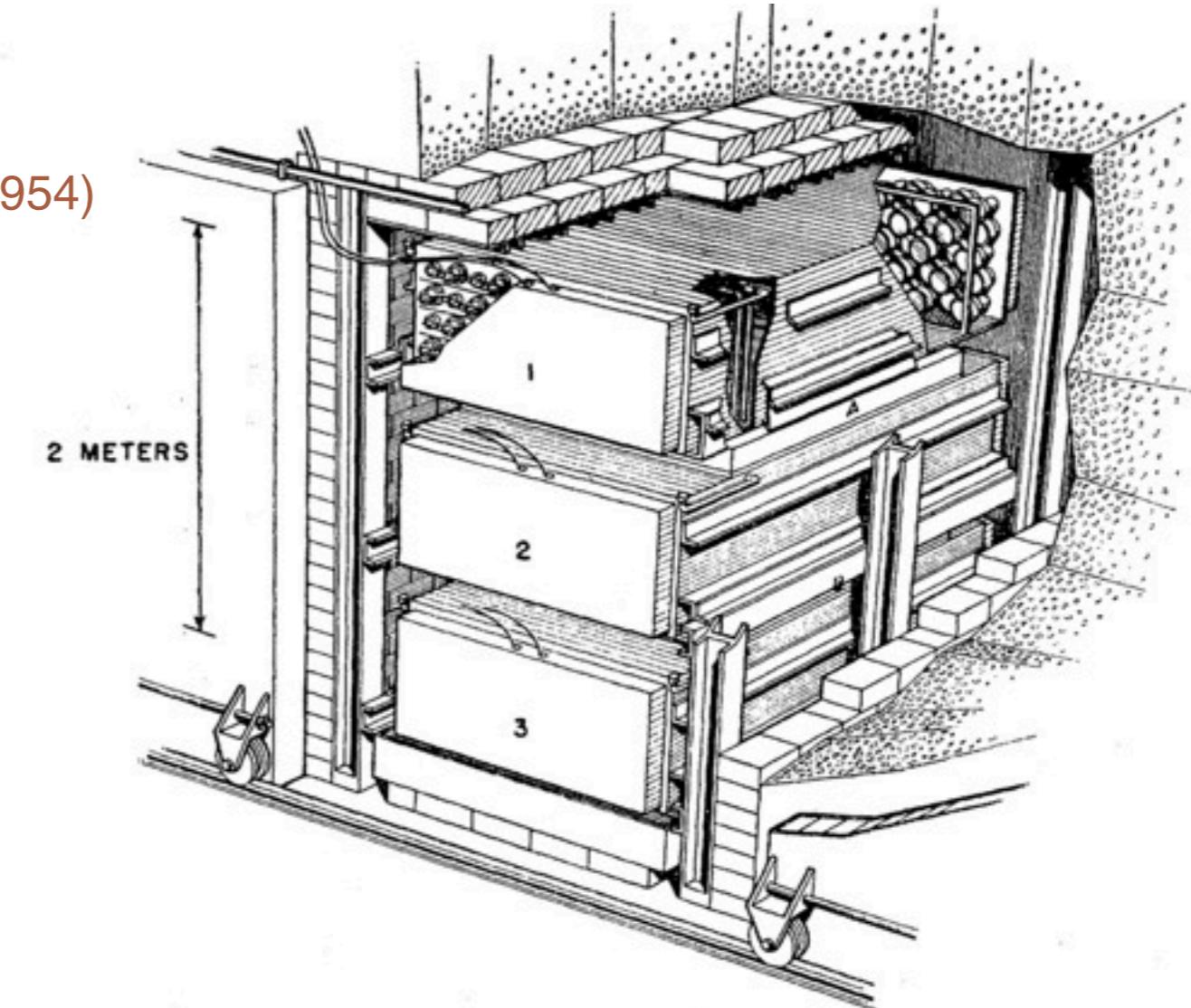


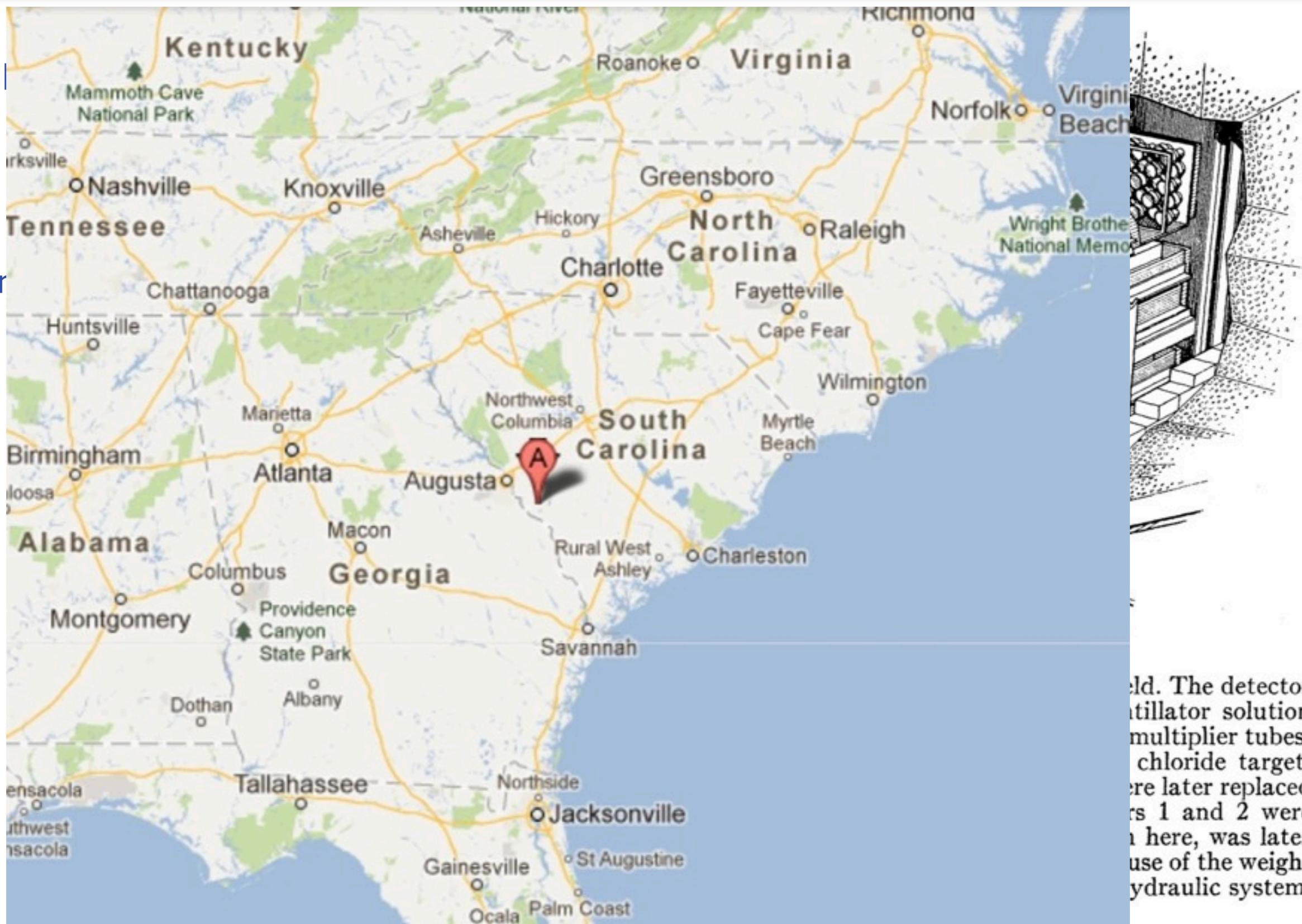
FIG. 2. Sketch of detectors inside their lead shield. The detector tanks marked 1, 2, and 3 contained liquid scintillator solution which was viewed in each tank by 110 5-in. photomultiplier tubes. The white tanks contained the water-cadmium chloride target, and in this picture are some 28 cm deep. These were later replaced by 7.5-cm deep polystyrene tanks, and detectors 1 and 2 were lowered correspondingly. A drip tank, not shown here, was later set underneath tank 3 in the event of a leak. Because of the weight it was necessary to move the lead doors with a hydraulic system.

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- 300 liters of a liquid scintillator
- detecting muons from inside the apparatus
- background about 6 Hz (30 meters)

$$\tau(p^+) > 10^{21} y$$

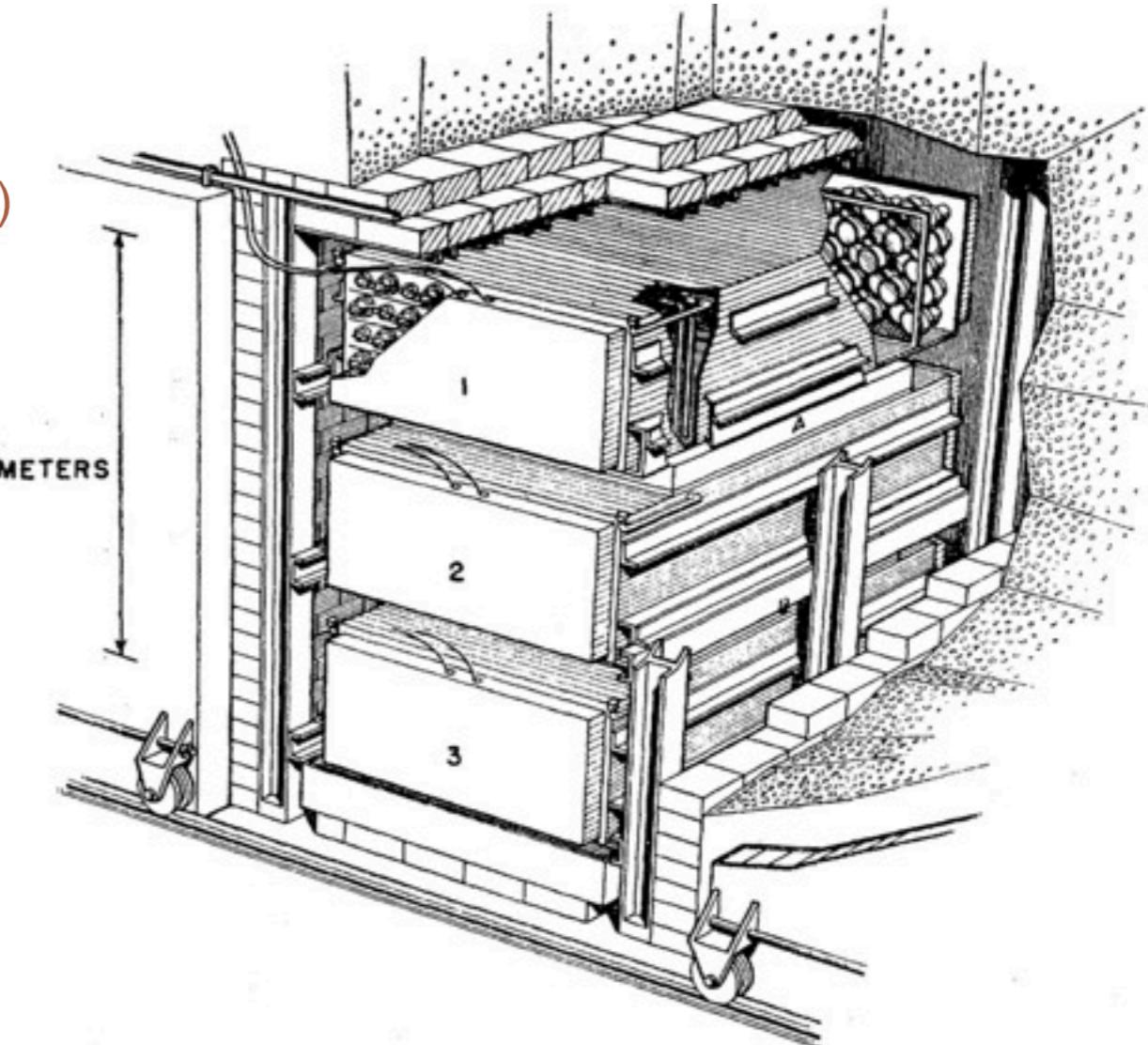


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Neutrino discovery 1956 !

C.L. Cowan, F. Reines, F. B. Harrison, H.W. Kruse,
A.D. McGuire, Science 124 (1956) 103-104

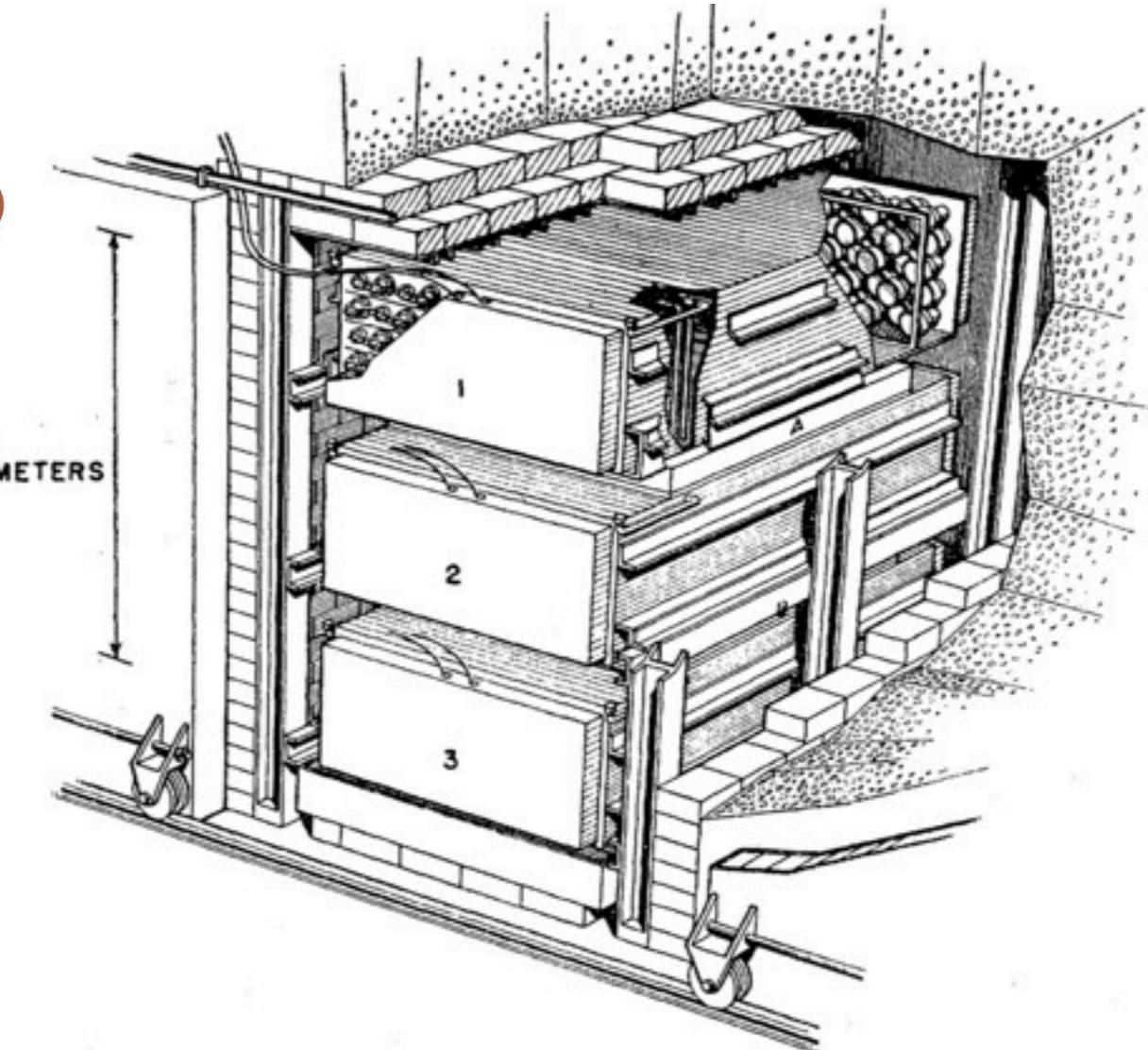


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1974 - F. Reines, M. Crouch et al.

F. Reines, M. Crouch, PRL 32, 493 (1974)

Case Western Reserve University - University of Witwatersrand - University
of California at Irvine deep under ground neutrino program



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3200 m deep!!!

muon background
under control

First experiments

F. Reines, M. Crouch, PRL 32, 493 (1974)

F. Reines et al., PRD 4, 80 (1971)

1974 - F. Reines, M. Crouch et al.

- primarily a detector of atmospheric neutrinos

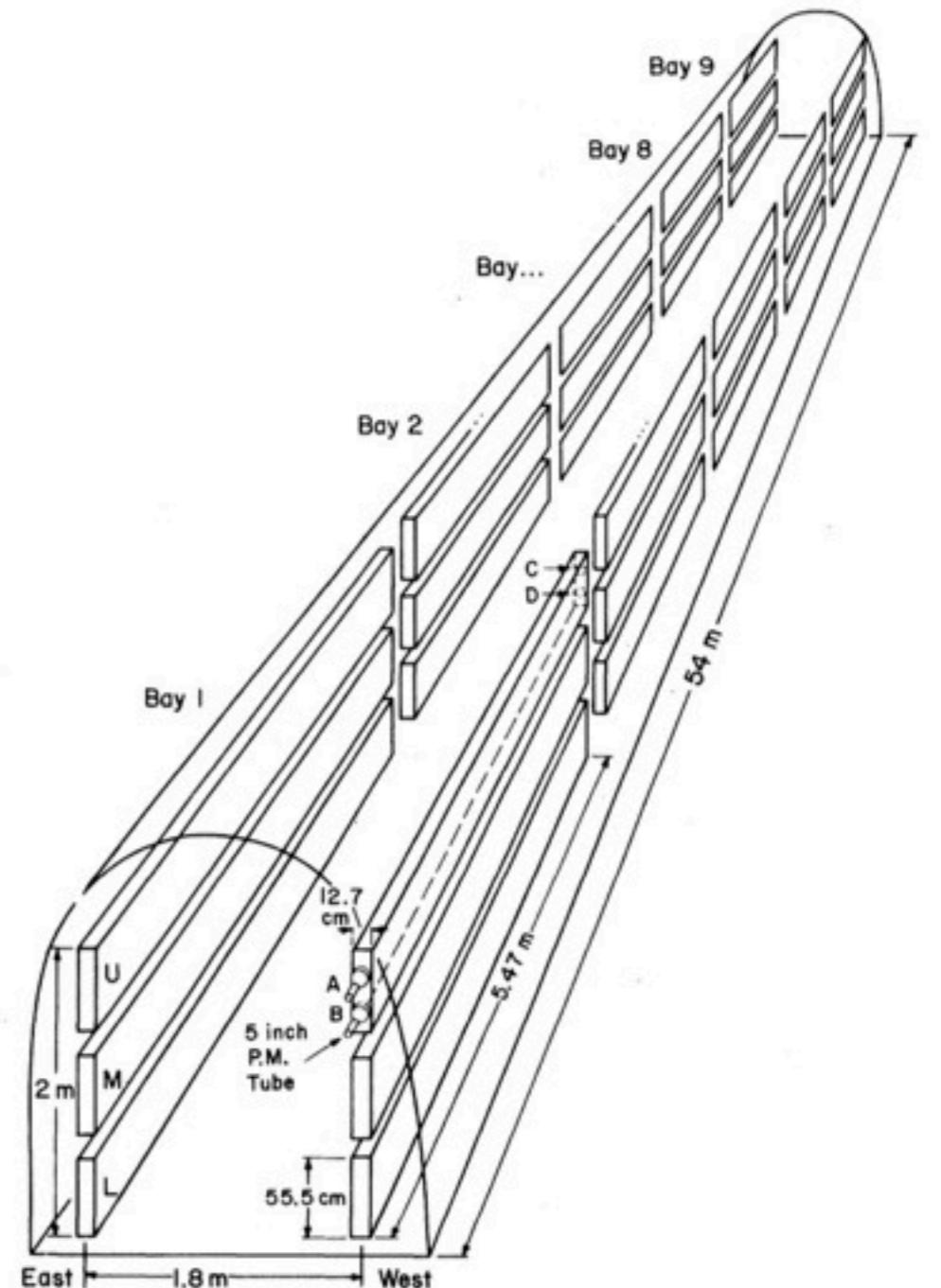


FIG. 1. Sketch of the detector array. Approximate array and element dimensions are given.

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- p-decay signal = horizontal muon events

- exp. from atmospheric neutrinos: few/year

- atmospheric muon background suppressed: 10^{-9}

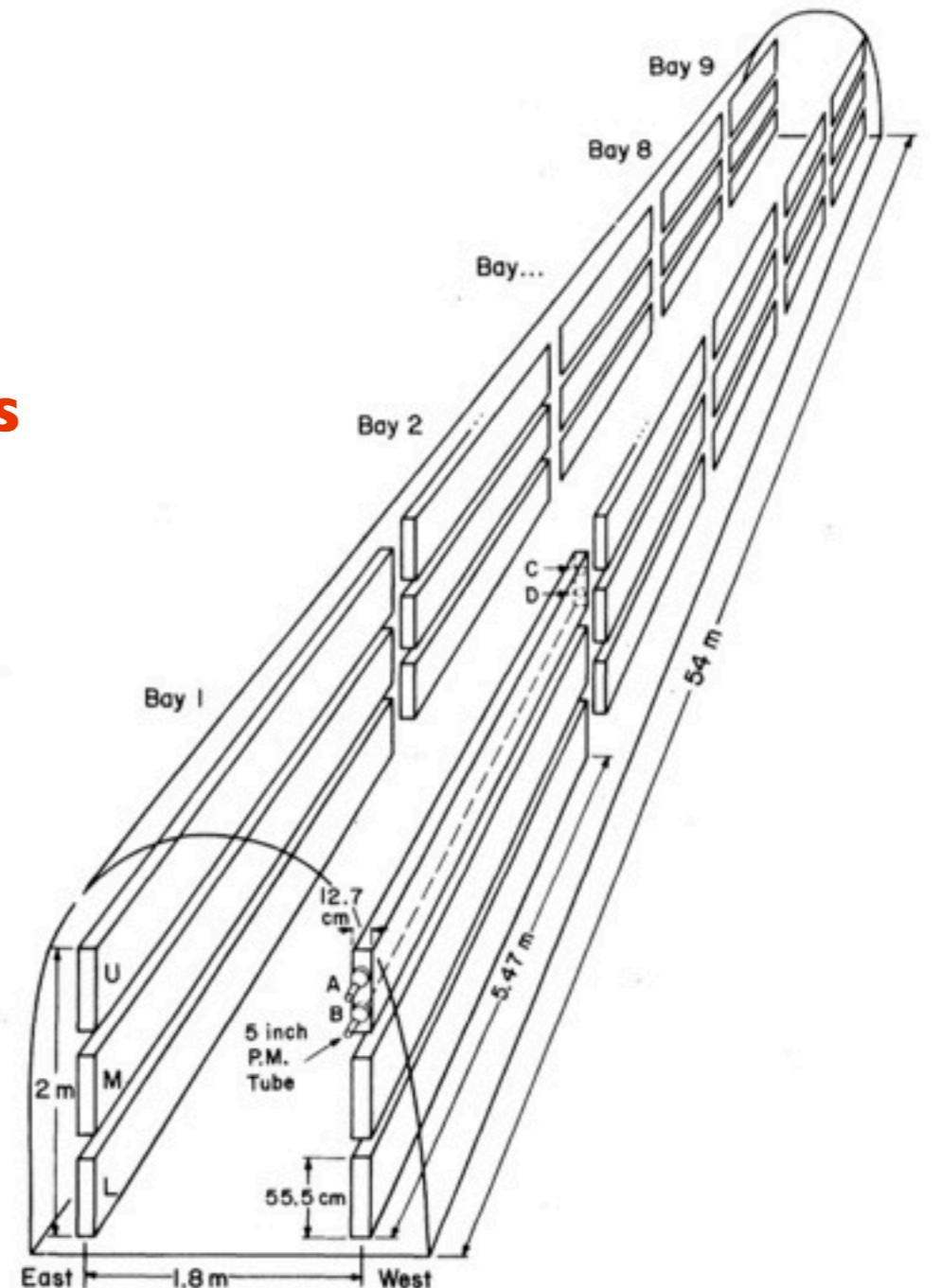


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- primarily a detector of atmospheric neutrinos

- **p-decay signal = horizontal muon events**

- exp. from atmospheric neutrinos: few/year

- atmospheric muon background suppressed: 10^{-9}

- compatibility with purely neutrino events:

$$\tau_p \gtrsim 10^{30} \text{ yr}$$

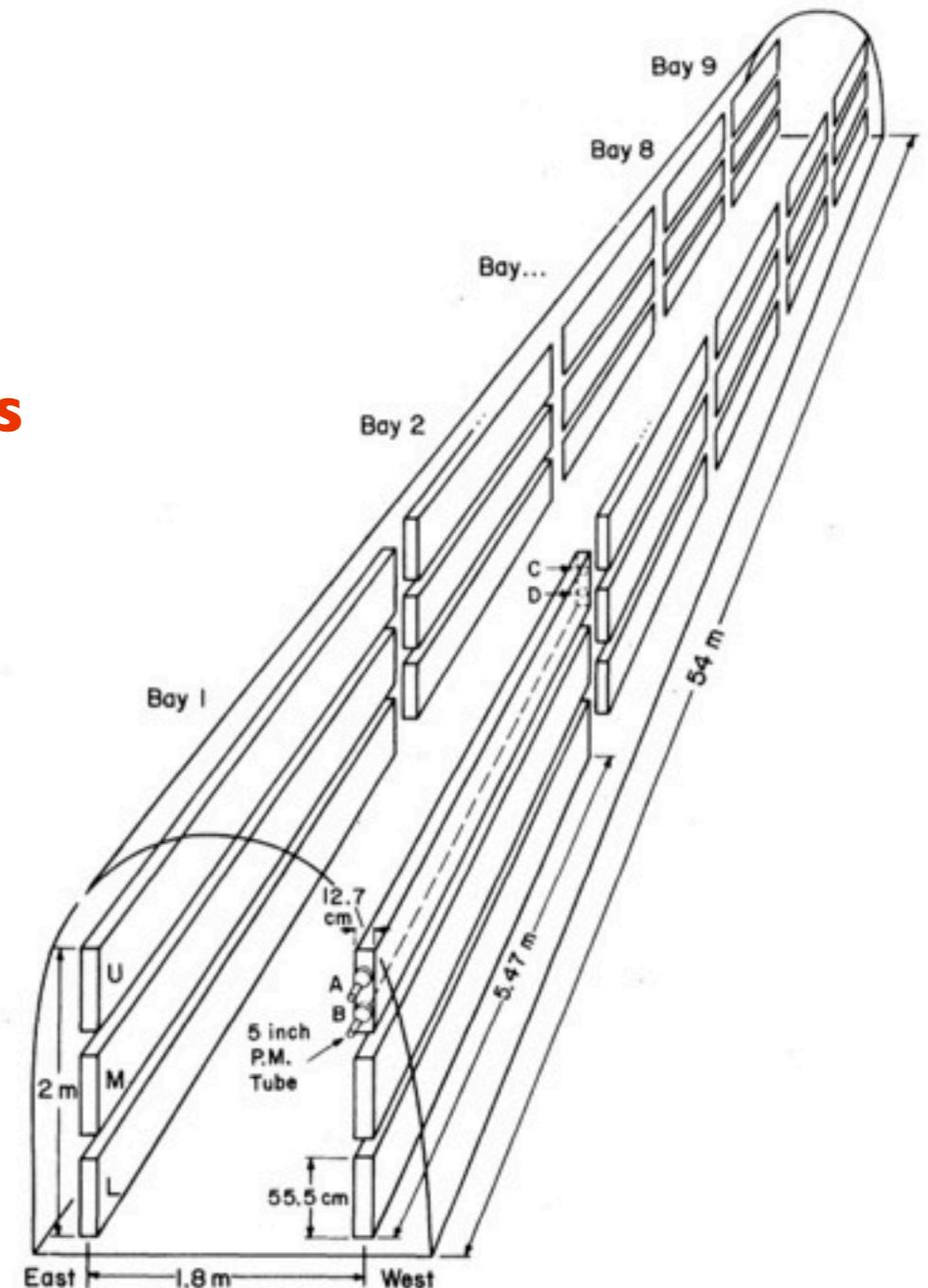


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|974

The minimal SU(5) GUT

VOLUME 32, NUMBER 8

PHYSICAL REVIEW LETTERS

25 FEBRUARY 1974

Unity of All Elementary-Particle Forces

Howard Georgi* and S. L. Glashow

Lyman Laboratory of Physics, Harvard University, Cambridge, Massachusetts 02138

(Received 10 January 1974)

Strong, electromagnetic, and weak forces are conjectured to arise from a single fundamental interaction based on the gauge group SU(5).

We present a series of hypotheses and speculations leading inescapably to the conclusion that SU(5) is the gauge group of the world—that all elementary particle forces (strong, weak, and electromagnetic) are different manifestations of the same fundamental interaction involving a single coupling strength, the fine-structure constant. Our hypotheses may be wrong and our speculations idle, but the uniqueness and simplicity of our scheme are reasons enough that it be taken seriously.

of the GIM mechanism with the notion of colored quarks⁴ keeps the successes of the quark model and gives an important bonus: Lepton and hadron anomalies cancel so that the theory of weak and electromagnetic interactions is renormalizable.⁵

The next step is to include strong interactions. We assume that *strong interactions are mediated by an octet of neutral vector gauge gluons* associated with local color SU(3) symmetry, and that there are no fundamental strongly interacting scalar-meson fields.⁶ This insures that

Uniqueness of SU(5) @ rank=4

The minimal SU(5) GUT

H.Georgi, S.Glashow, Phys.Rev.Lett. 30 (1974)

The minimal SU(5) GUT

H.Georgi, S.Glashow, Phys.Rev.Lett. 30 (1974)

$$SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$$

$$(1, 2, -\frac{1}{2}) \quad \begin{pmatrix} \nu_e \\ e \end{pmatrix} \quad \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}$$
$$(1, 1, +1) \quad e^c \quad \mu^c$$

$$(3, 2, +\frac{1}{6}) \quad \begin{pmatrix} u \\ d \end{pmatrix} \quad \begin{pmatrix} c \\ s \end{pmatrix}$$
$$(\bar{3}, 1, -\frac{2}{3}) \quad u^c \quad c^c$$
$$(\bar{3}, 1, +\frac{1}{3}) \quad d^c \quad s^c$$

The minimal SU(5) GUT

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$$SU(5)$$

$$(1, 2, -\frac{1}{2}) \quad \begin{pmatrix} \nu_e \\ e \end{pmatrix} \quad \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}$$

$$(1, 1, +1) \quad e^c \quad \mu^c$$

$$\bar{5}$$

$$\begin{pmatrix} d_1^c \\ d_2^c \\ d_3^c \\ -e \\ \nu_e \end{pmatrix}$$

$$\begin{pmatrix} s_1^c \\ s_2^c \\ s_3^c \\ -\mu \\ \nu_\mu \end{pmatrix}$$

$$(3, 2, +\frac{1}{6}) \quad \begin{pmatrix} u \\ d \end{pmatrix} \quad \begin{pmatrix} c \\ s \end{pmatrix}$$

$$(\bar{3}, 1, -\frac{2}{3}) \quad u^c \quad c^c$$

$$(\bar{3}, 1, +\frac{1}{3}) \quad d^c \quad s^c$$

$$10$$

$$\begin{pmatrix} 0 & u_3^c & -u_2^c & u^1 & d^1 \\ . & 0 & u_1^c & u^2 & d^2 \\ . & . & 0 & u^3 & d^3 \\ . & . & . & 0 & e^c \\ . & . & . & . & 0 \end{pmatrix} \begin{pmatrix} 0 & c_3^c & -c_2^c & c^1 & s^1 \\ . & 0 & c_1^c & c^2 & s^2 \\ . & . & 0 & c^3 & s^3 \\ . & . & . & 0 & \mu^c \\ . & . & . & . & 0 \end{pmatrix}$$

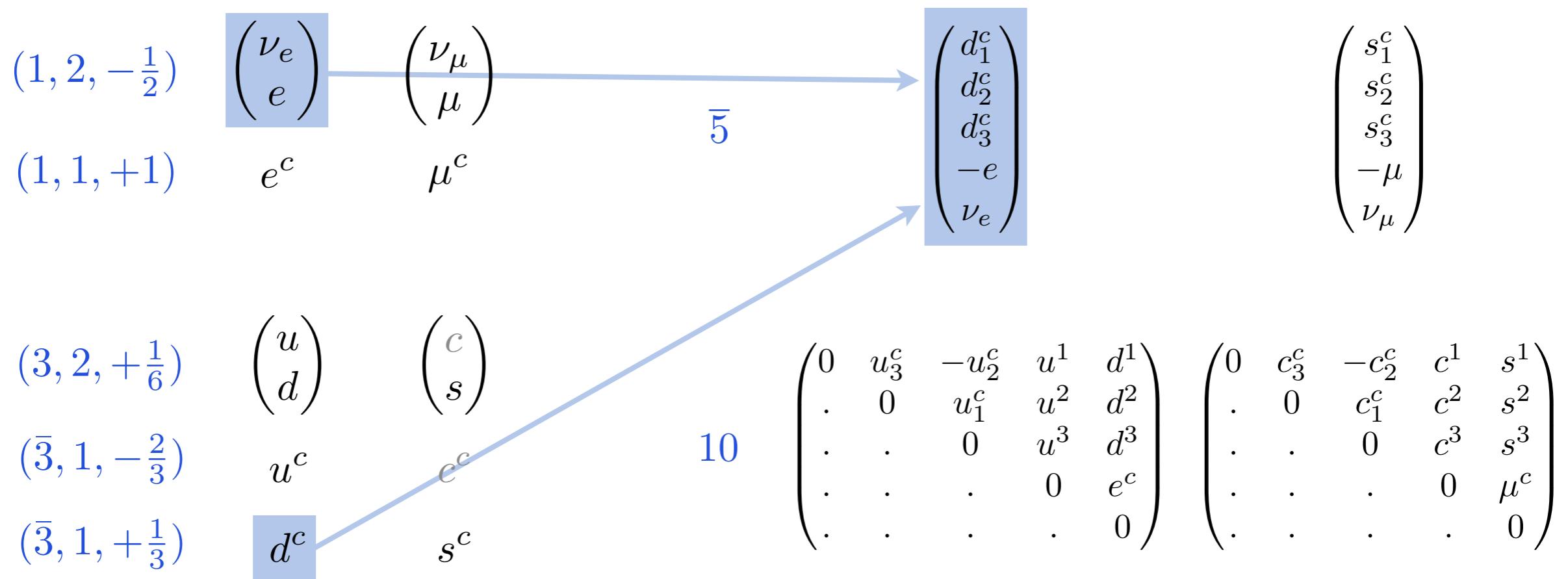
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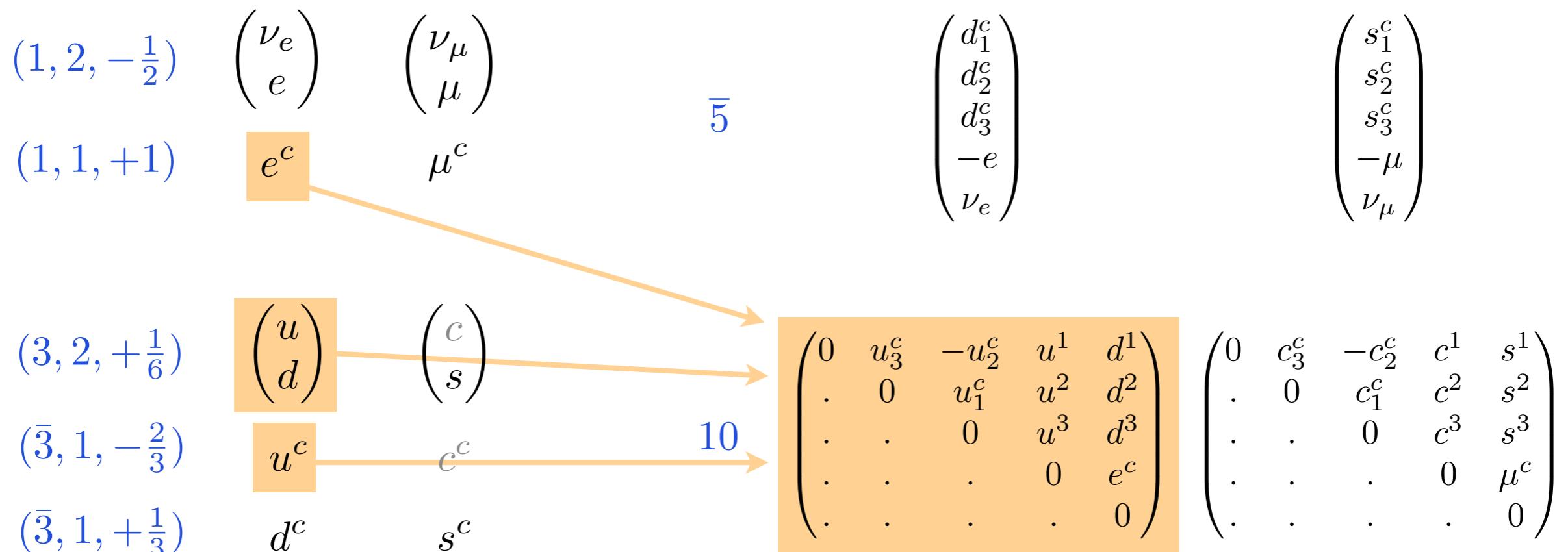
$$SU(5)$$



The minimal SU(5) GUT

H.Georgi, S.Glashow, Phys.Rev.Lett. 30 (1974)

$$SU(3)_c \otimes SU(2)_L \otimes U(1)_Y \longrightarrow SU(5)$$



The minimal SU(5) GUT

Gauge sector:

$$24 = (8, 1, 0) \oplus (1, 3, 0) \oplus (1, 1, 0) \oplus (3, 2, -\frac{5}{6}) \oplus (\bar{3}, 2, +\frac{5}{6})$$

$$\left. \begin{array}{c} G^\mu \\ A^\mu \\ B^\mu \end{array} \right\} W^\pm, Z, \gamma \quad G^\mu \quad A^\mu \quad B^\mu \quad X^\mu$$

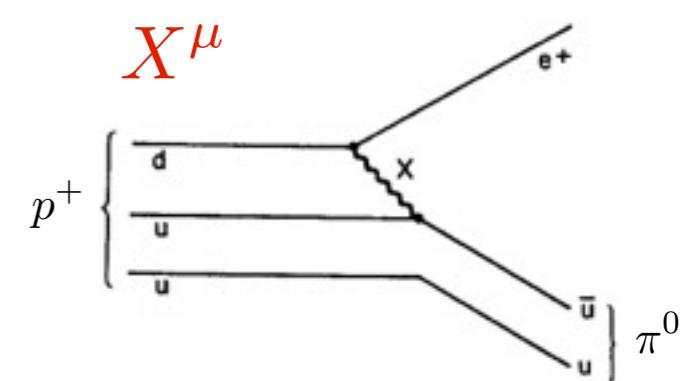
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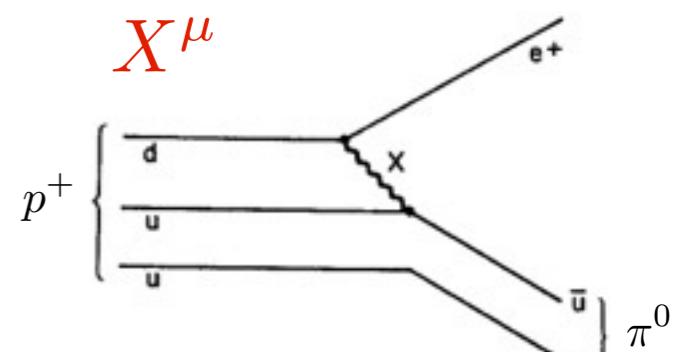
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Scalar sector:

$$SU(3)_c \otimes SU(2)_L \otimes U(1)_Y \rightarrow SU(3)_c \otimes U(1)_Q$$

SM Higgs:

$$\bar{5} = (1, \bar{2}, +\frac{1}{2}) \oplus (\bar{3}, 1, -\frac{1}{3})$$

$$H \quad \Delta$$

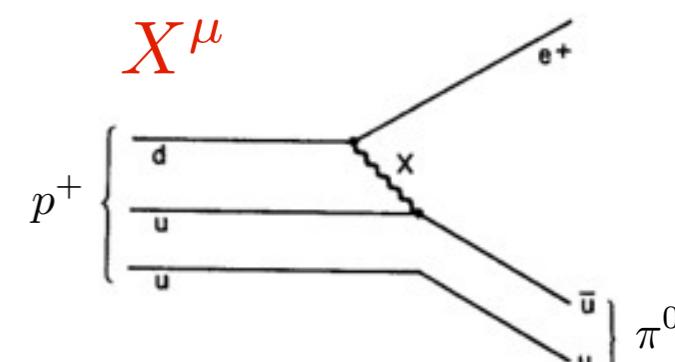
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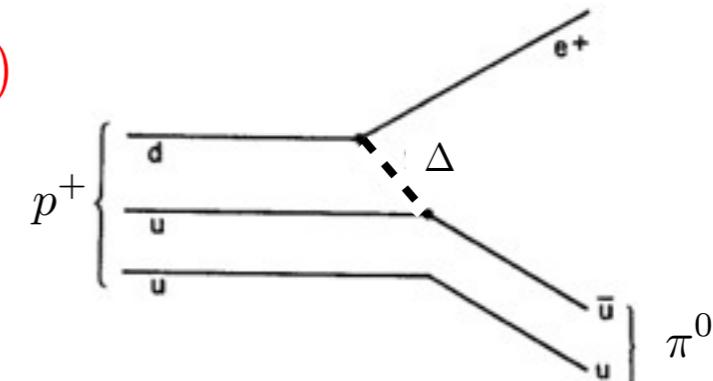
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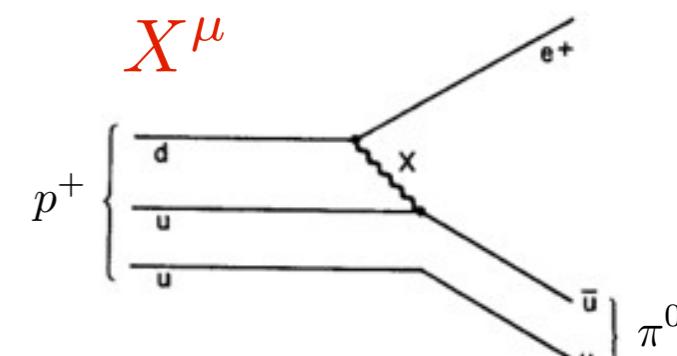
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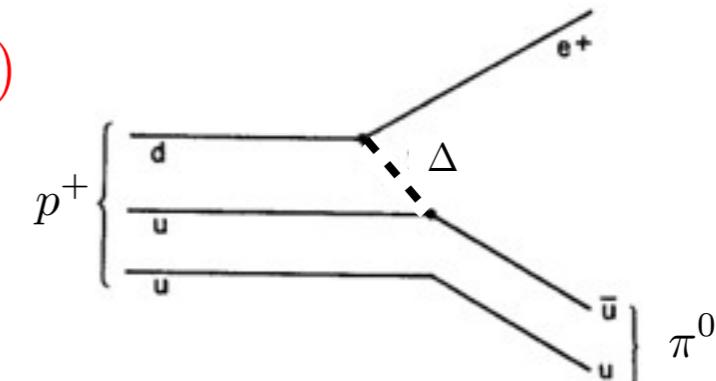
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$$H$$

$$\Delta$$



GUT-breaking scalars:

$$SU(5) \rightarrow SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$$

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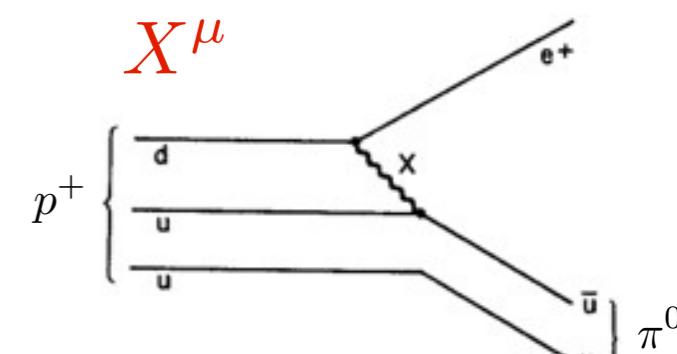
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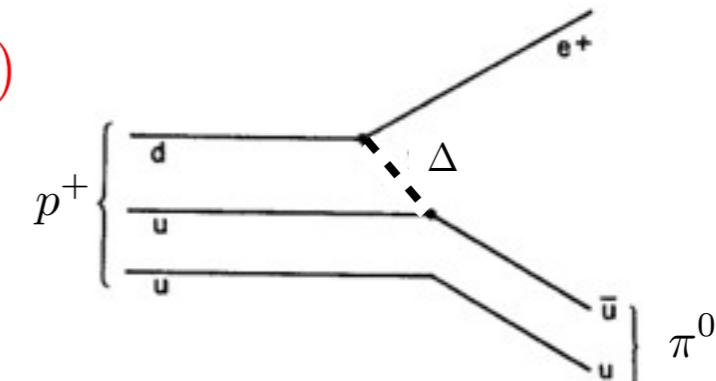
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Pure group theory, no dynamical picture yet...

SM running gauge couplings

SM running couplings

Running gauge couplings in the SM:

Gross, Wilczek, Politzer 1973

Georgi, Quinn, Weinberg 1974

$$\mu \frac{d}{d\mu} g = \beta(g, \dots)$$

calculable in perturbation theory

$$\beta = \frac{g^3}{16\pi^2} \left(-\frac{11}{3} C_2(G) + \frac{2}{3} \sum_{f_W} T_2^G(R_{f_W}) + \frac{1}{3} \sum_{s_C} T_2^G(R_{s_C}) \right) + \dots$$

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b

Better coordinates:

$$\alpha_i \equiv \frac{g_i^2}{4\pi} \quad t = \frac{1}{2\pi} \log \frac{\mu}{M_Z}$$

$$\boxed{\frac{d}{dt} \alpha_i^{-1} = -b_i}$$

first order linear differential
equation with constant coefficients
(at the leading order)

SM running couplings

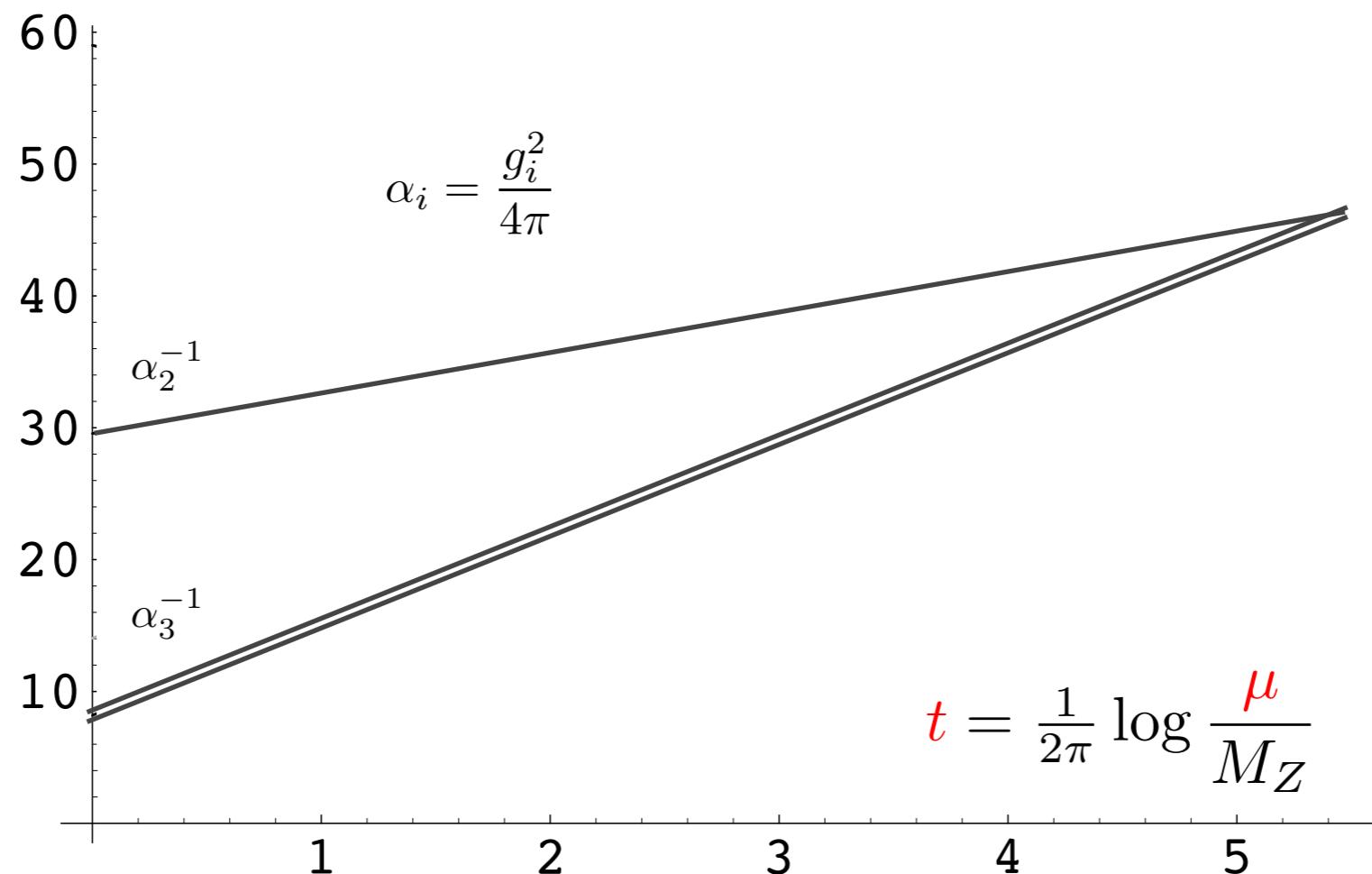
Running gauge couplings in the SM

$$\begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix} = -\frac{11}{3} \begin{pmatrix} 0 \\ 2 \\ 3 \end{pmatrix}_{gauge} + 2 \begin{pmatrix} \frac{10}{3} \\ 2 \\ 2 \end{pmatrix}_{ferm.} + \frac{1}{3} \begin{pmatrix} \frac{1}{2} \\ \frac{1}{2} \\ 0 \end{pmatrix}_{scal.}$$

SM running couplings

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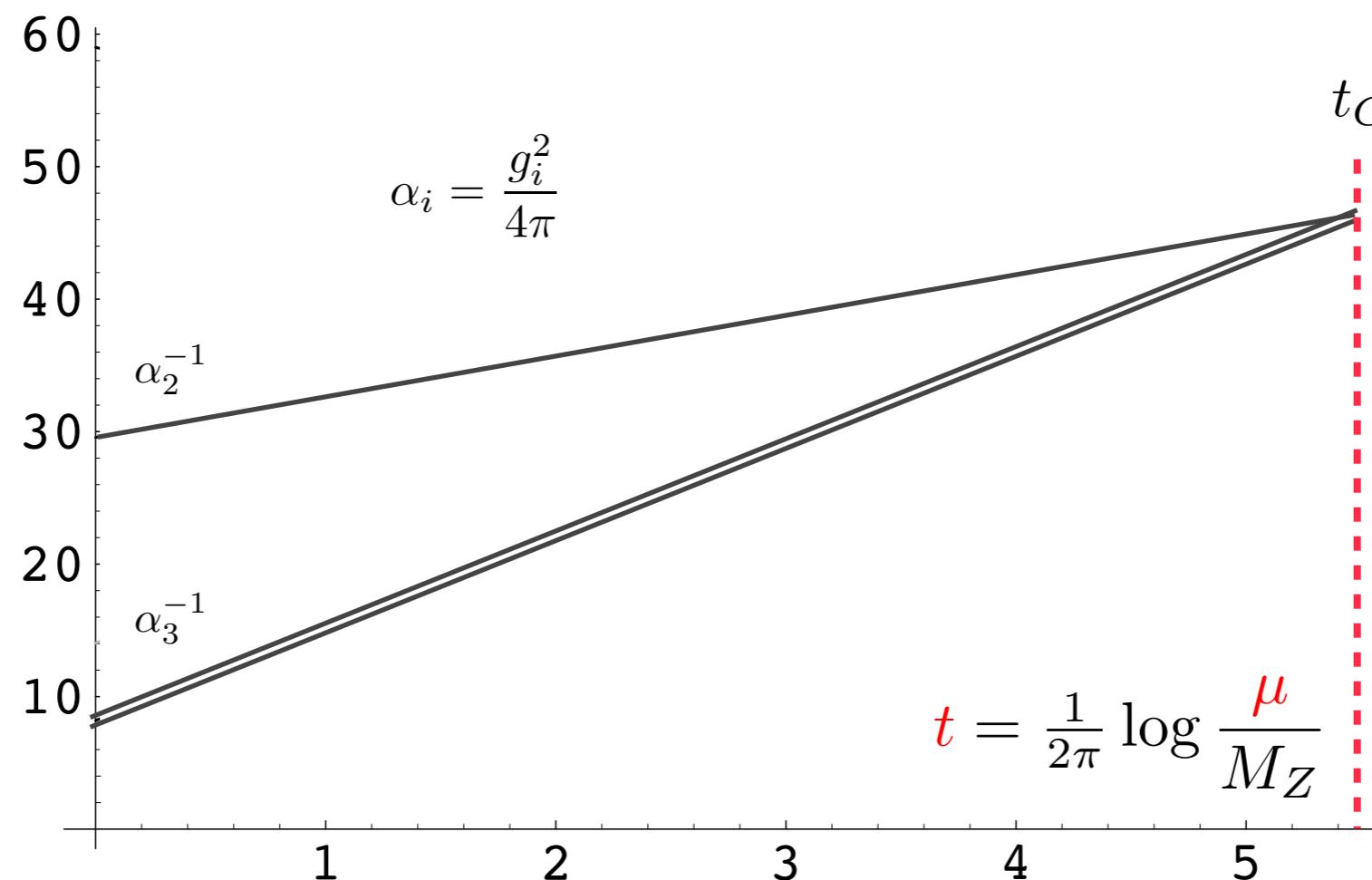
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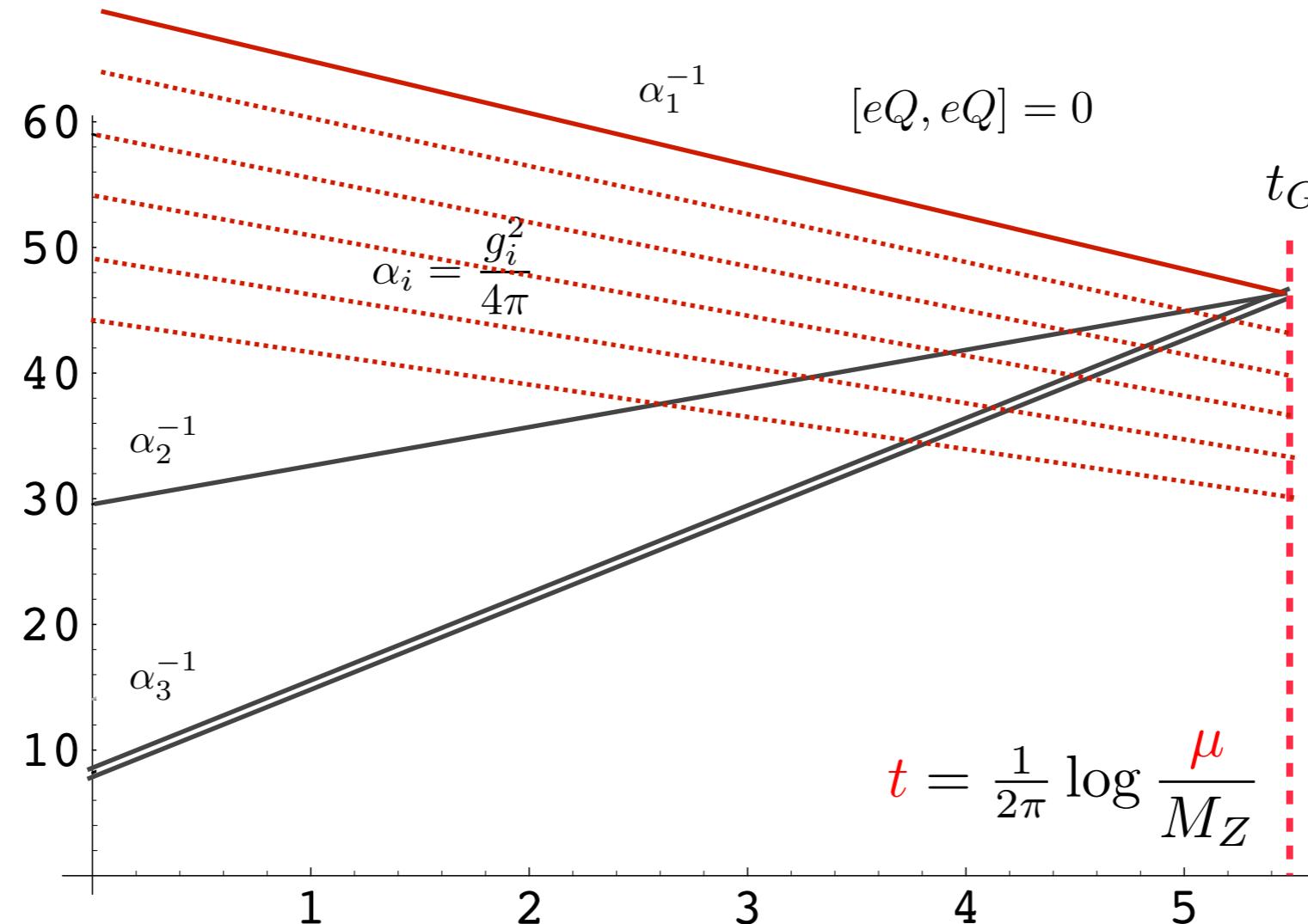
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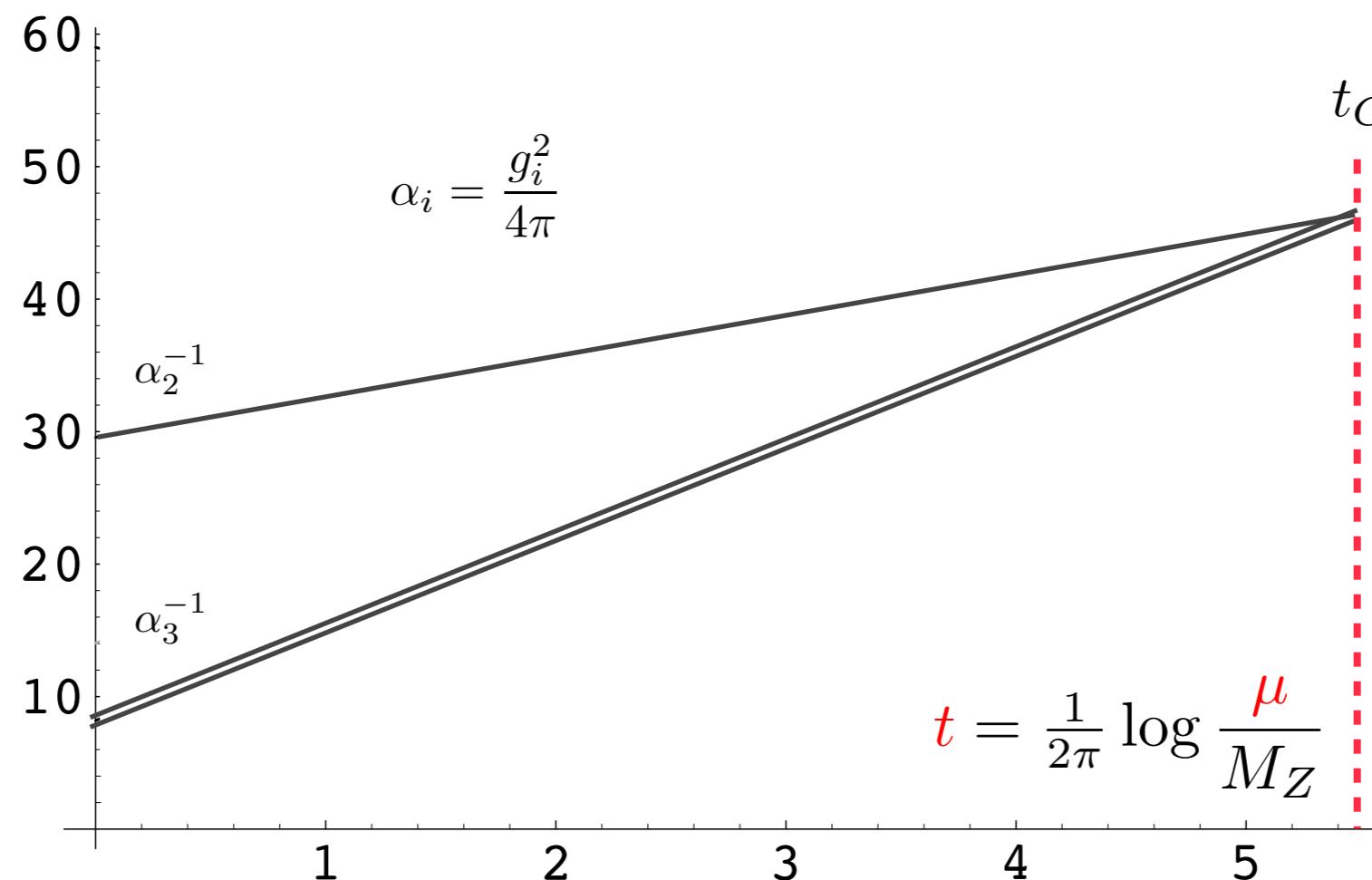
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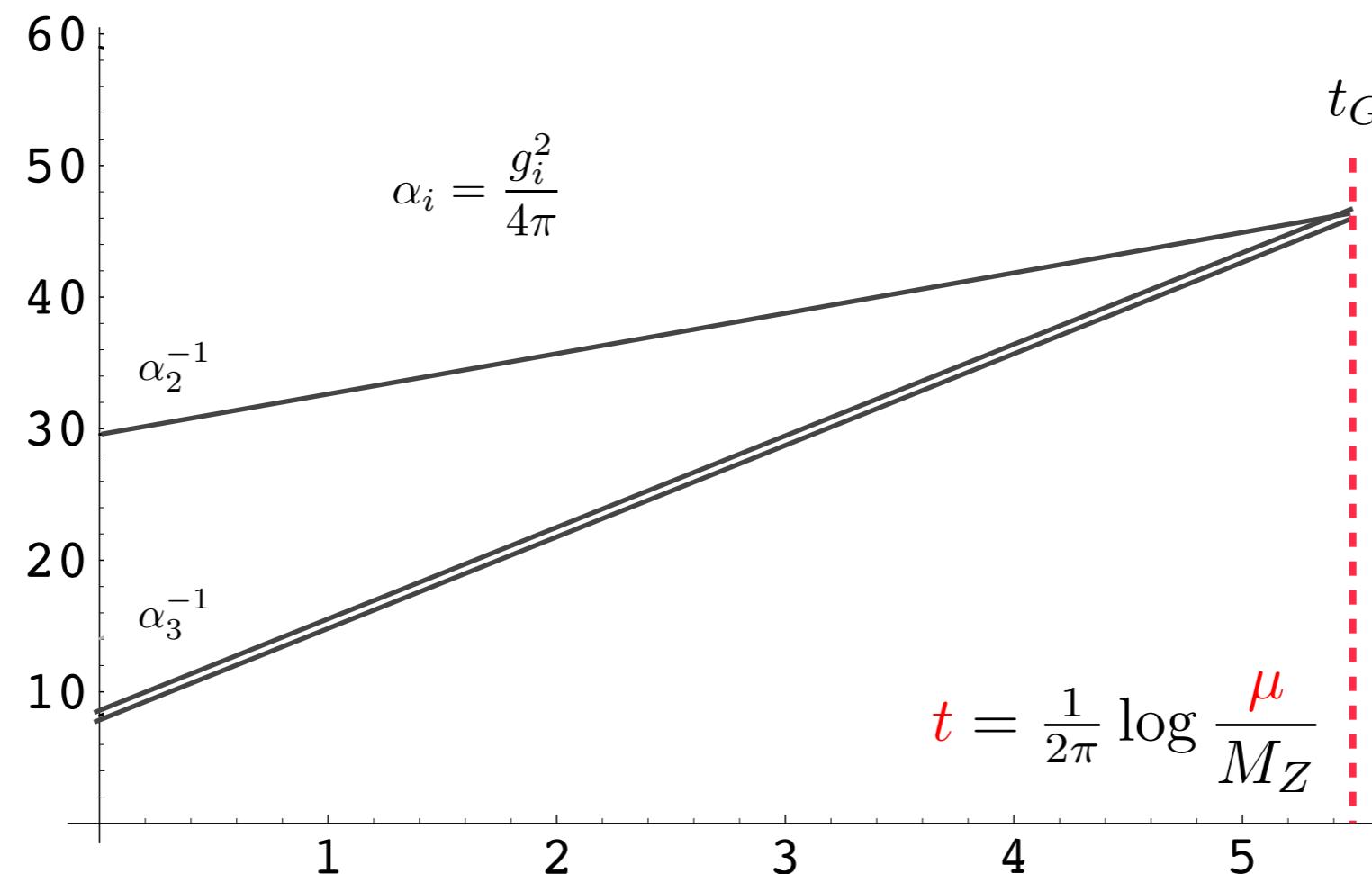


SM running couplings

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d=6 BNV mediators

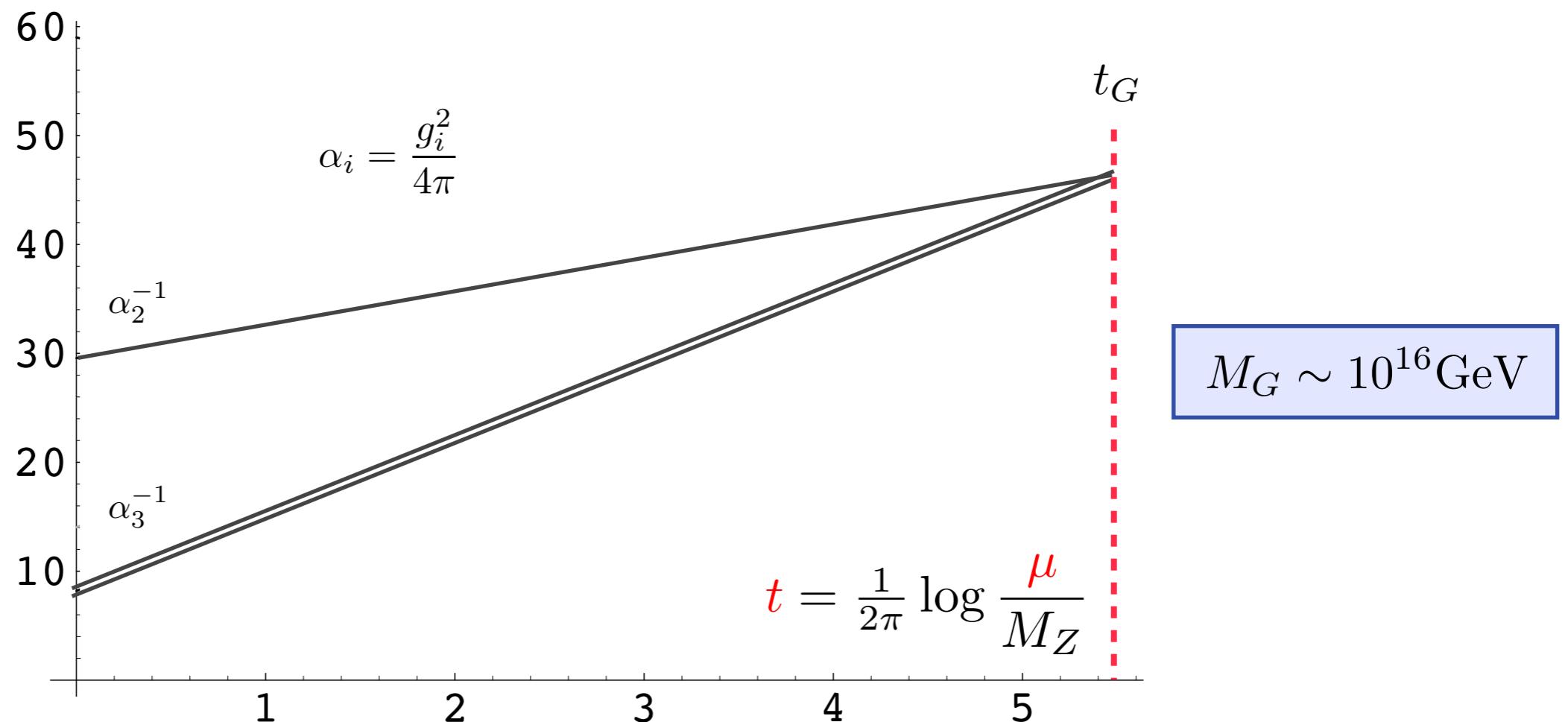


SM running couplings

Running gauge couplings in the SM + $X + \Delta$ d=6 BNV mediators

$$\begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix} = -\frac{11}{3} \begin{pmatrix} 0+\frac{25}{3} \\ 2+3 \\ 3+2 \end{pmatrix}_{gauge} + 2 \begin{pmatrix} \frac{10}{3} \\ 2 \\ 2 \end{pmatrix}_{ferm.} + \frac{1}{3} \begin{pmatrix} \frac{1}{2}+\frac{1}{3} \\ \frac{1}{2} \\ 0+\frac{1}{2} \end{pmatrix}_{scal.}$$

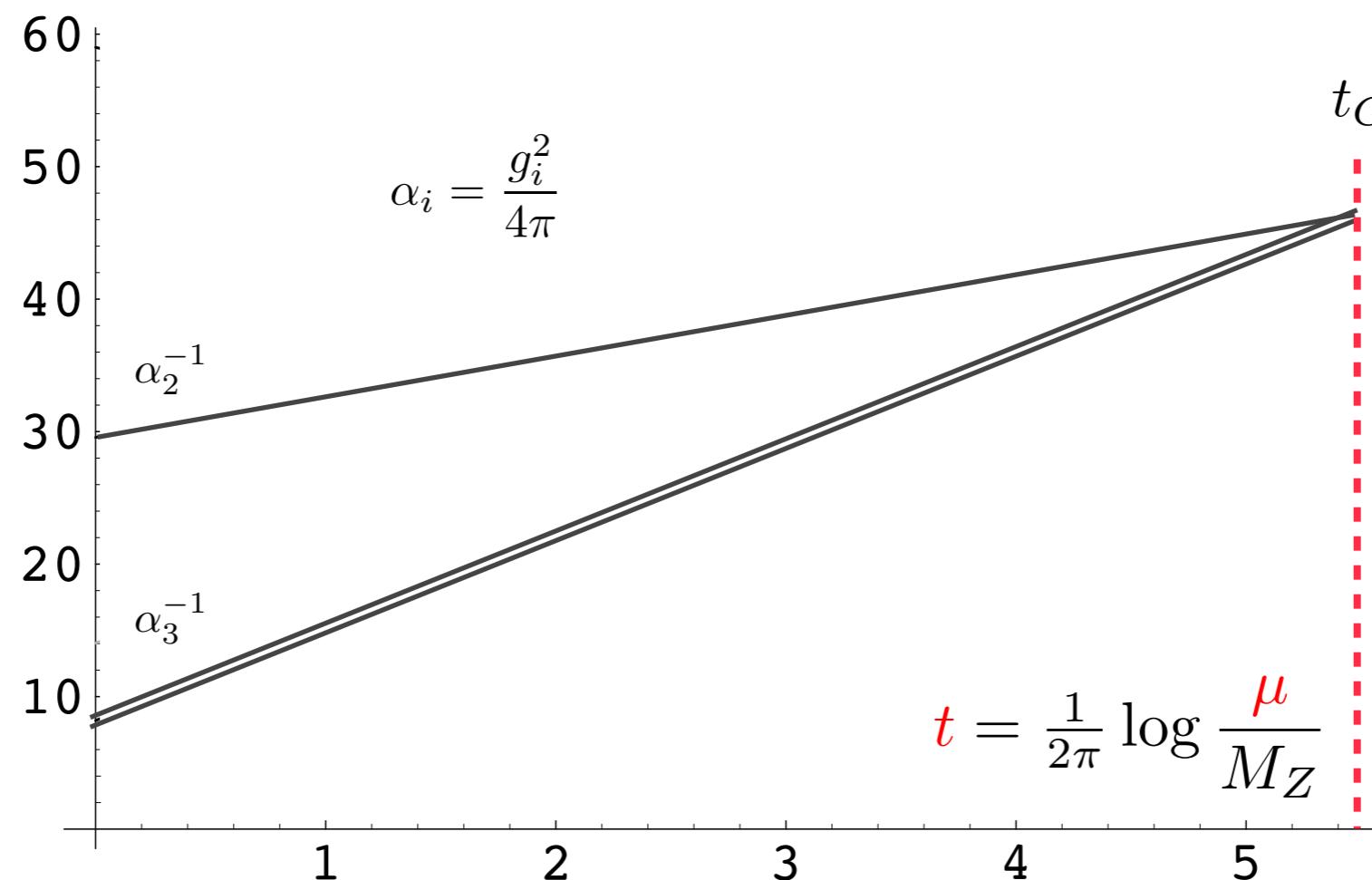
$$(3, 2, -\frac{5}{6}) \oplus h.c. \quad (3, 1, -\frac{1}{3})$$



SM running couplings

Running gauge couplings in the SM $+ X + \Delta$ d=6 BNV mediators

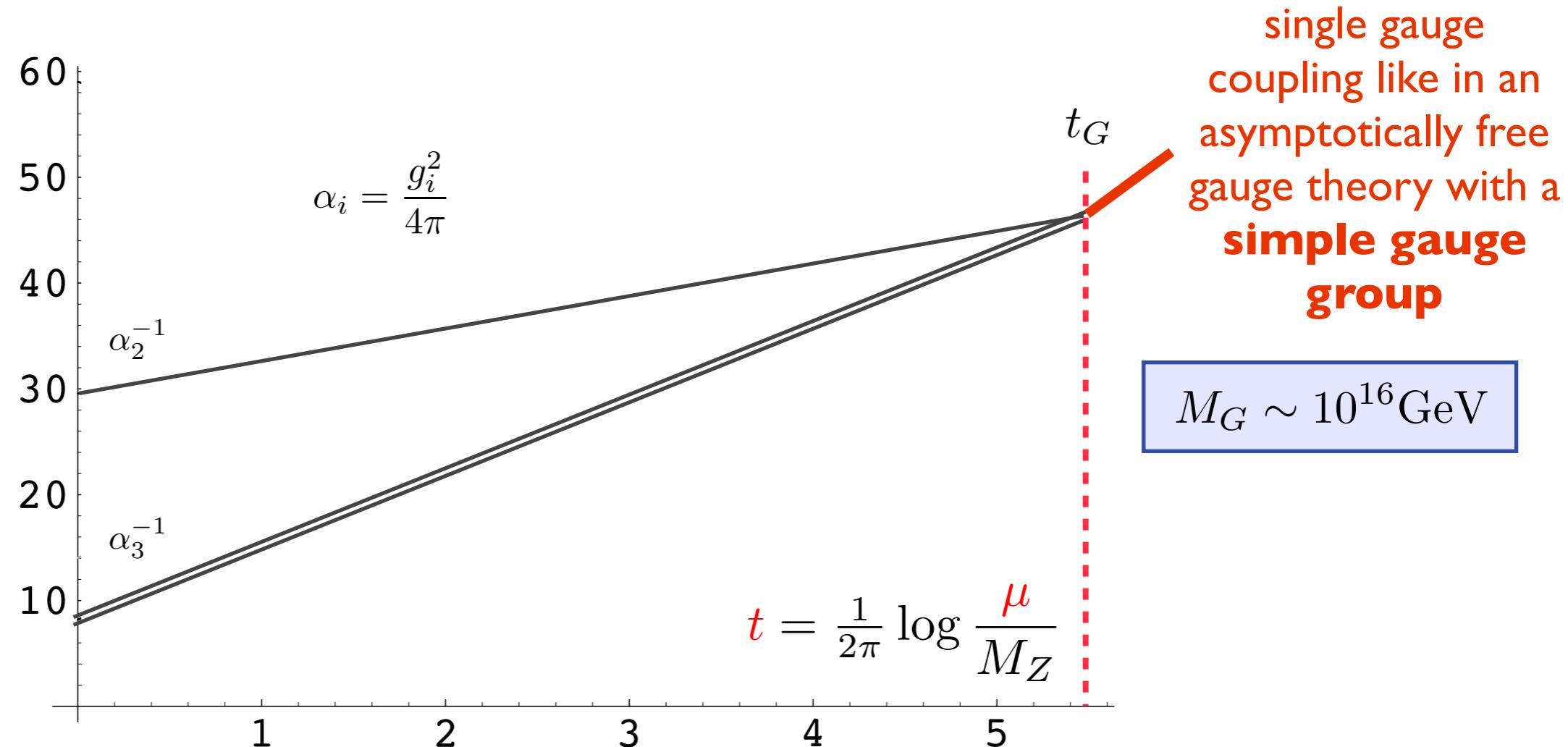
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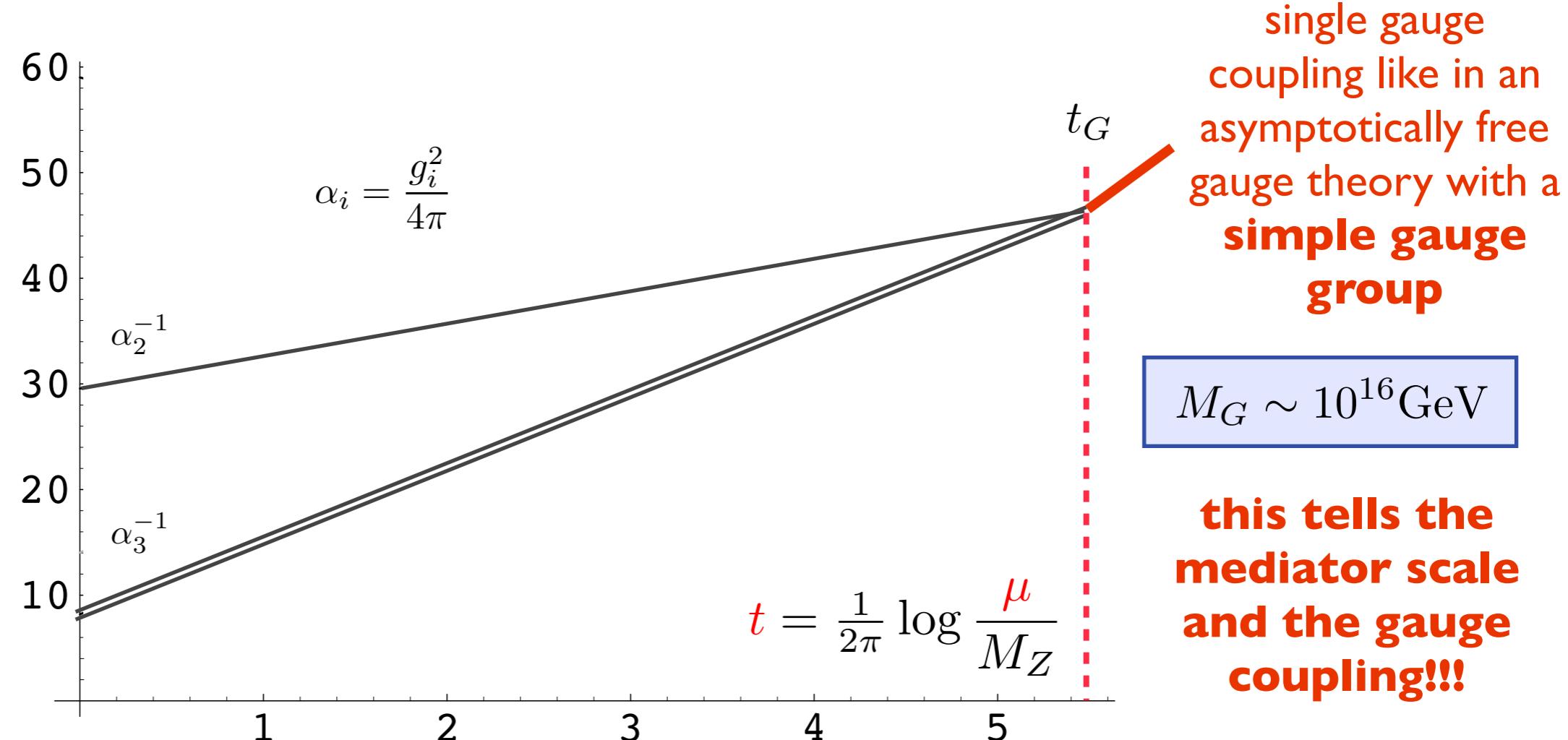
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Proton lifetime experimental constraints II

Proton decay searches II

The proximity of the GQW result and the Reines, Crouch et al. limit:

$$\Gamma_p \sim \frac{m_p^5}{M^4} \lesssim (10^{30} \text{y})^{-1} \quad \text{corresponds to } M \sim 10^{15} \text{ GeV !!!}$$

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This triggered a proton decay rush!



ASCENDING CHILCOOT PASS, MAY, 1898.

rush for a large WC



ASCENDING CHILCOOT PASS, MAY, 1898.

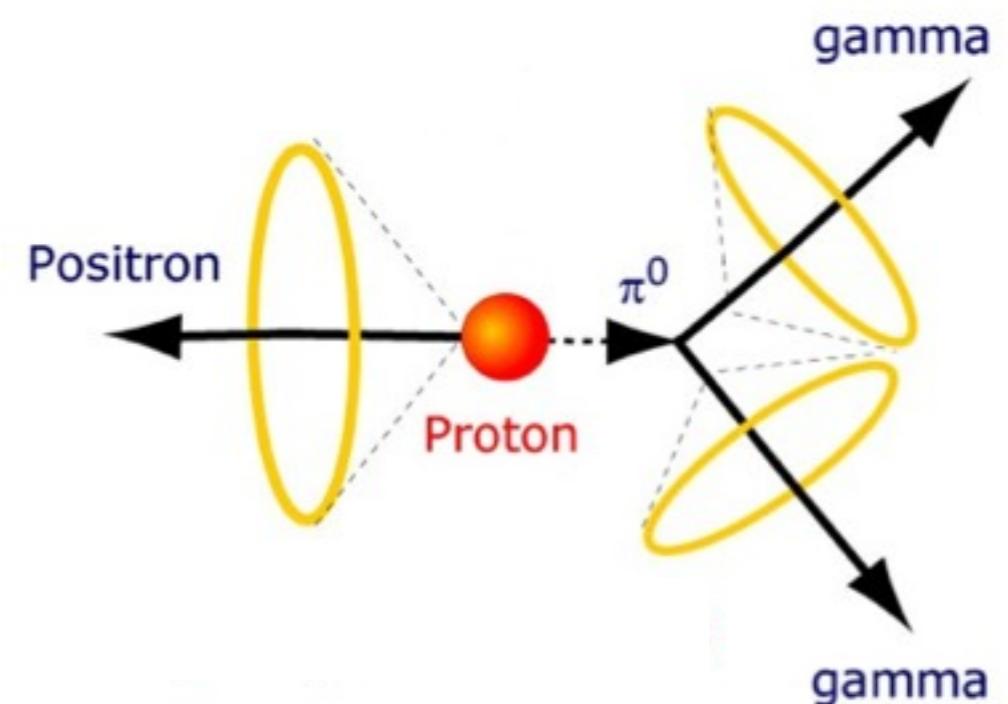


**rush for a large WC
detector**

ASCENDING CHILCOOT PASS, MAY, 1898.

Proton decay in water

“Golden channel”: $p \rightarrow \pi^0 e^+$ $p_\pi = p_e = 459 \text{ MeV}$
 $\pi^0 \rightarrow 2\gamma$ $p_\gamma / p_{\pi(\text{rest})} = 68 \text{ MeV}$

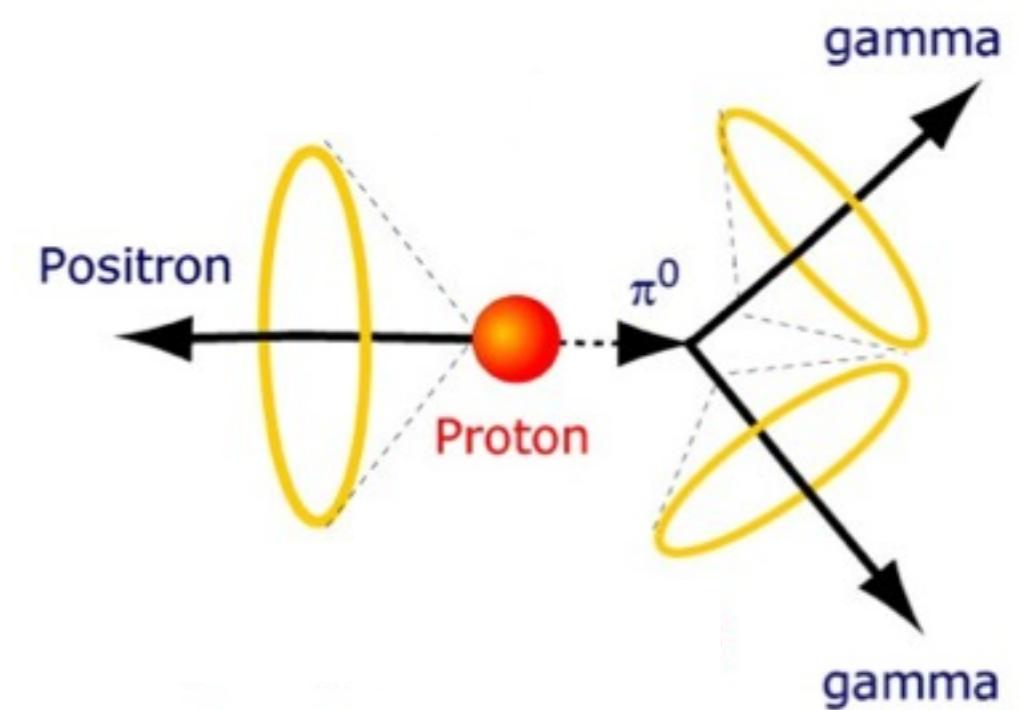
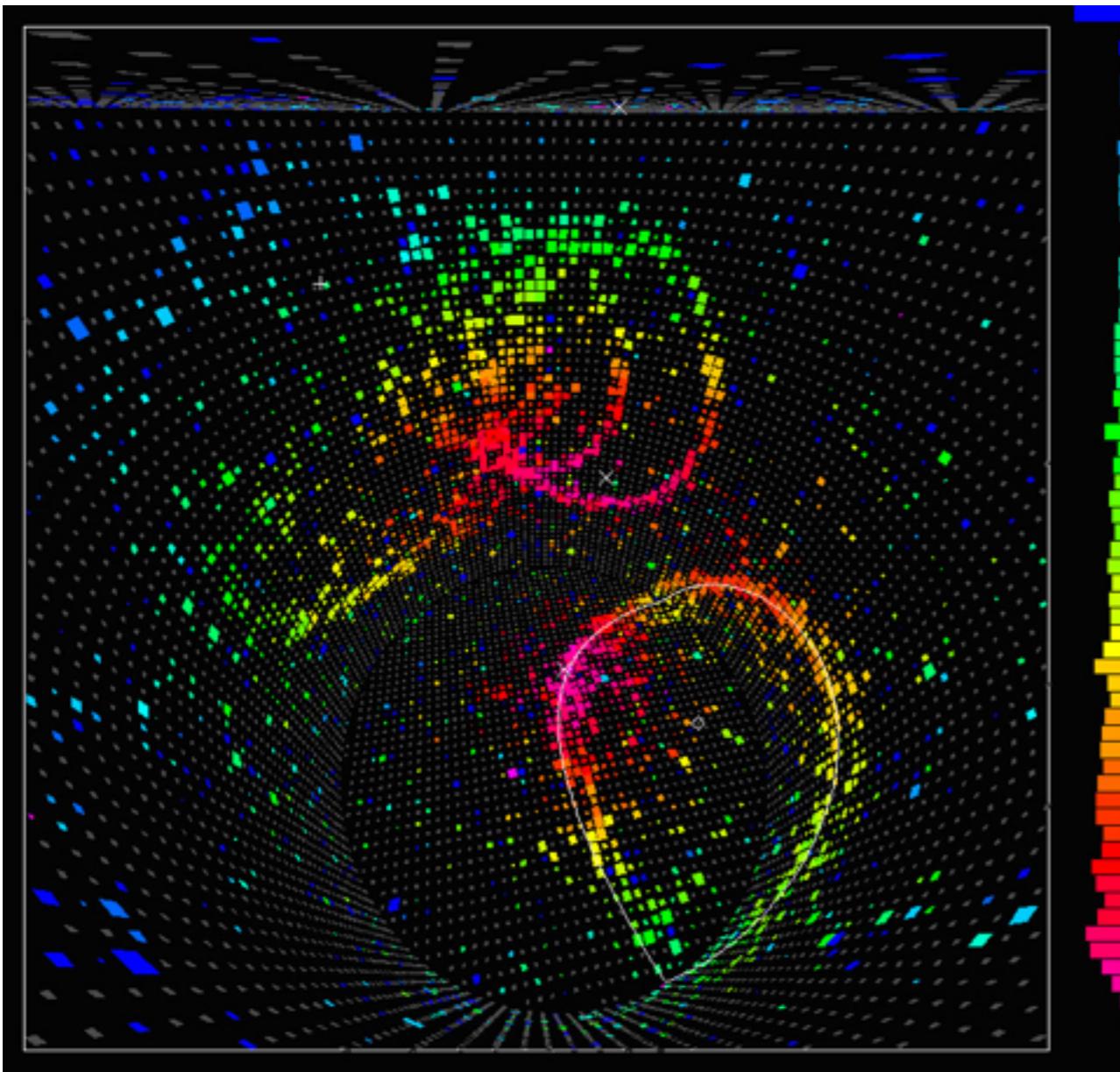


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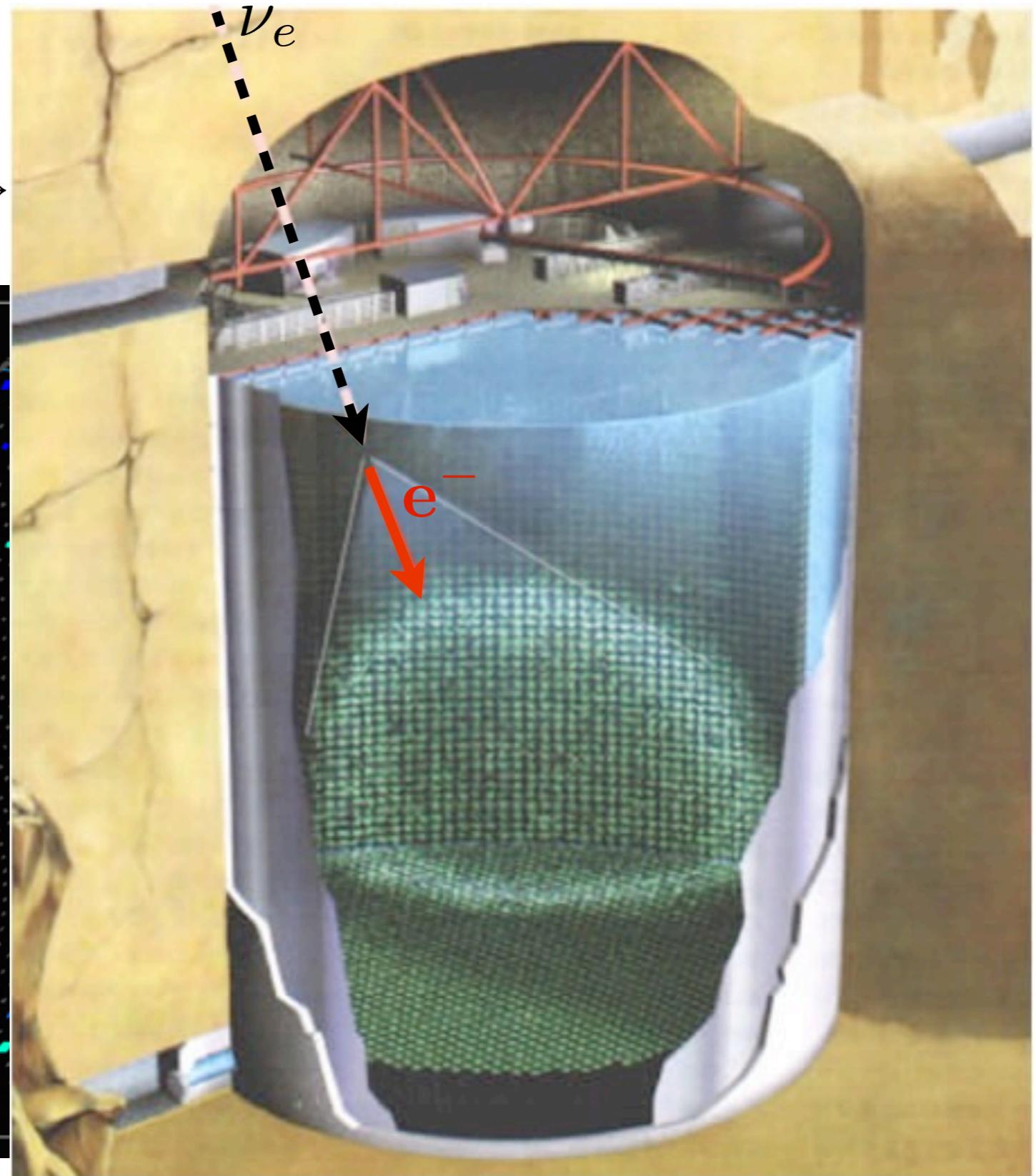
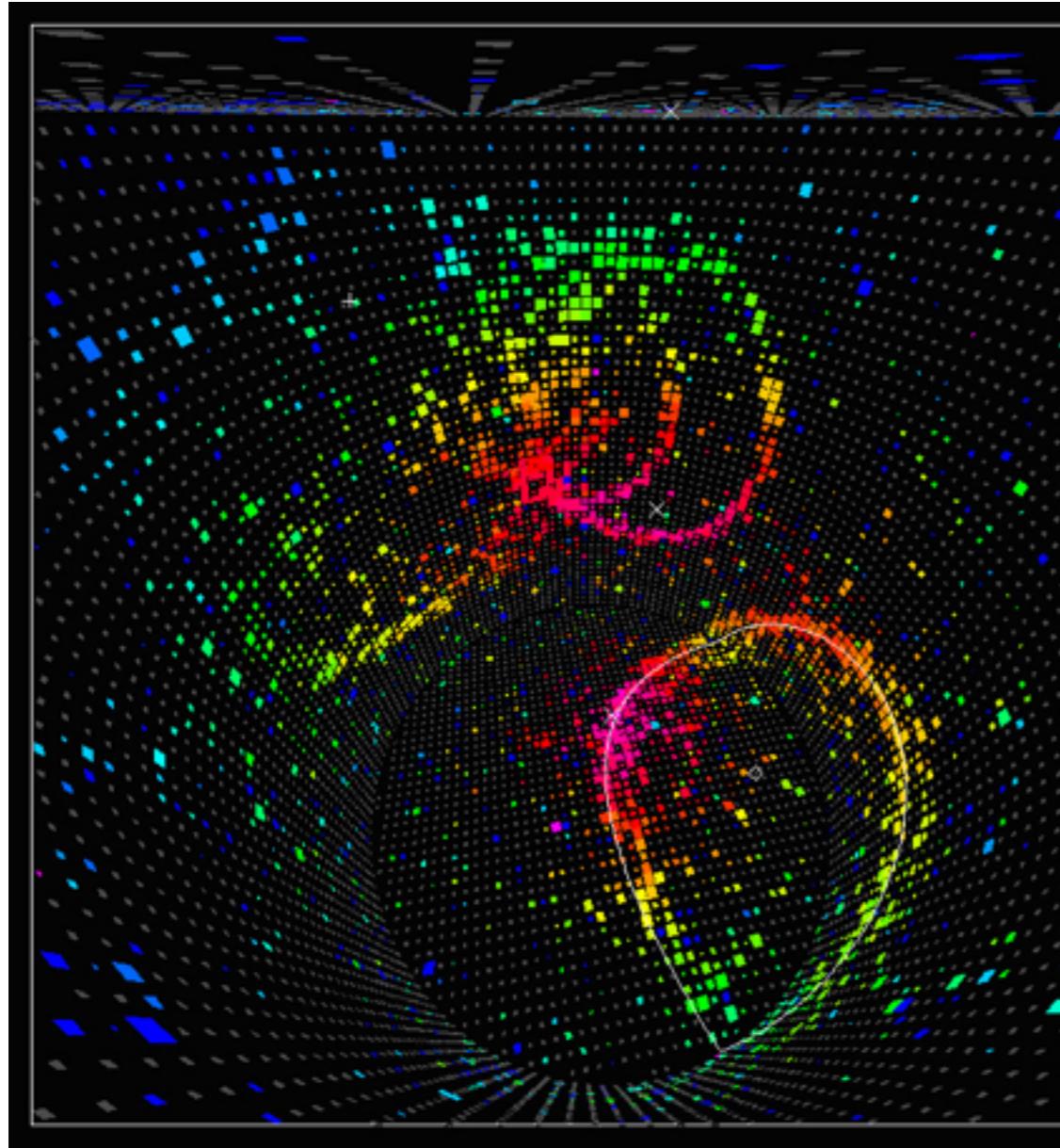
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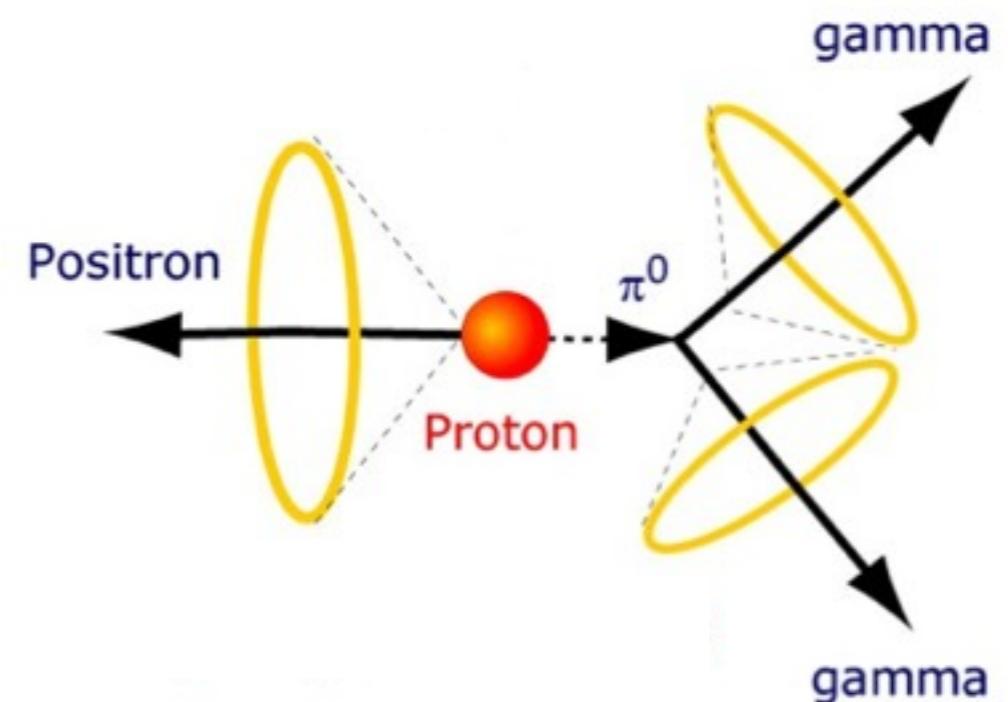
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Main background: $\nu N \rightarrow Ne^+ + \# \pi$ inelastic CC scattering of atmospheric neutrinos



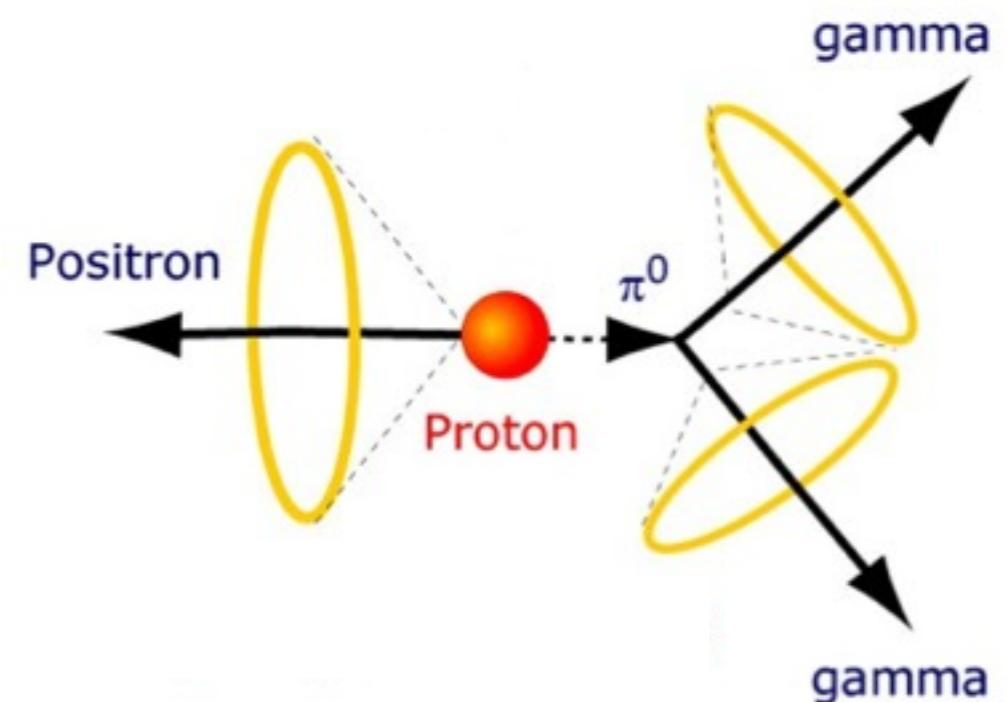
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Other complication - nuclear effects

- majority of nucleons in oxygen
- Fermi motion
- pion charge exchange
- absorption



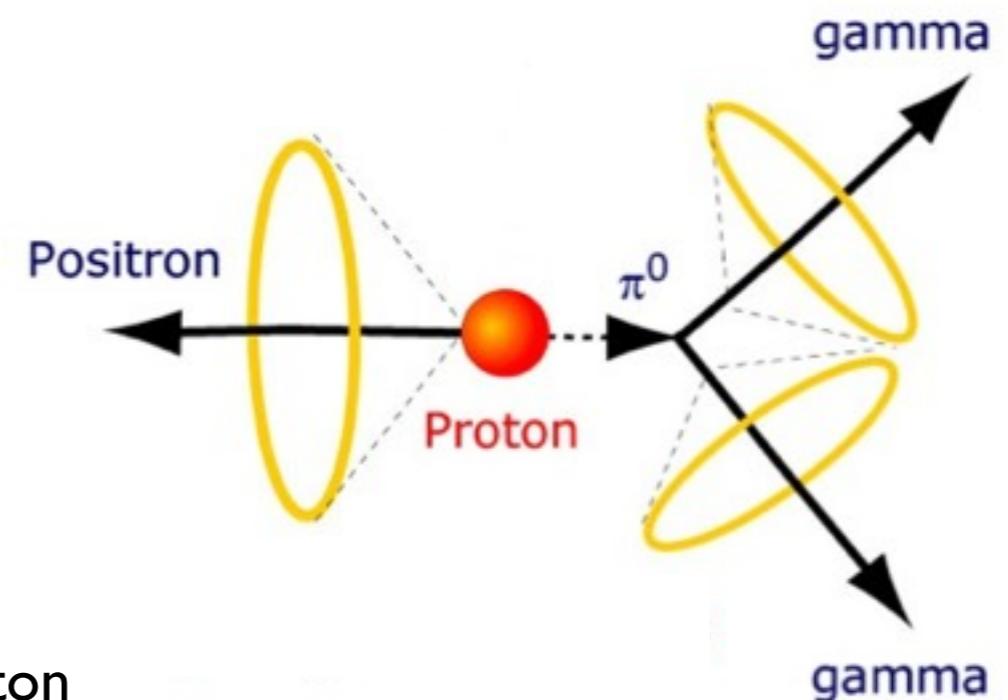
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Other signals

- nuclear recombination - extra 6.3 MeV photon
- neutron capture at a dope (Gd, ...)

Proton decay in water

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Proton decay in water

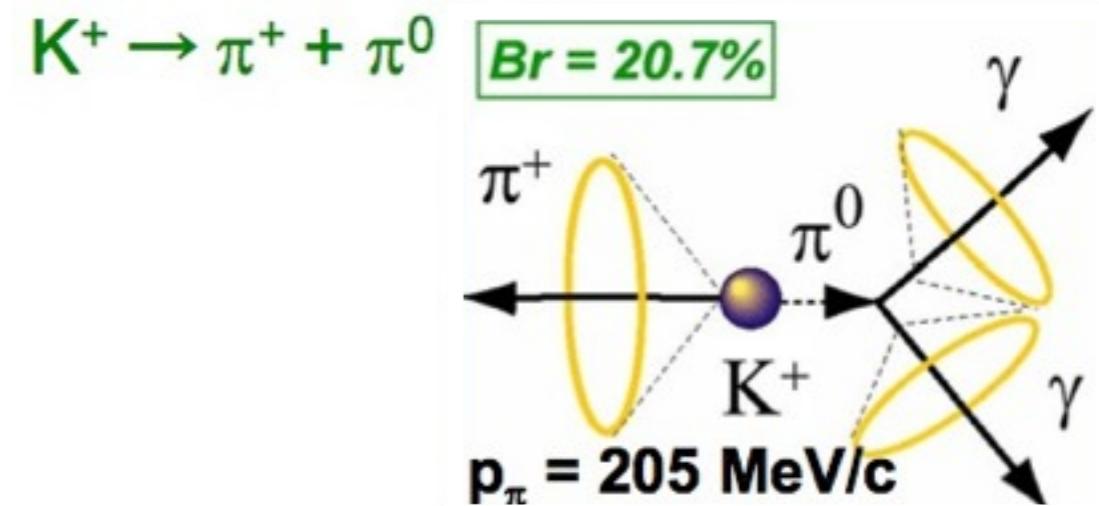
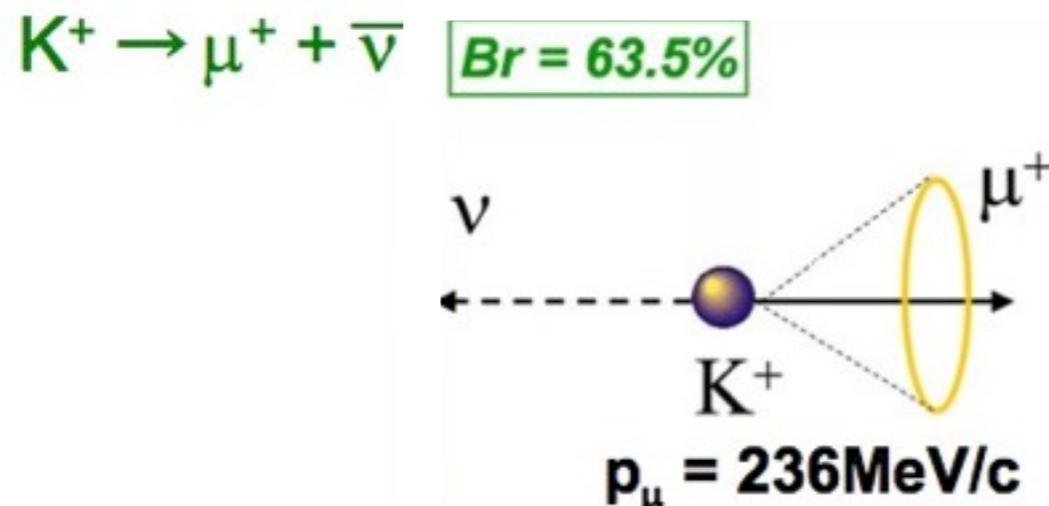
“Silver channel”: $p \rightarrow K^+ \nu$ $p_K = 340 \text{ MeV}$ Kaons don't shine !

Proton decay in water

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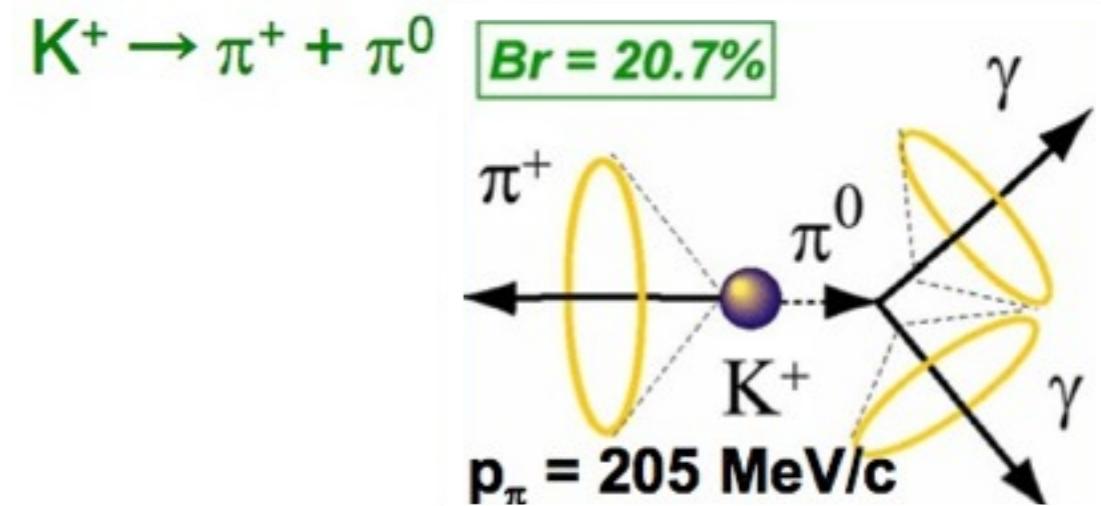
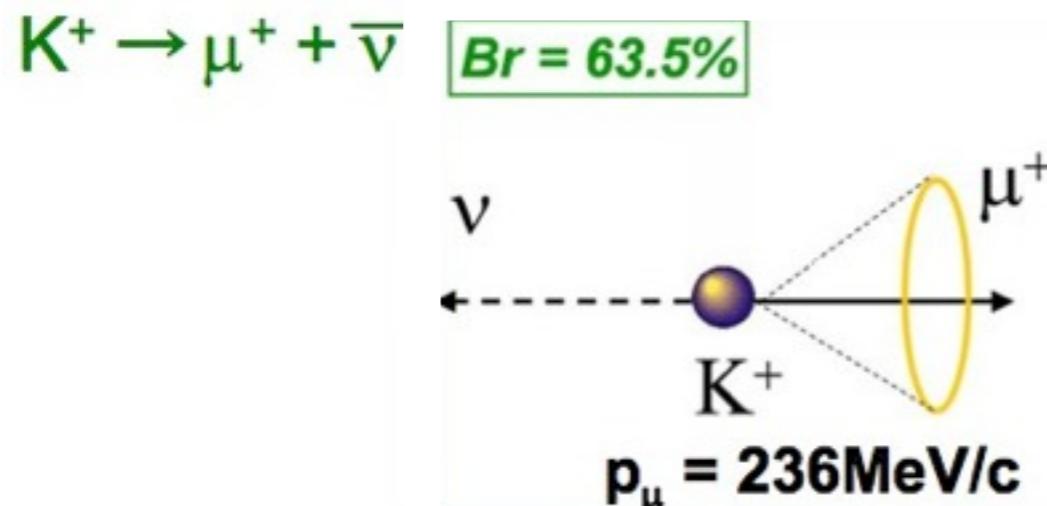


- single cone

- 2 EM cones
- little opposite-side activity

Proton decay in water

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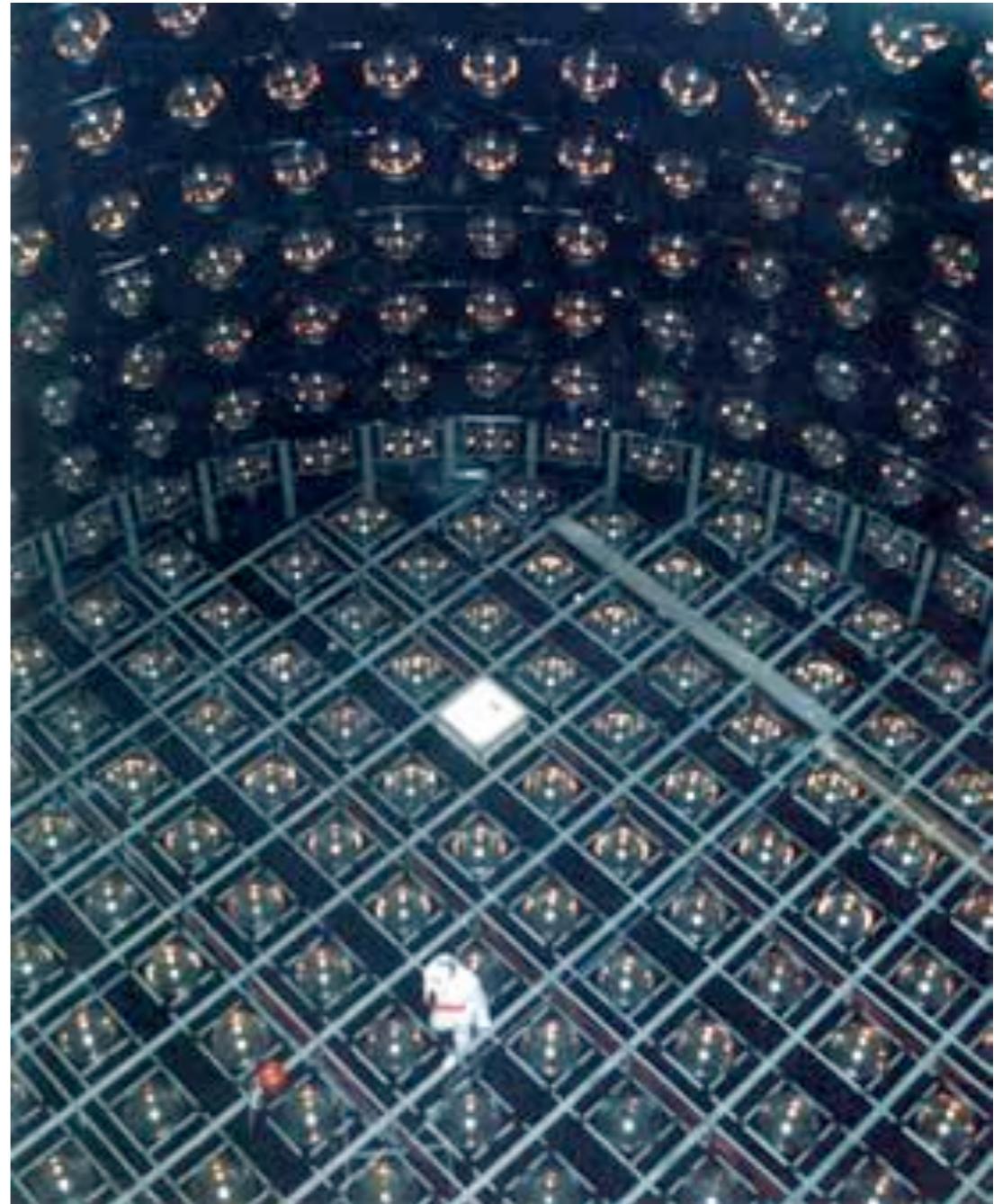
About one order of magnitude less sensitive than $p \rightarrow \pi^0 e^+$

First large water-Cherenkov detectors

KamiokaNDe

Kamioka-cho, Gifu, Japan

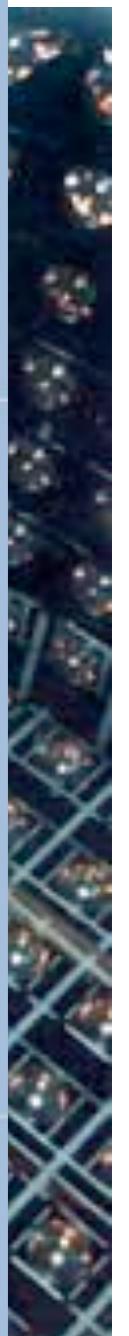
3,000 tons of pure water, about 1,000 PMs



First large water-Cherenkov detectors

Kamioka

3,000

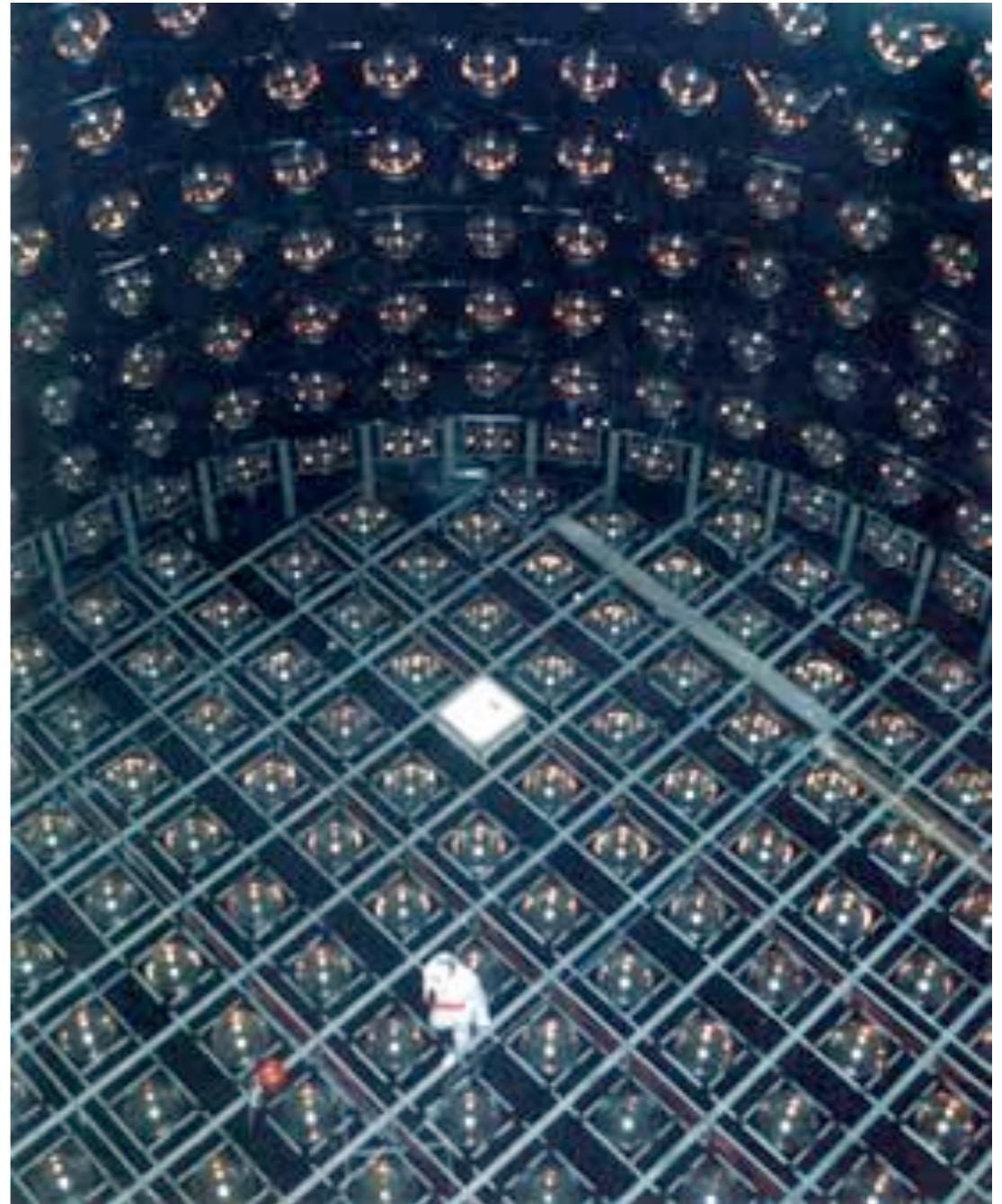


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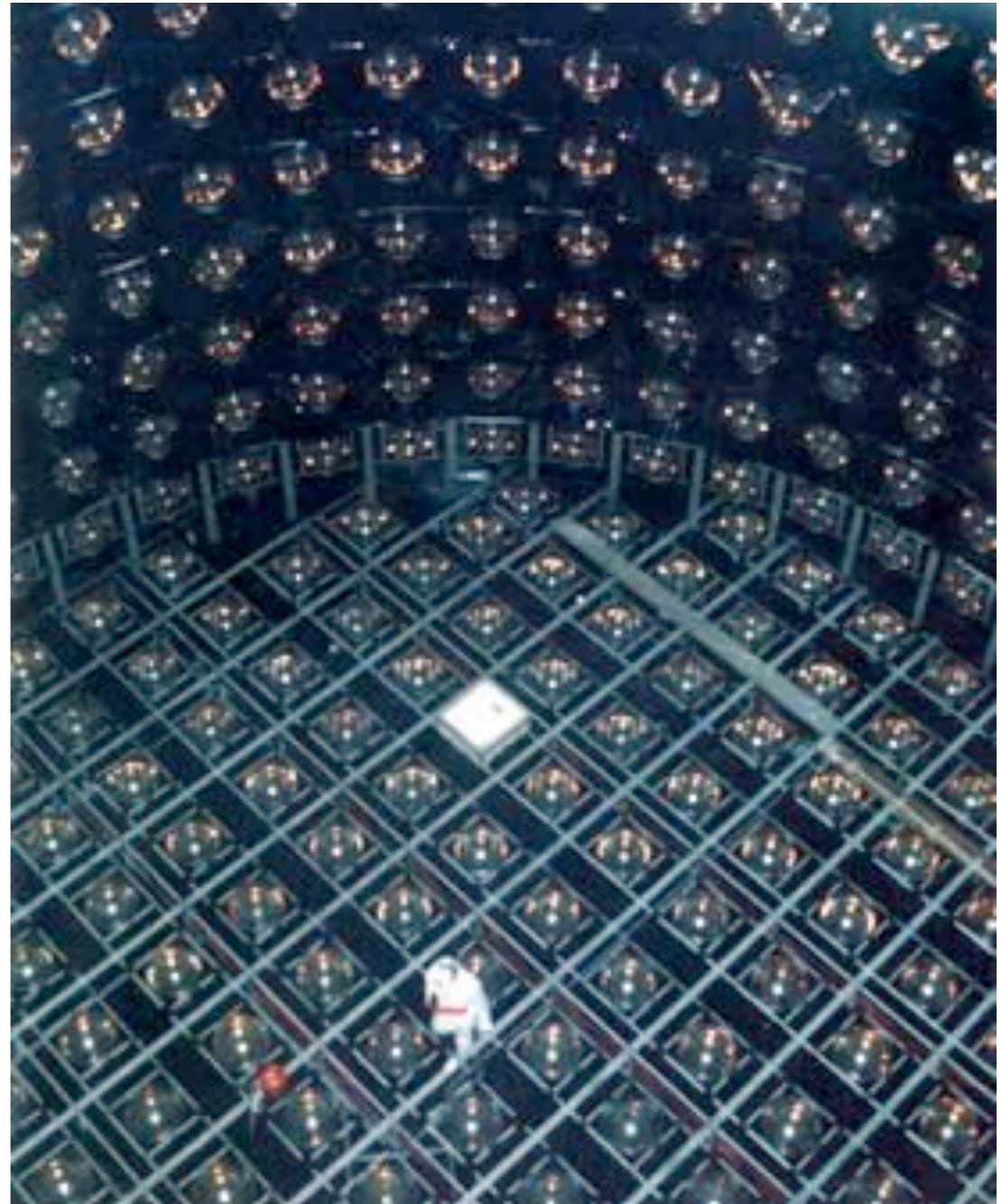
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1983-1985 - first phase (proton decay focused)

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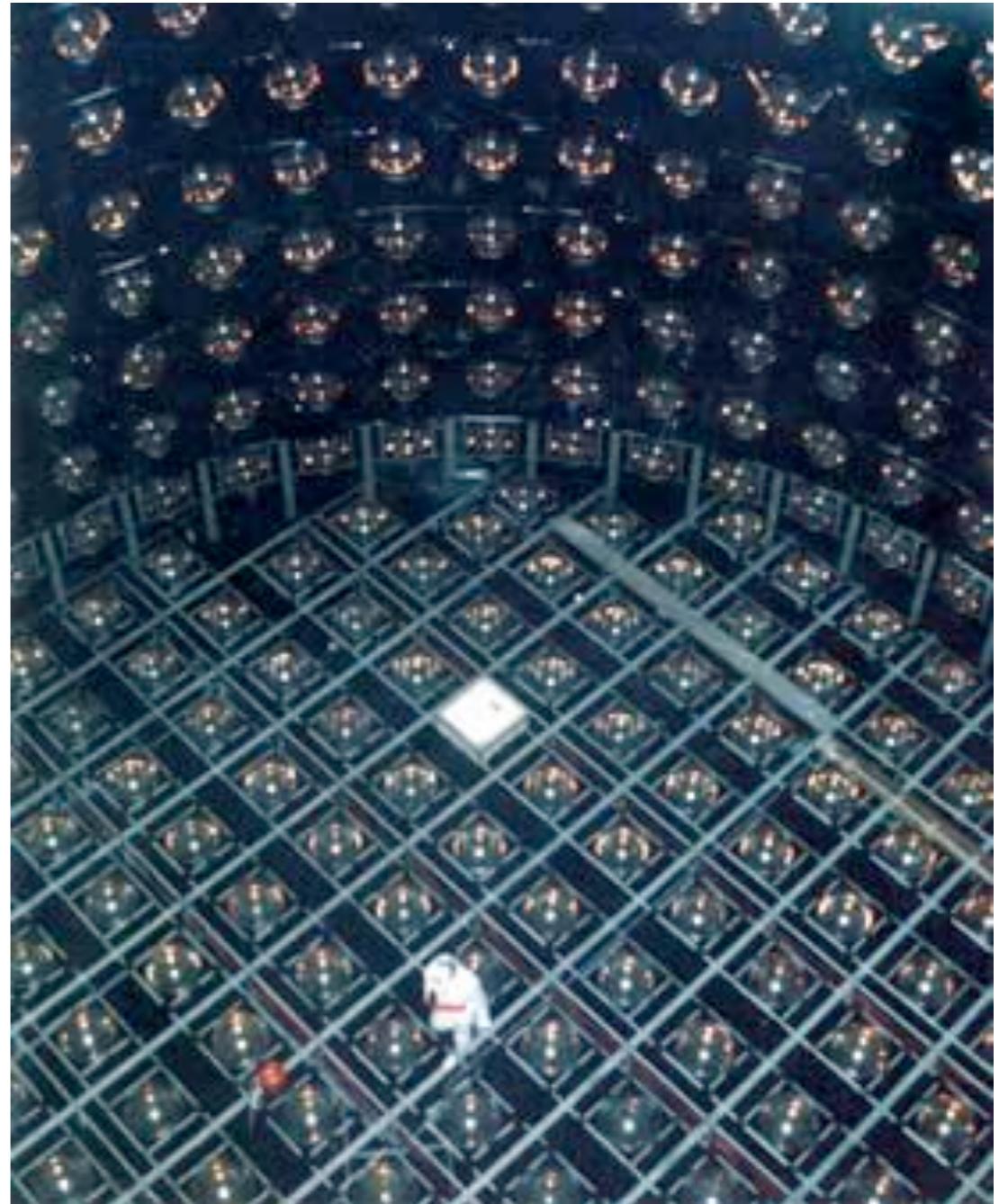
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1987-1990 - solar neutrino deficit studies

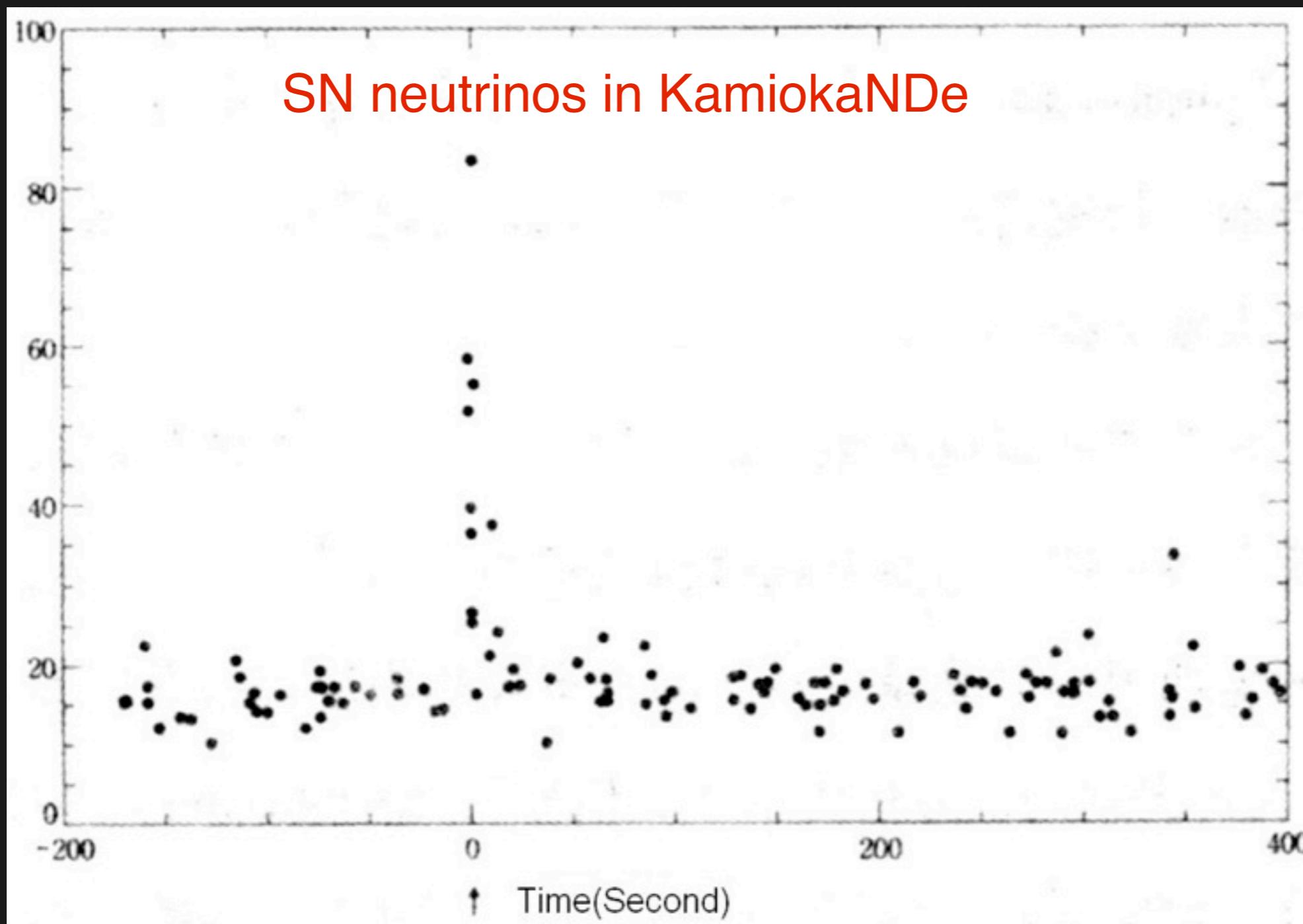
1990 Solar neutrino deficit confirmation



2002 Nobel prize for Masatoshi Koshiba

Feb 23 1987 07:35 UT

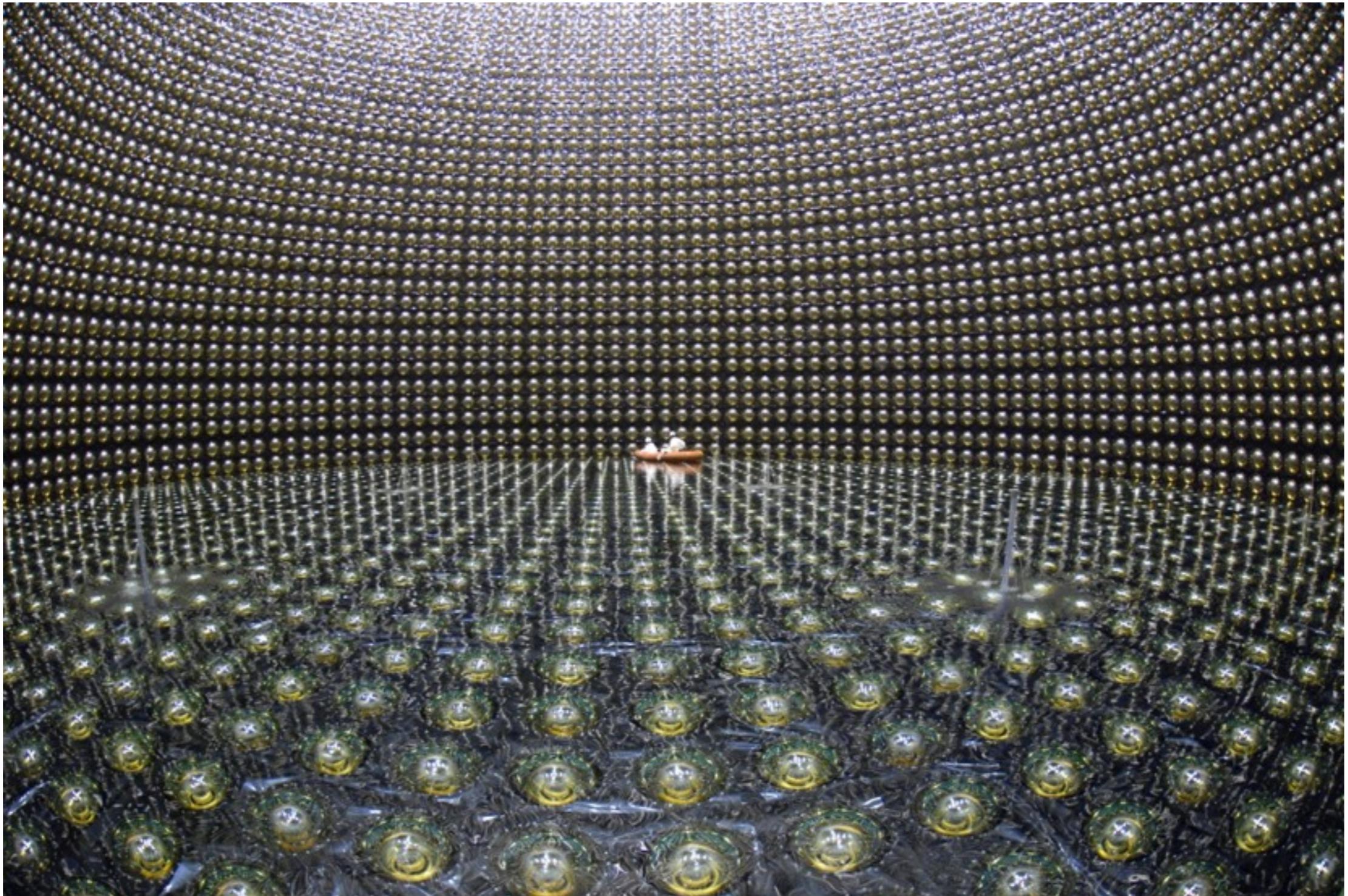
SN neutrinos in KamiokaNDe



Current limits

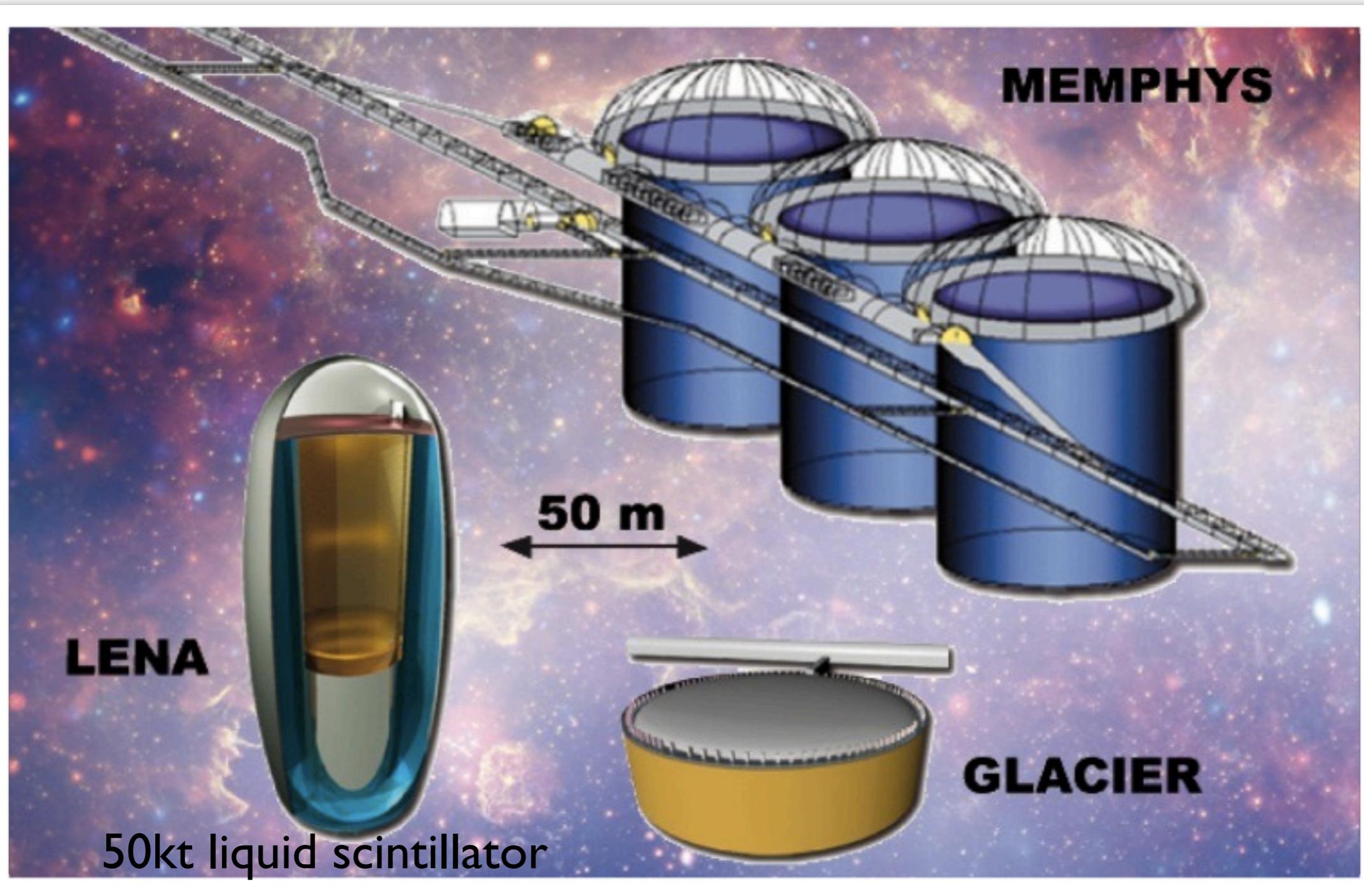
Super-K (30kt WC):

$$\tau(p \rightarrow \pi^0 e^+) \gtrsim 2 \times 10^{34} \text{ yr}$$



Future?

Large volume p-decay searches proposals

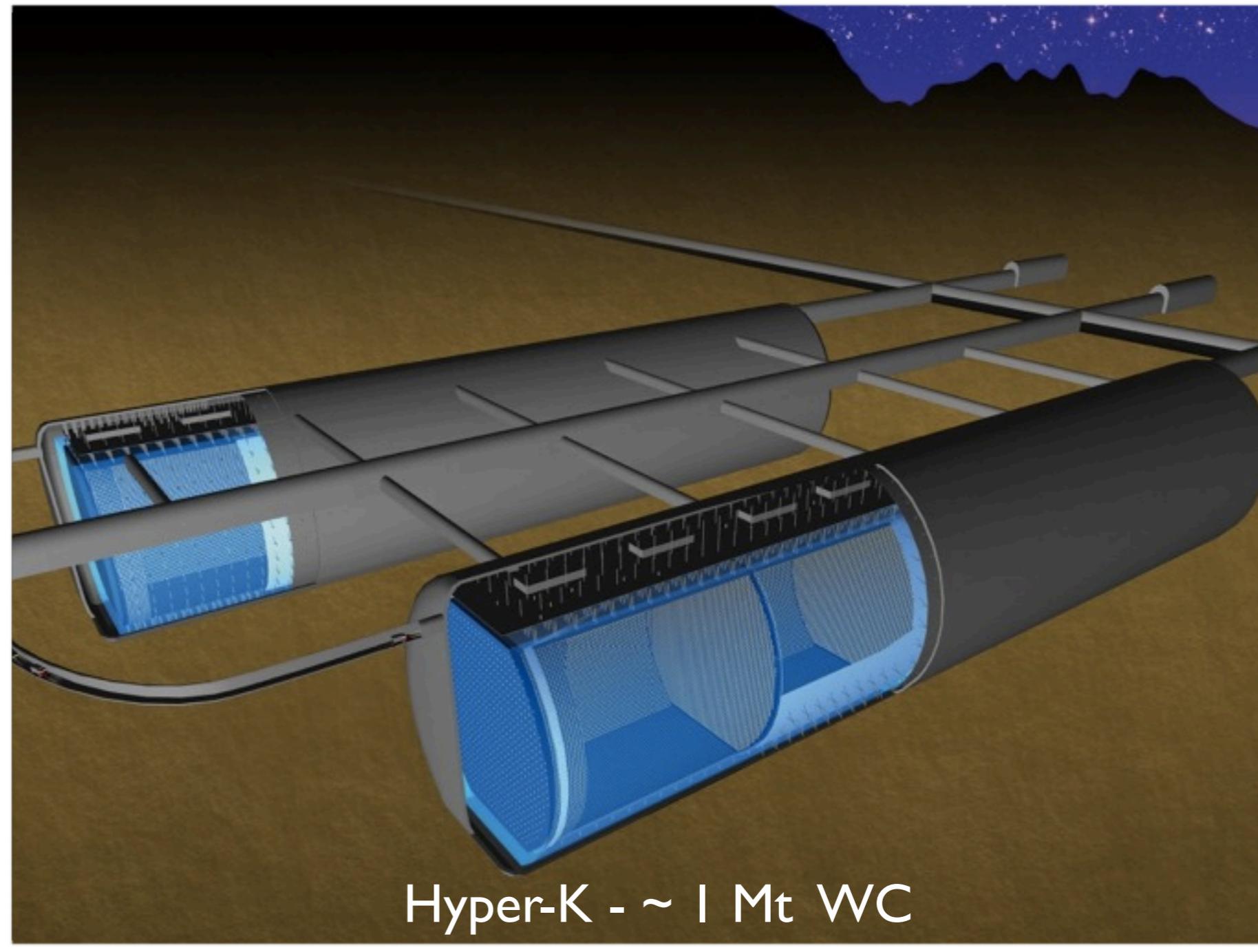


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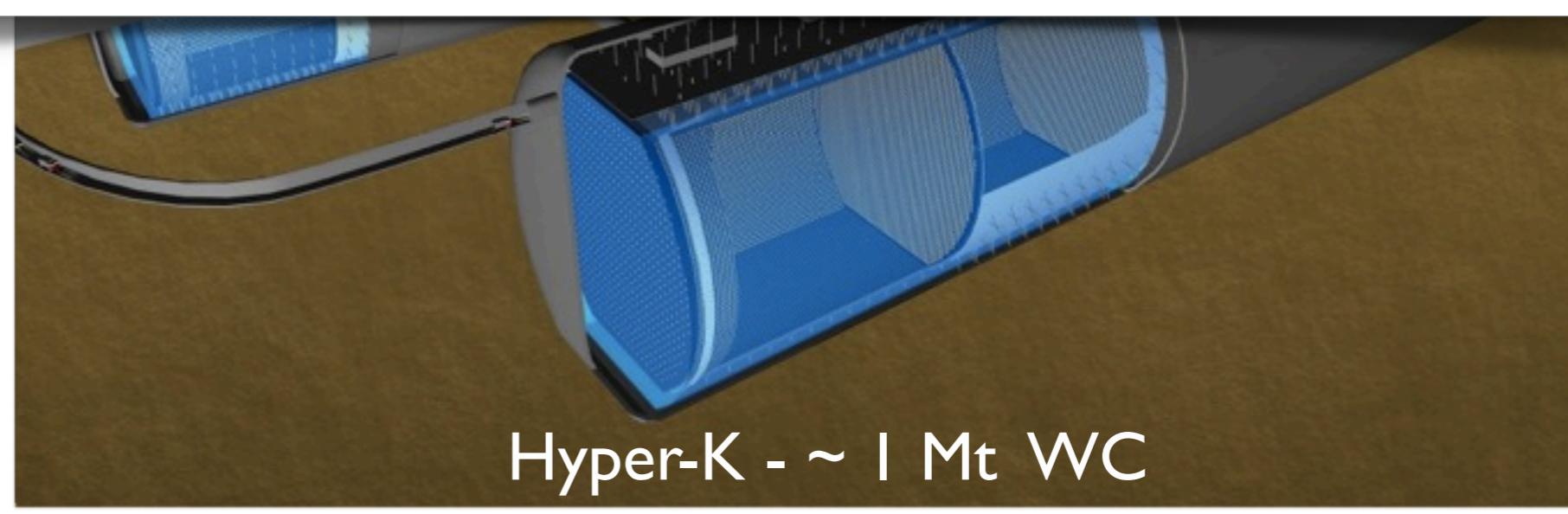
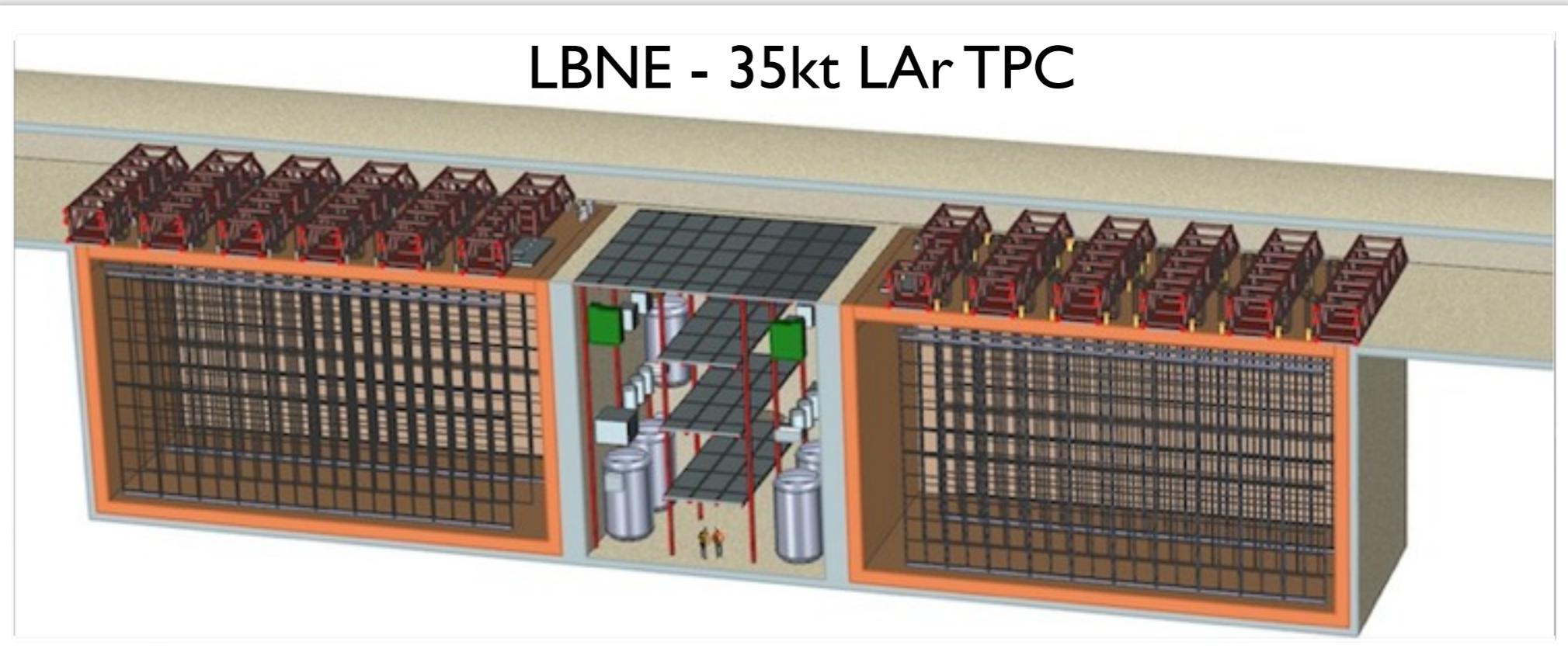
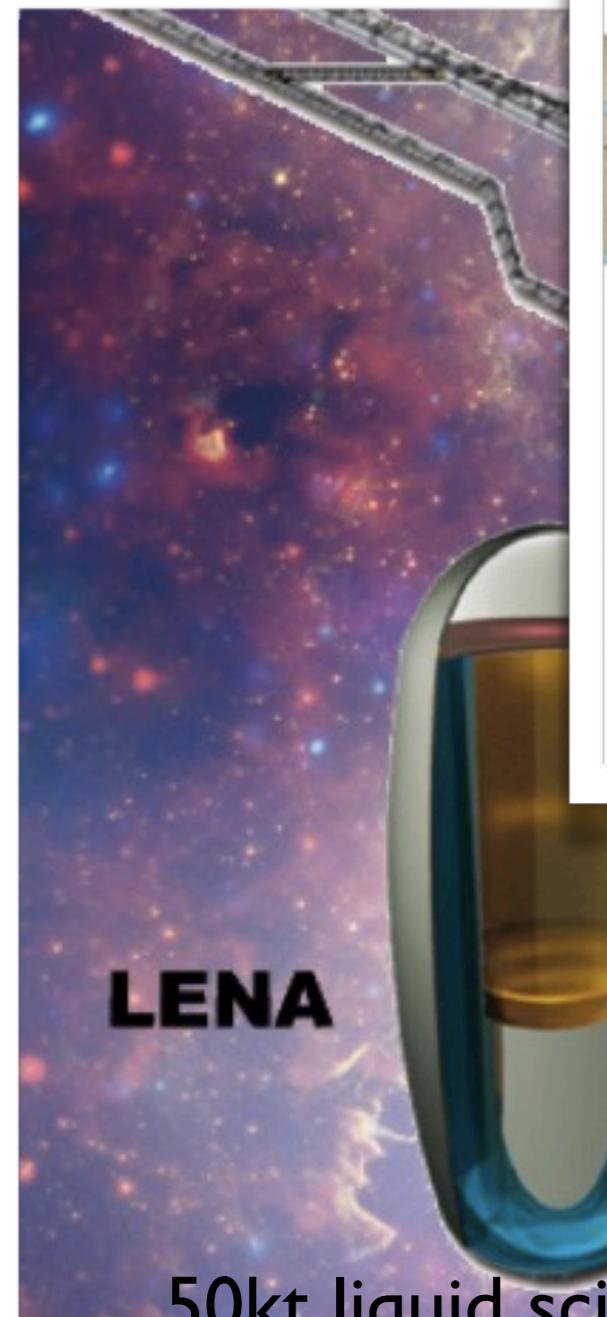
50kt liquid scintillat



Hyper-K - ~ 1 Mt WC

Future?

Large volume p-decay searches proposals



The prospects of getting the Hyper-K built are improving...

提 言

第 22 期学術の大型研究計画に関する
マスター プラン
(マスター プラン 2014)



平成26年（2014年）2月28日

日本 学 術 会 議

科学者委員会

学術の大型研究計画検討分科会

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Japanese master plan for large scale research projects



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学術の大型研究計画検討分科会

分野	計画番号	学術領域番号	計画名称	計画の概要	学術的な意義
物理学	85	23-2	大型先端検出器による核子崩壊・ニュートリノ振動実験	スーパーカミオカンデに代わる100万トン級水チェレンコフ検出器ハイパーカミオカンデを建設し、J-PARC加速器ニュートリノビームと組み合わせる事により、世界最先端の核子崩壊・ニュートリノ研究を行う。	ニュートリノにおける(粒子・反粒子対称性)探索し、ニュートリノ宇宙の進化論に対する。さらに核子崩壊せ、素粒子物理学の超える物理の確立を
	86	23-2	高エネルギー重イオン衝突実験によるクオーク・グルーオン・プラズマ相の解明	高エネルギー重イオン衝突実験(RHIC-PHENIX/LHC-Alice実験)を国際協力の下で推進し、宇宙開拓直後の姿である新しい物質相QGP(クオーク・グルーオン・プラズマ)の物性科学を開拓する。	ハドロン物質の相構性の理解を通じて、質相構造の理解が、カイラル対称性の自、クオークの閉じ込め度場の物理、非線形相関物性現象の解明
	87	23-2	光子ビームによるクオーク核物理研究	光子ビームによるクオーク核物理研究を推進し、量子色力学真空とハドロン内クオーク相関を究明する。東北大学電子光物理学研究拠点と大阪大学サブアトミック科学研究拠点との拠点間連携研究計画である。	物質の質量の99.9%を担っており、その98%をカイラル対称性によって創成され、それによって学術的観点複雑な階層の研究がなされる。

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Hyper-K

- The HK/T2HK collaboration is excited and active
- MOU signed on January 31 2015
- The european part of the collaboration is just forming
- R&D funding secured (both the HK and T2K/J-PARC upgrade)
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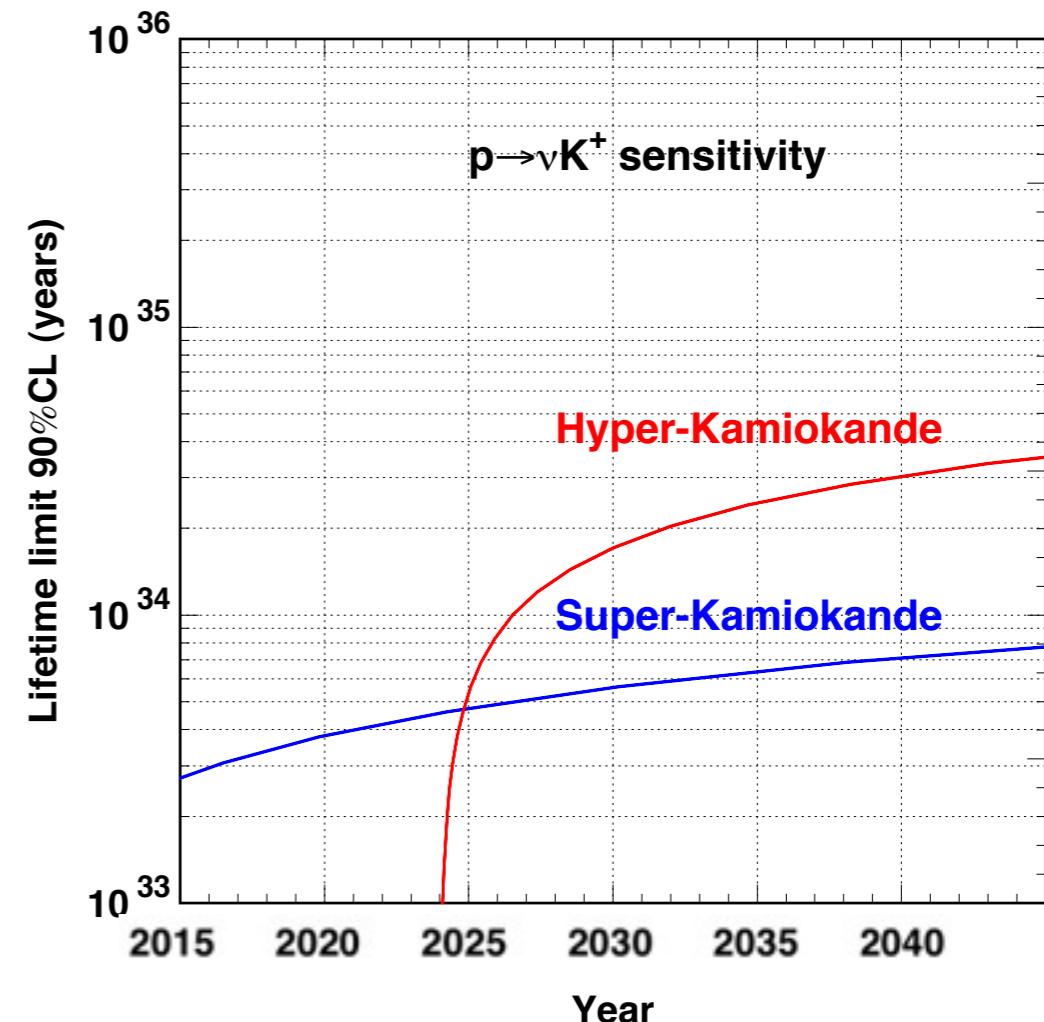
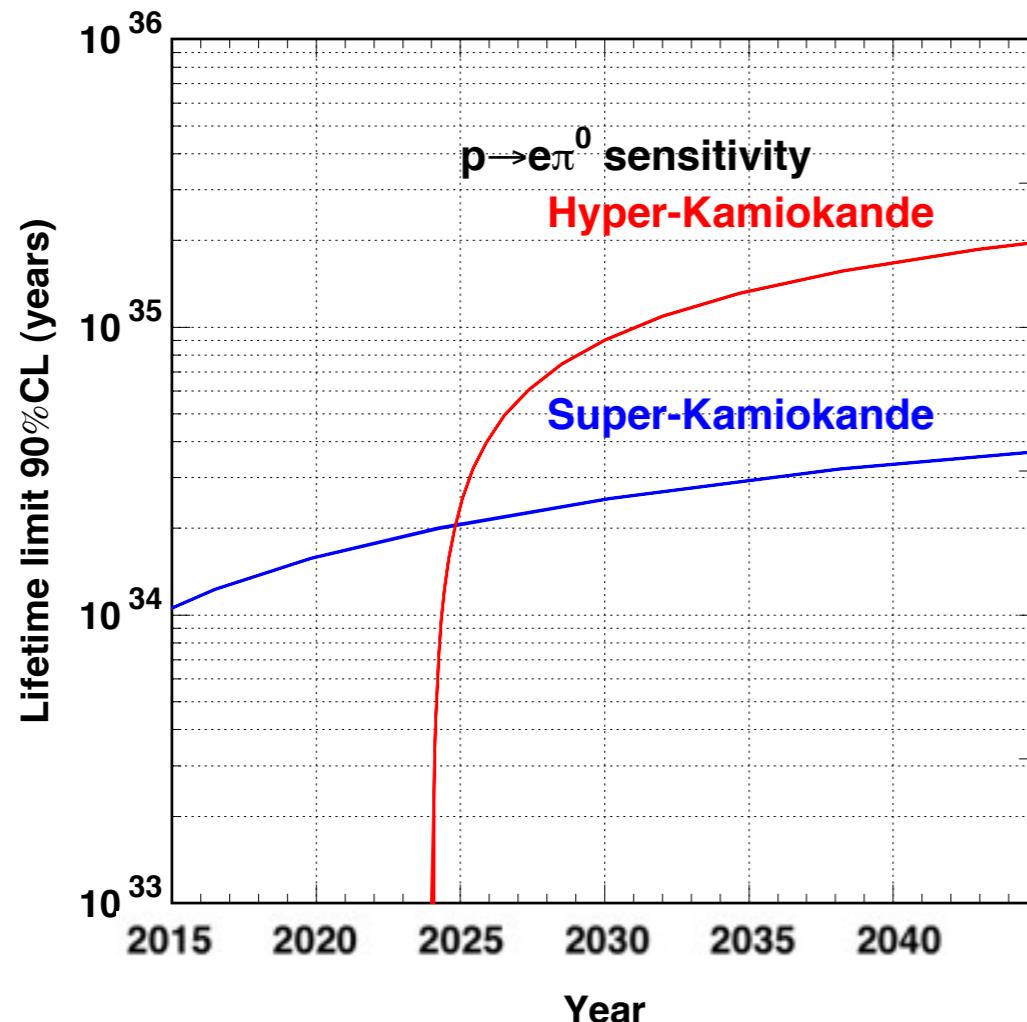


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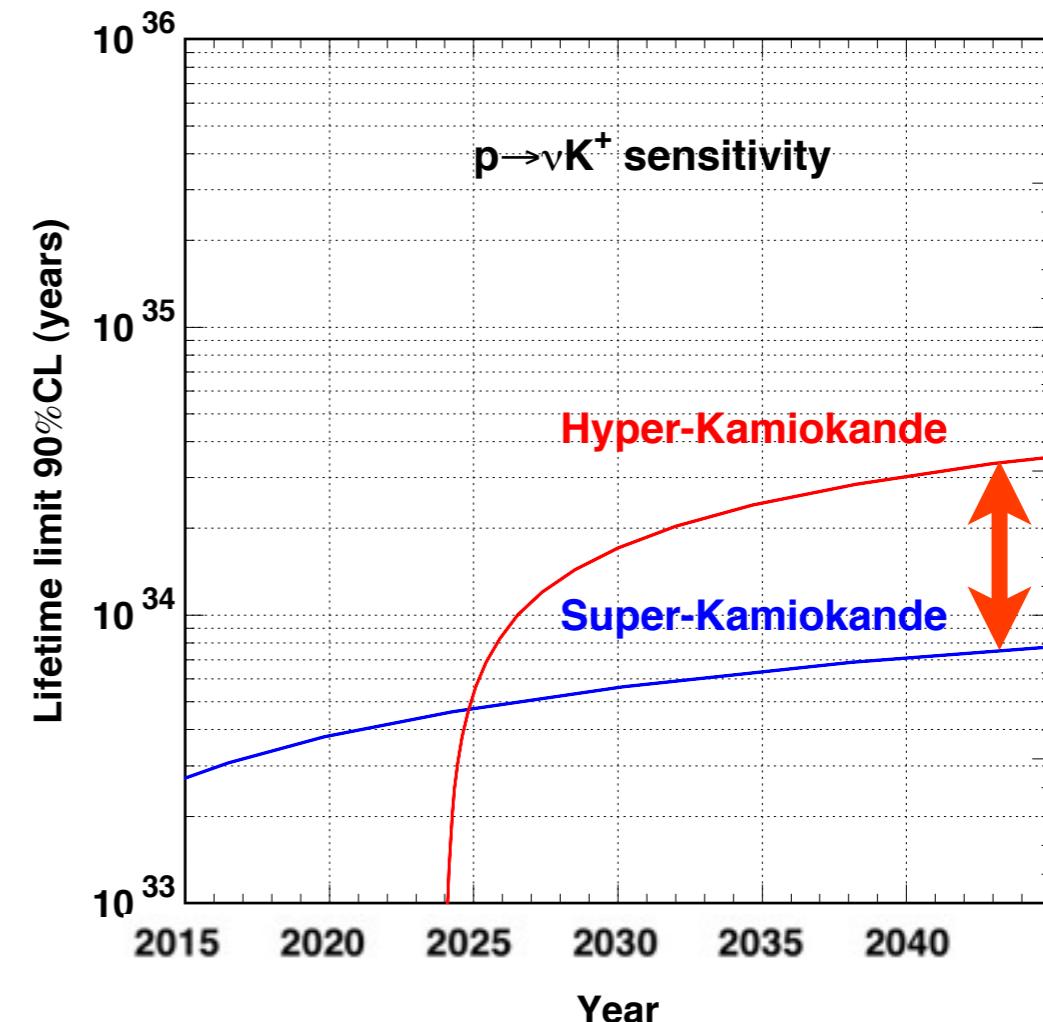
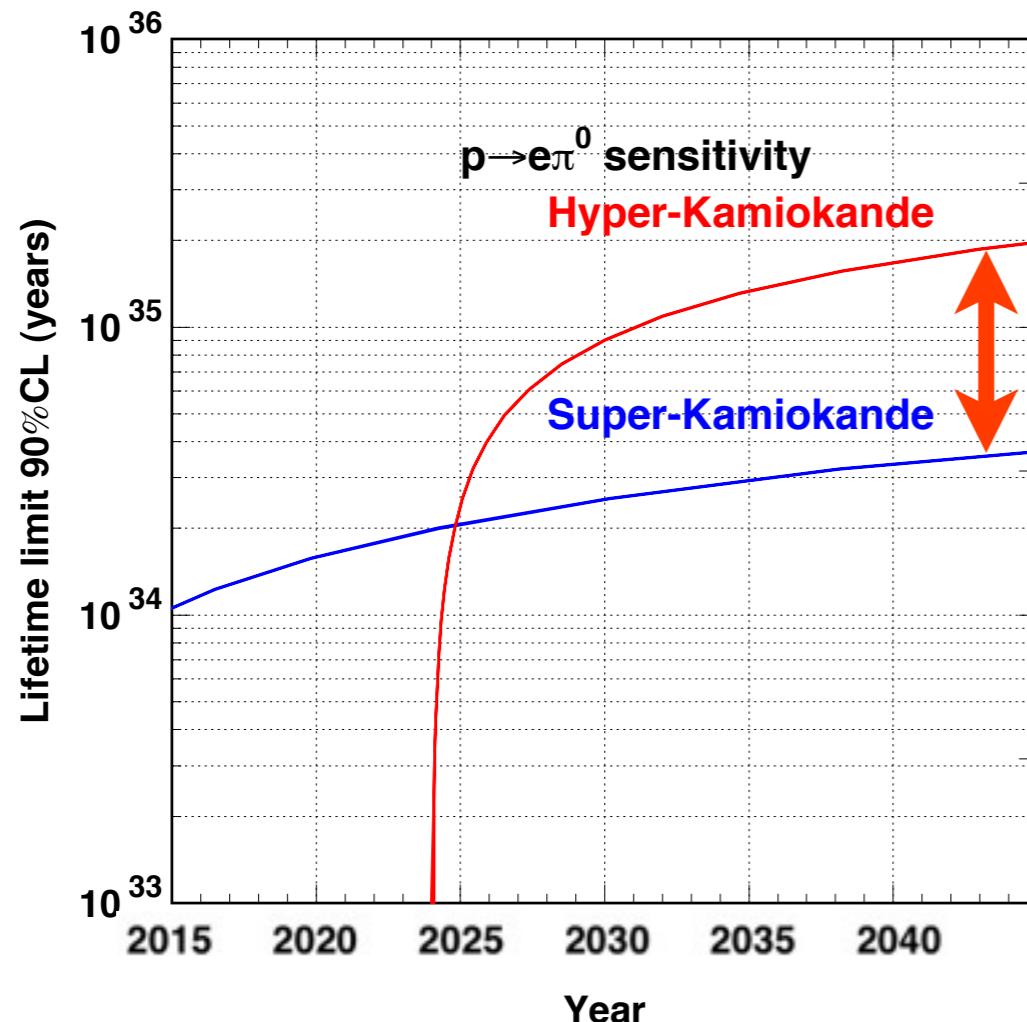
Hyper-K p-decay sensitivity projection



Abe et al., arXiv:1109.3262 [hep-ex]

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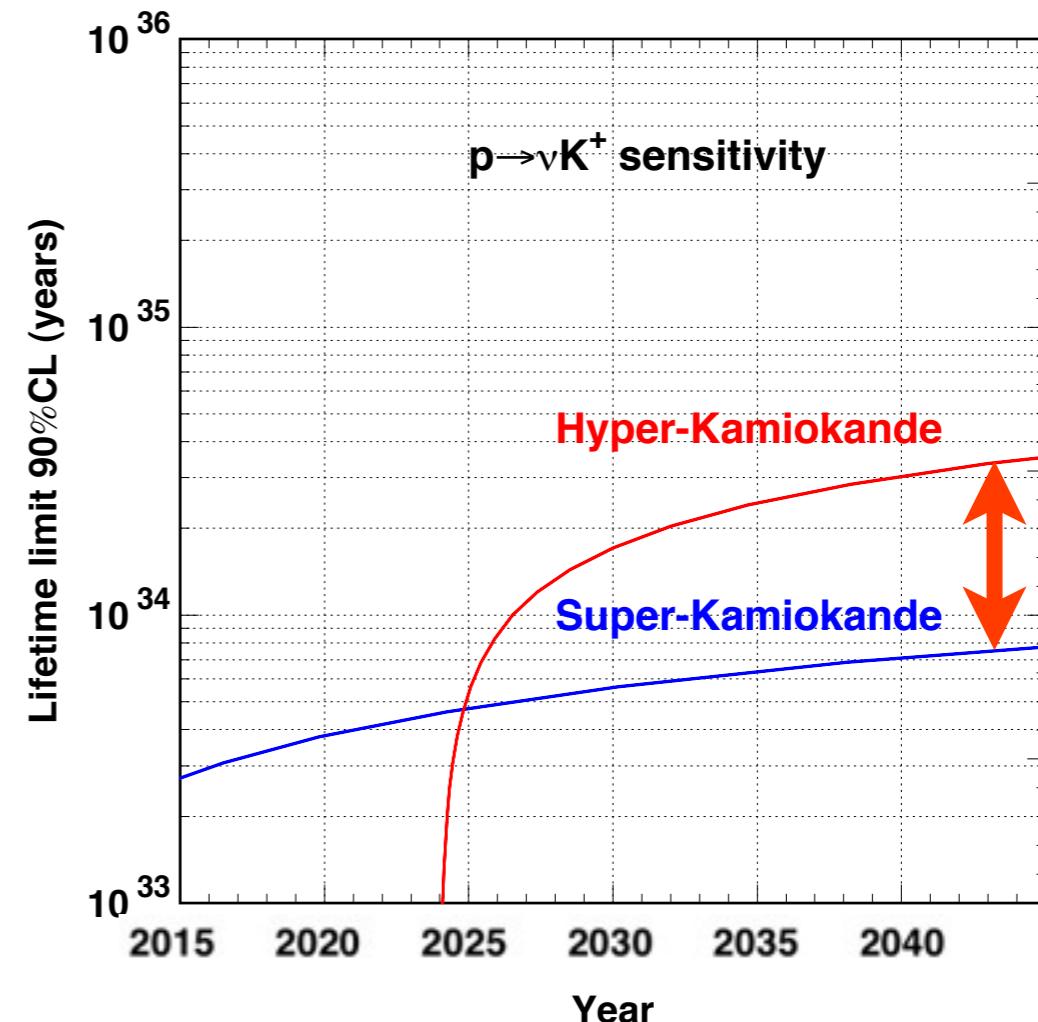
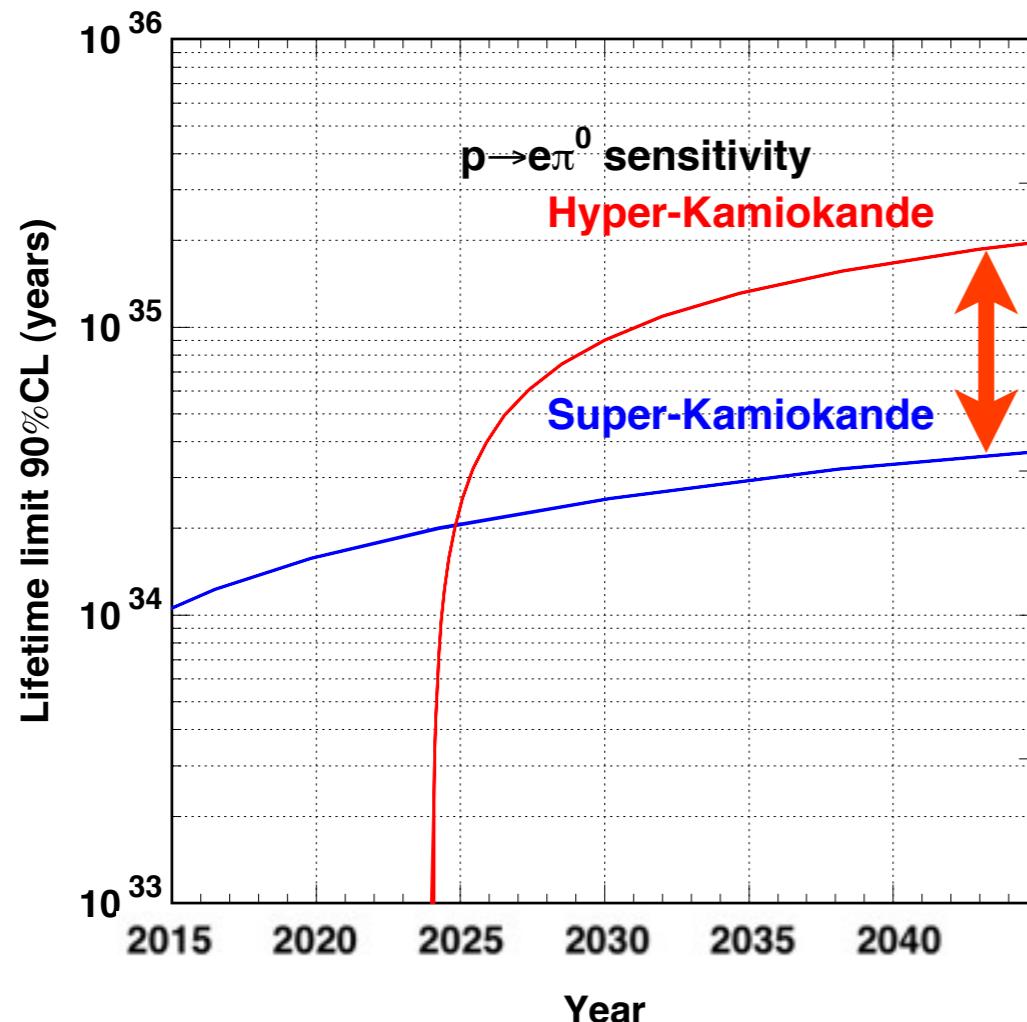


Abe et al., arXiv:1109.3262 [hep-ex]

Accuracy of a **factor of few** in Γ_p estimates needed to make a case !

Regardless of what happens...

Hyper-K p-decay sensitivity projection



Abe et al., arXiv:1109.3262 [hep-ex]

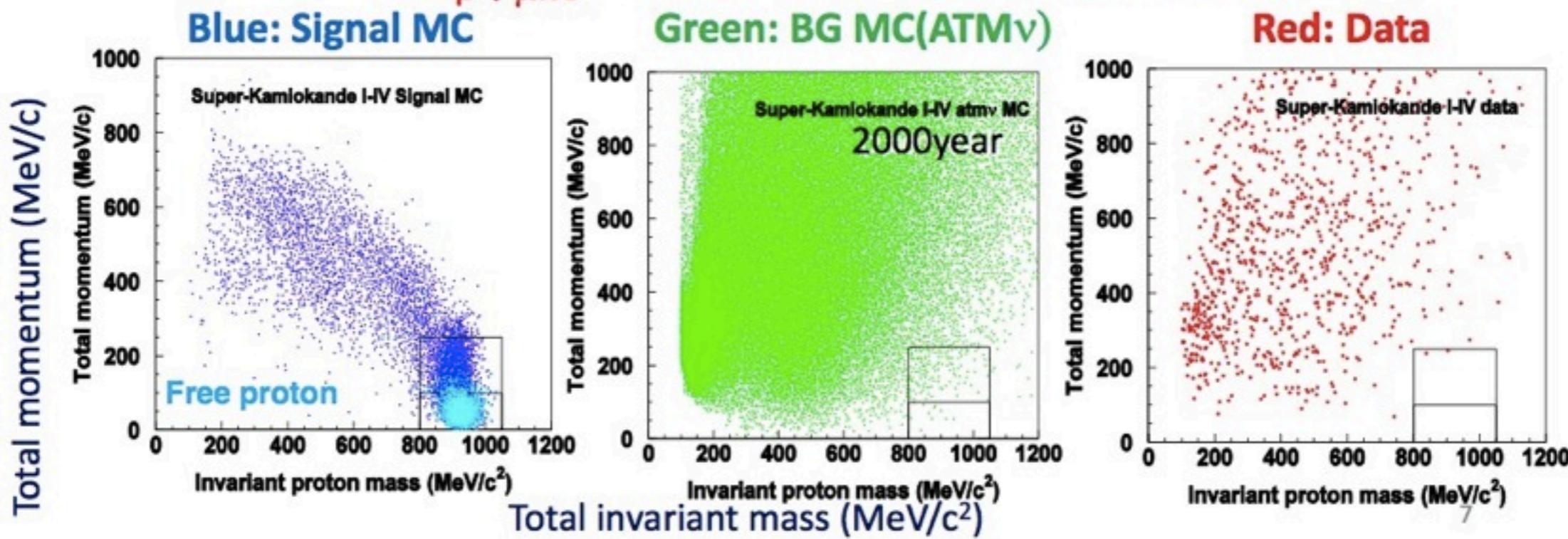
Accuracy of a **factor of few** in Γ_p estimates needed to make a case !
(At least) **NLO theory precision required**

Results of $p \rightarrow \mu^+ \pi^0$

(analysis proceeds as with $e^+ \pi^0$ with additional requirement of 1 Michel-e)

- **306.3 kton·yrs (SKI-IV)** (220kt·yrs in PRD)
- signal $\epsilon(P_{\text{tot}} < 250 \text{ MeV}/c)$: 30-40%
- total expected #BKG:
 - $P_{\text{tot}} < 100$: ~0.05, $100 \leq P_{\text{tot}} < 250$: ~0.82
- no significant data excess

$$\tau/B_{p \rightarrow \mu\pi^0} > 7.78 \times 10^{33} \text{ years (90\% CL)}$$



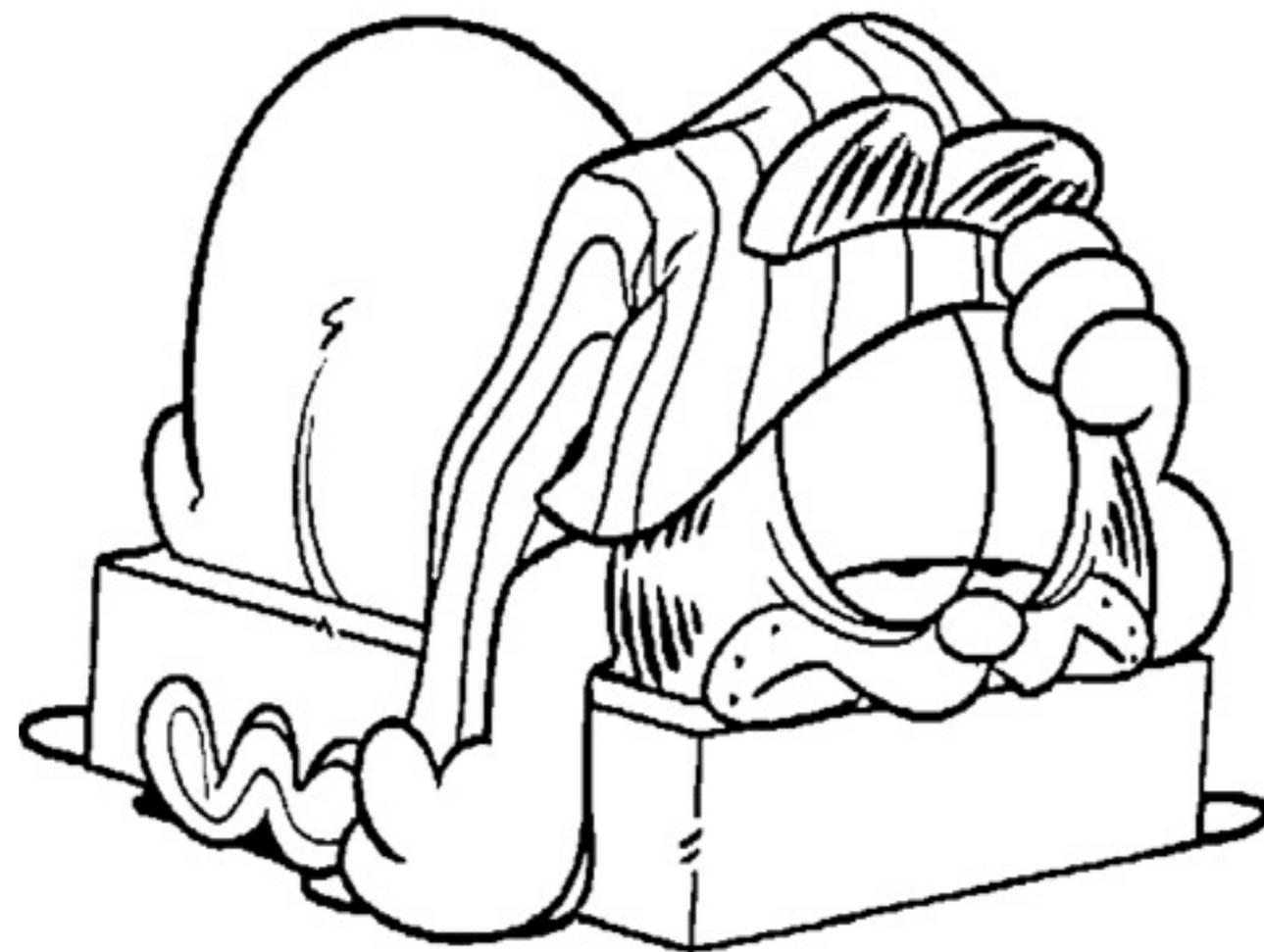
Regardless of what happens...

Optimistic scenario: Day I



Regardless of what happens...

Optimistic scenario: Day 2



www.fun-with-pictures.com

Regardless of what happens...

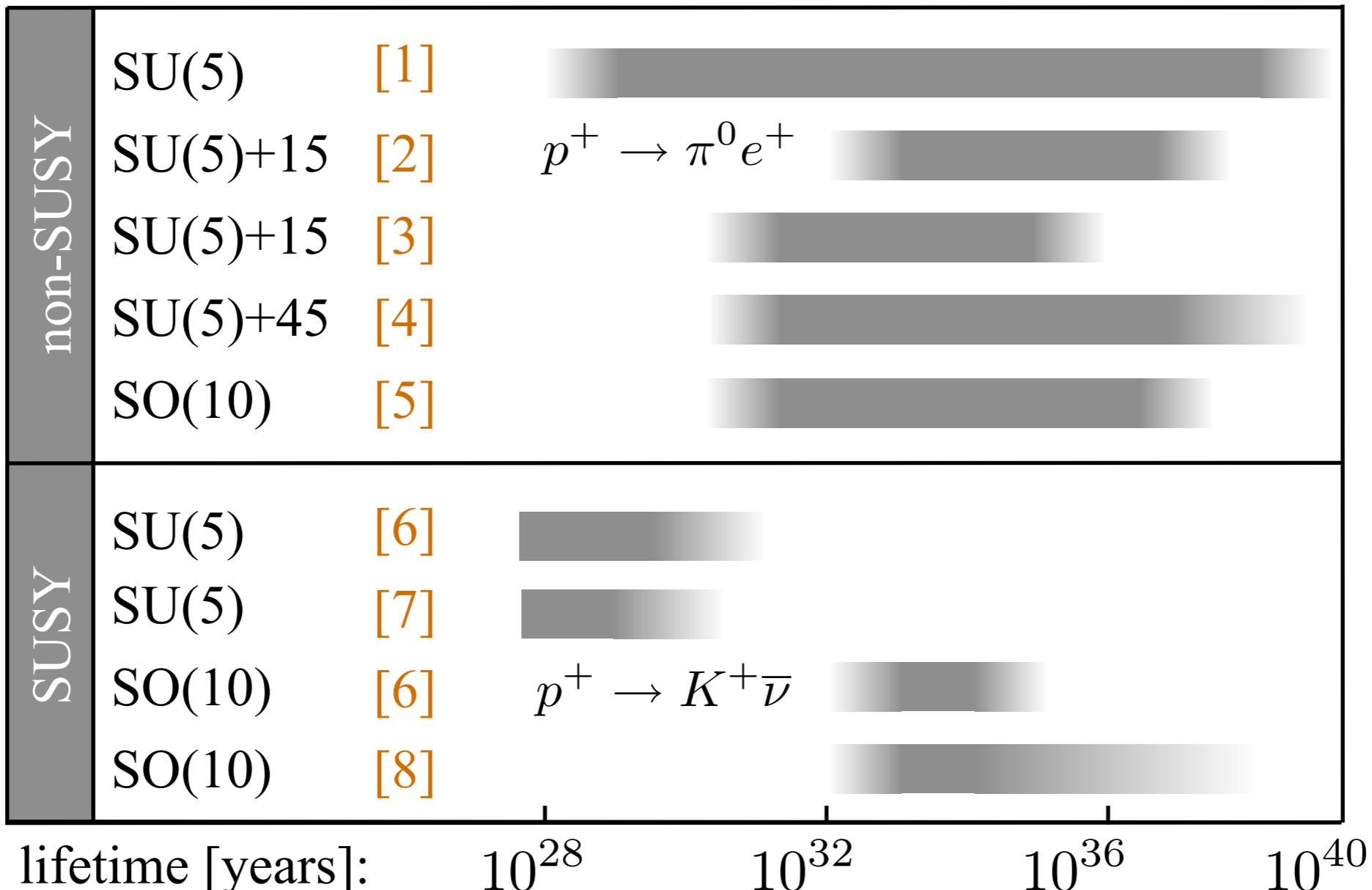
Optimistic scenario: Day 3



Are we in a position to discriminate among different GUTs ?

Proton lifetime estimates in GUTs

Proton lifetime estimates in GUTs



[1] Georgi, Quinn, Weinberg, PRL 33, 451 (1974)

[2] Dorsner, Fileviez Perez, NPB 723, 53 (2005)

[3] Dorsner, Fileviez Perez, Rodrigo, PRD75, 125007 (2007)

[4] Dorsner, Fileviez Perez, PLB 642, 248 (2006)

[5] Lee, Mohapatra, Parida, Rani, PRD 51 (1995)

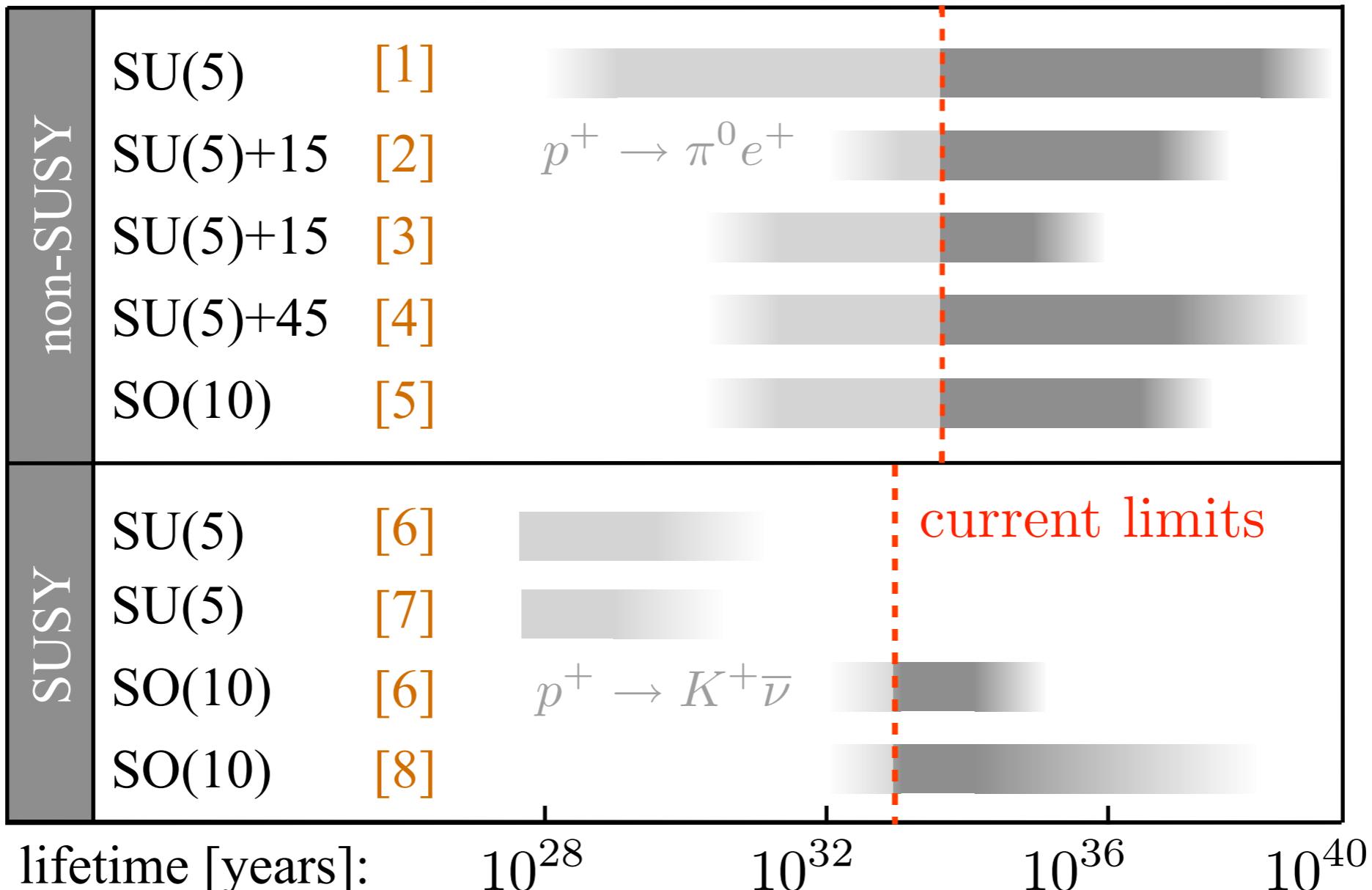
[6] Pati, hep-ph/0507307

[7] Murayama, Pierce, PRD 65. 055009 (2002)

[8] Dutta, Mimura, Mohapatra, PRL 94, 091804 (2005)

... and many more.

Proton lifetime estimates in GUTs



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... and many more.

Main theoretical uncertainties in p-decay estimates in GUTs

■ Hadronic matrix elements

■ GUT-scale (= effective mediator mass) determination

- one- vs. two-loop running (or even higher?)
- scalar spectrum & threshold effects
- Planck-scale effects
 - gauge kinetic form = matching
 - effective cut-off in GUTs

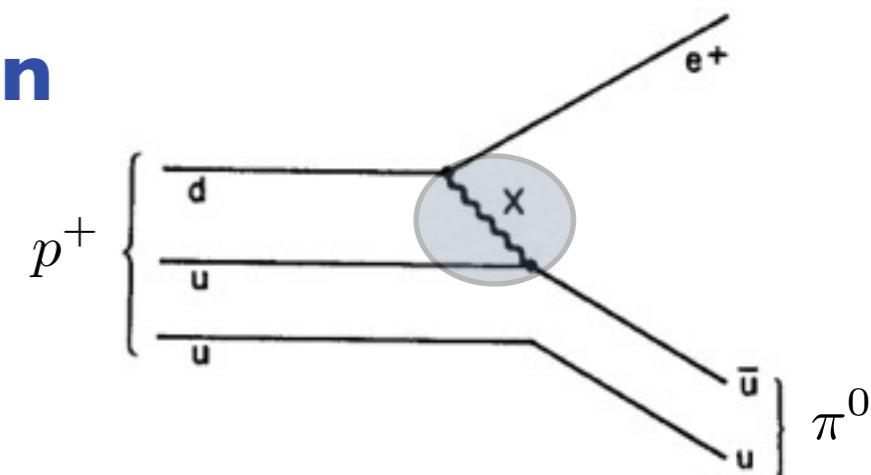
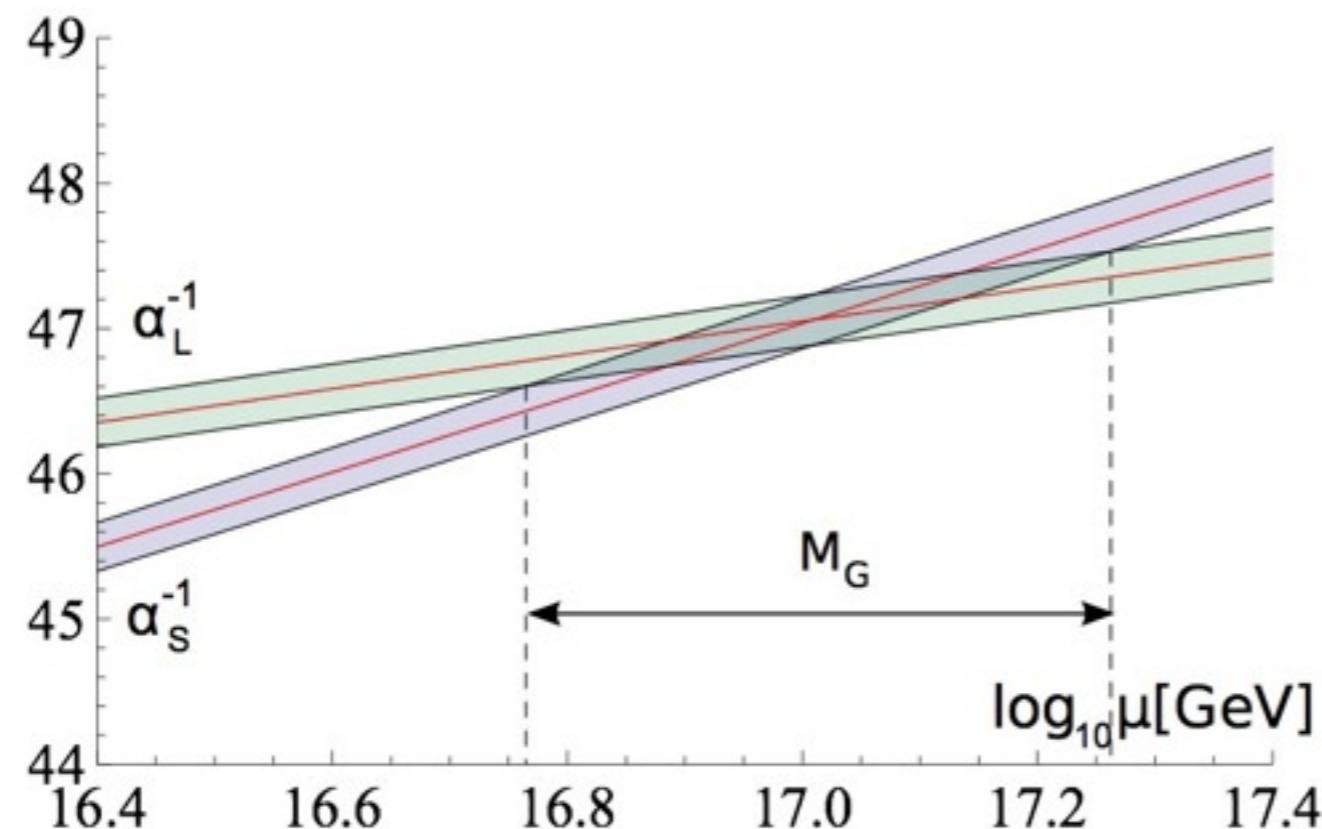
■ Flavor structure of the B & L violating currents

- Yukawa sector fits
- Planck-scale effects
 - scalar & fermionic kinetic forms = matching
 - higher-order operators

Main theoretical uncertainties in p-decay estimates

GUT scale determination

- at least **two-loop** running necessary!

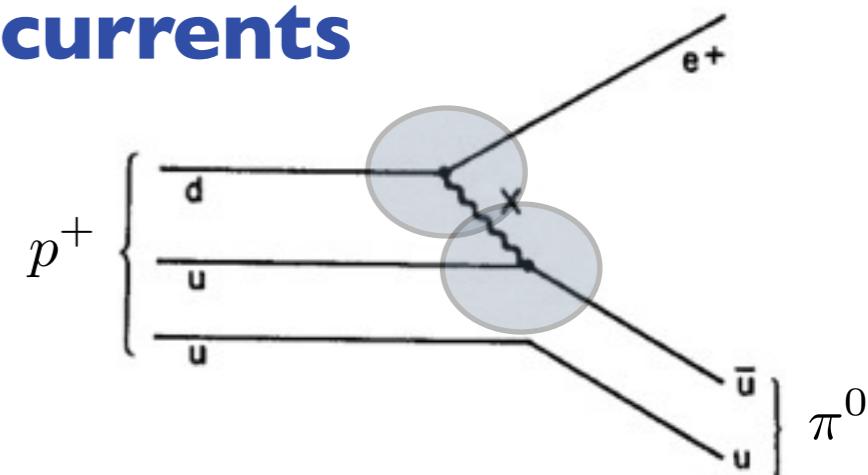


Credit: H. Kolesova

- requires a **very good** understanding of the **entire** spectrum

Main theoretical uncertainties in p-decay estimates

Flavour structure of the BLNV currents



Example:

$$\frac{g^2}{M_{1/6}^2} C_{ijk} \bar{u}^c \gamma^\mu d_i \bar{d}_j^c \gamma_\mu \nu_k$$

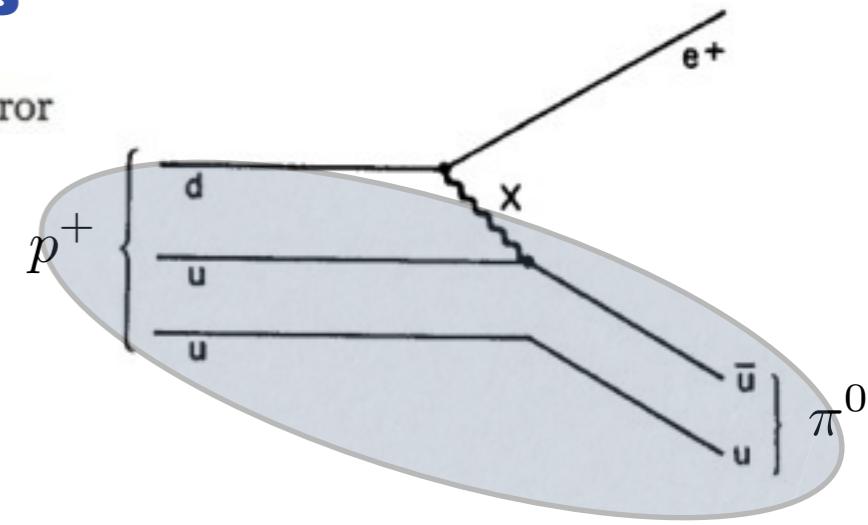
$$C_{ijk} = (V_{d^c}^\dagger V_d)_{ji} (V_{u^c}^\dagger V_\nu)_{1k}$$

- RH rotations enter here
- simple Yukawa sector desirable!
- some channels are more “robust” than others

Main theoretical uncertainties in p-decay estimates

Hadronic matrix elements

Matrix element $W_0(\mu = 2\text{GeV}) \text{ GeV}^2$	(%)	Total error
$\langle \pi^0 (ud)_R u_L p \rangle$ -0.103 (23) (34)	40	
$\langle \pi^0 (ud)_L u_L p \rangle$ 0.133 (29) (28)	30	
$\langle \pi^+ (ud)_R d_L p \rangle$ -0.146 (33) (48)	40	
$\langle \pi^+ (ud)_L d_L p \rangle$ 0.188 (41) (40)	30	
$\langle K^0 (us)_R u_L p \rangle$ 0.098 (15) (12)	20	
$\langle K^0 (us)_L u_L p \rangle$ 0.042 (13) (8)	36	
$\langle K^+ (us)_R d_L p \rangle$ -0.054 (11) (9)	26	
$\langle K^+ (us)_L d_L p \rangle$ 0.036 (12) (7)	39	
$\langle K^+ (ud)_R s_L p \rangle$ -0.093 (24) (18)	32	
$\langle K^+ (ud)_L s_L p \rangle$ 0.111 (22) (16)	25	
$\langle K^+ (ds)_R u_L p \rangle$ -0.044 (12) (5)	30	
$\langle K^+ (ds)_L u_L p \rangle$ -0.076 (14) (9)	22	
$\langle \eta (ud)_R u_L p \rangle$ 0.015 (14) (17)	147	
$\langle \eta (ud)_L u_L p \rangle$ 0.088 (21) (16)	30	



Y.Aoki, E. Shintani, A. Soni, Phys.Rev. D89 (2014) 014505 (lattice)

Main theoretical uncertainties in p-decay estimates

“Gravity smearing” effects

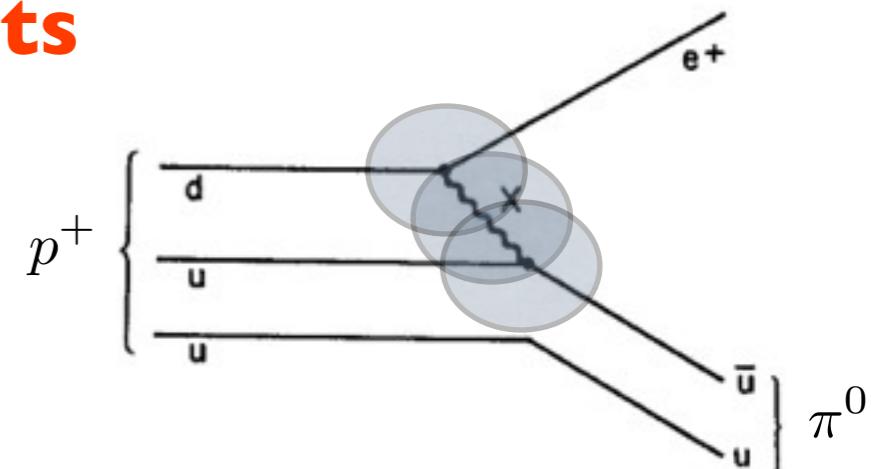
Larsen, Wilczek, NPB 458, 249 (1996)

G. Veneziano, JHEP 06 (2002) 051

Calmet, Hsu, Reeb, PRD 77, 125015 (2008)

G. Dvali, Fortsch. Phys. 58 (2010) 528-536

$$\mathcal{L} \ni \frac{\kappa}{\Lambda} F^{\mu\nu} \langle \Phi \rangle F_{\mu\nu}$$



Main theoretical uncertainties in p-decay estimates

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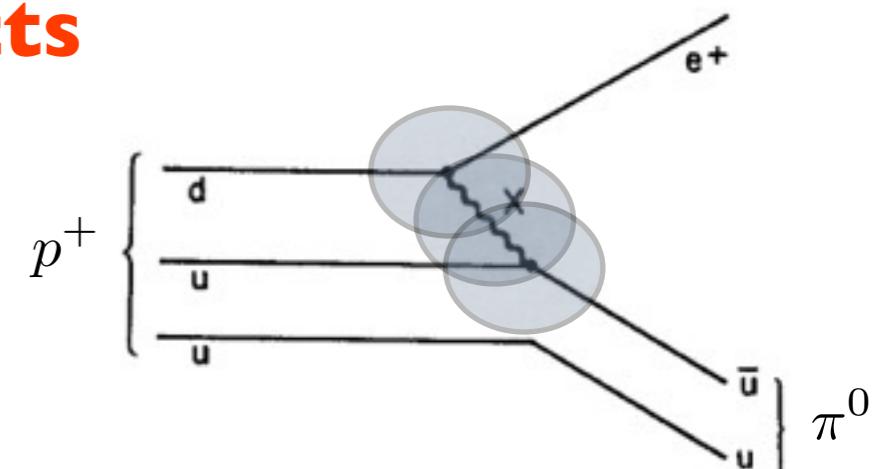
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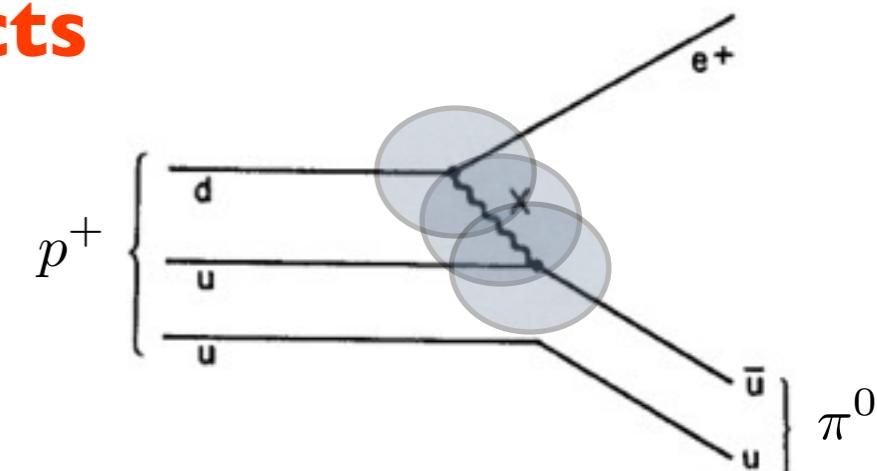
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Main theoretical uncertainties in p-decay estimates

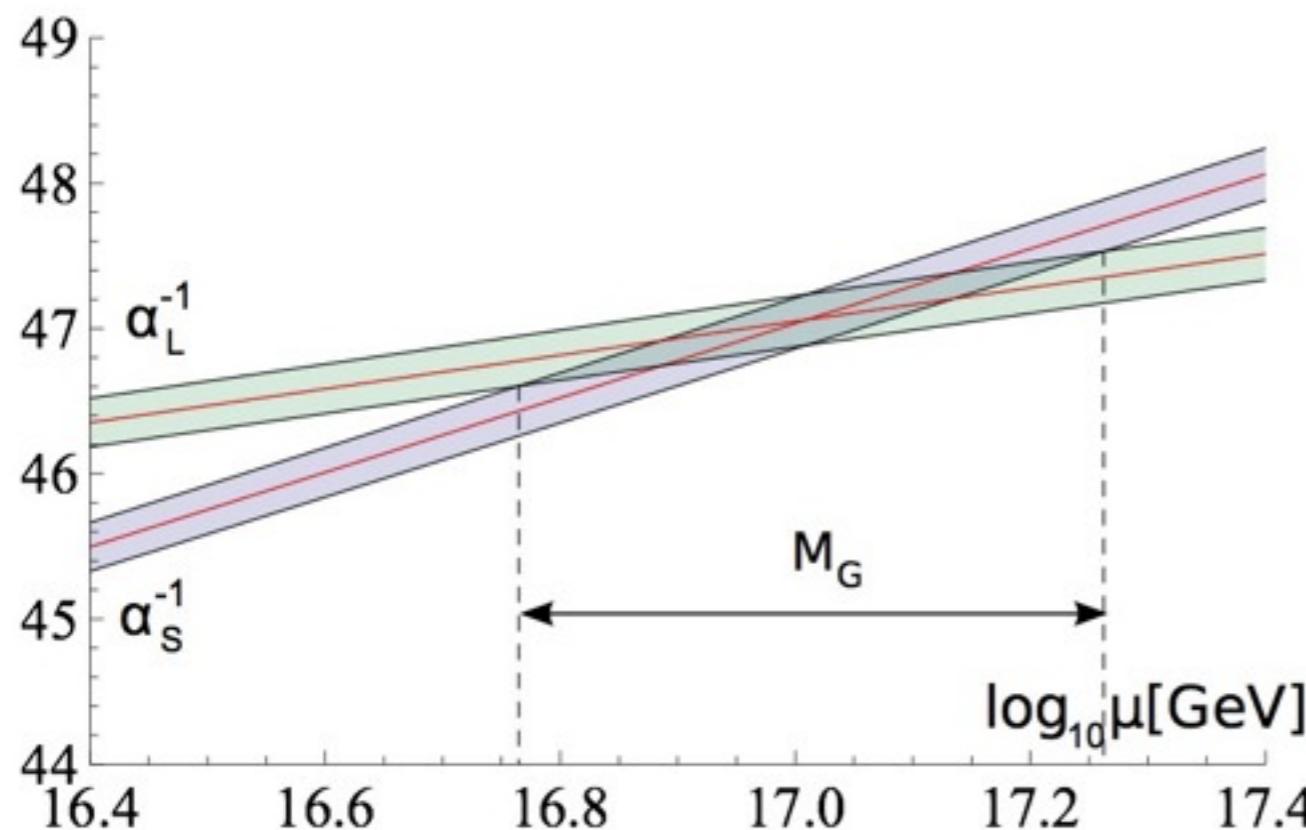
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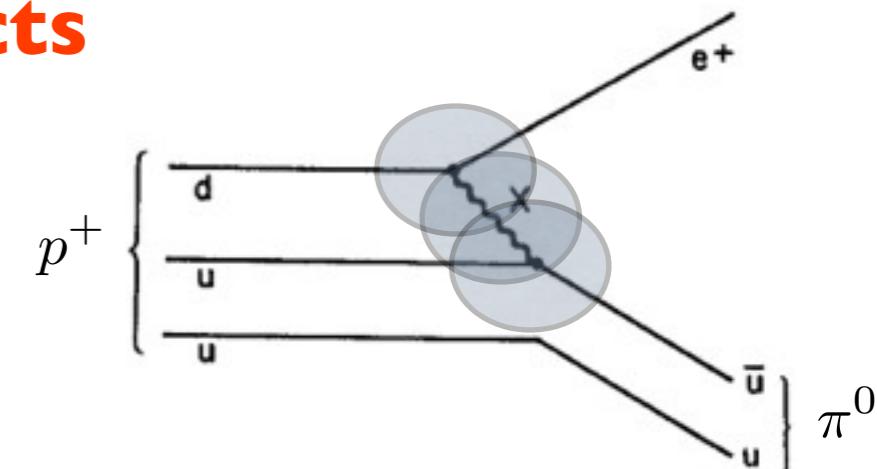


Main theoretical uncertainties in p-decay estimates

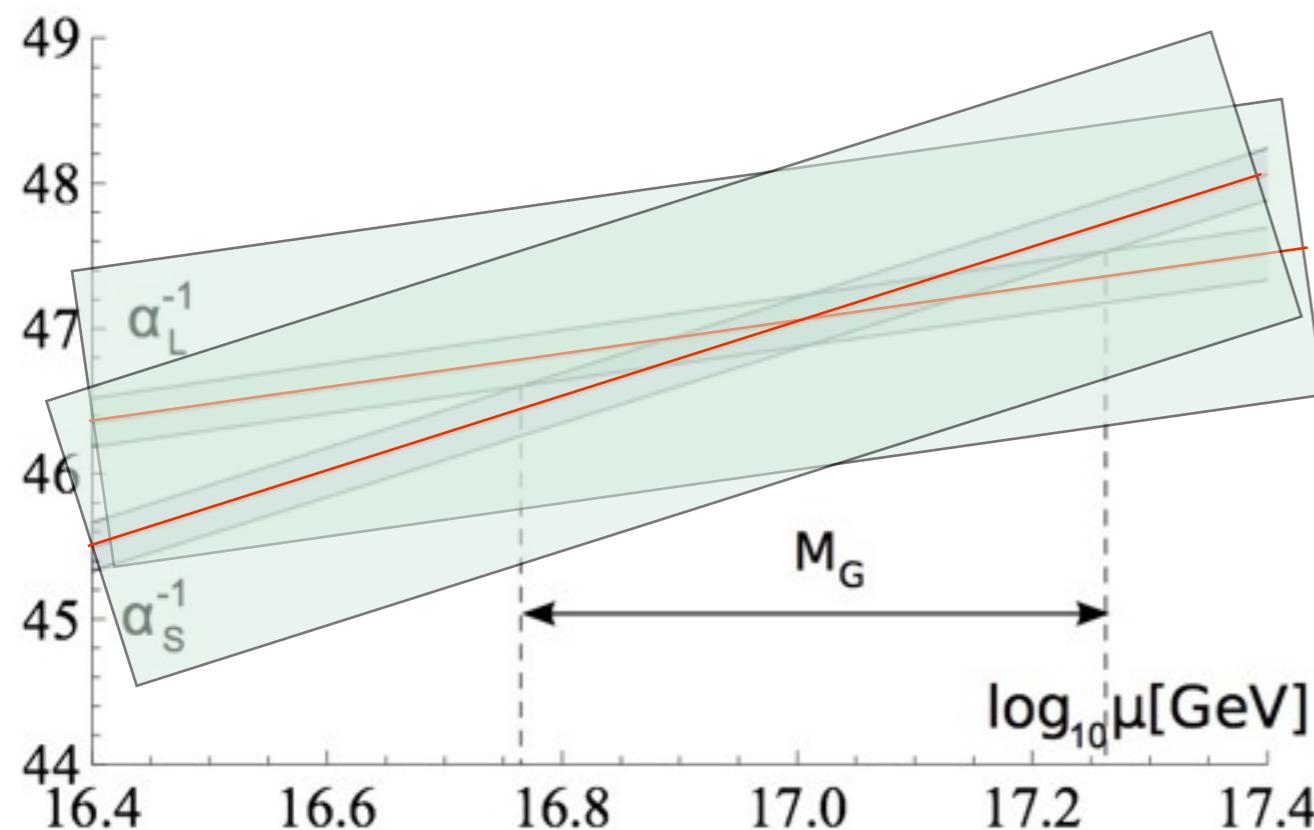
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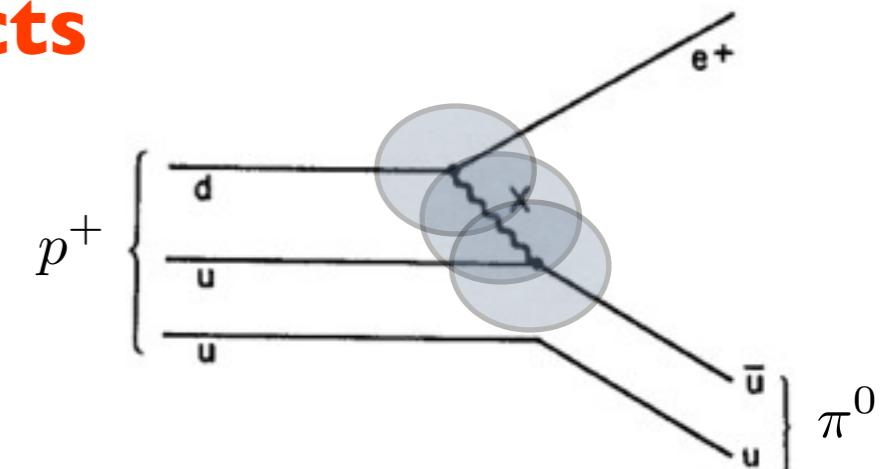
in principle orders
of magnitude uncertainty in M_G !

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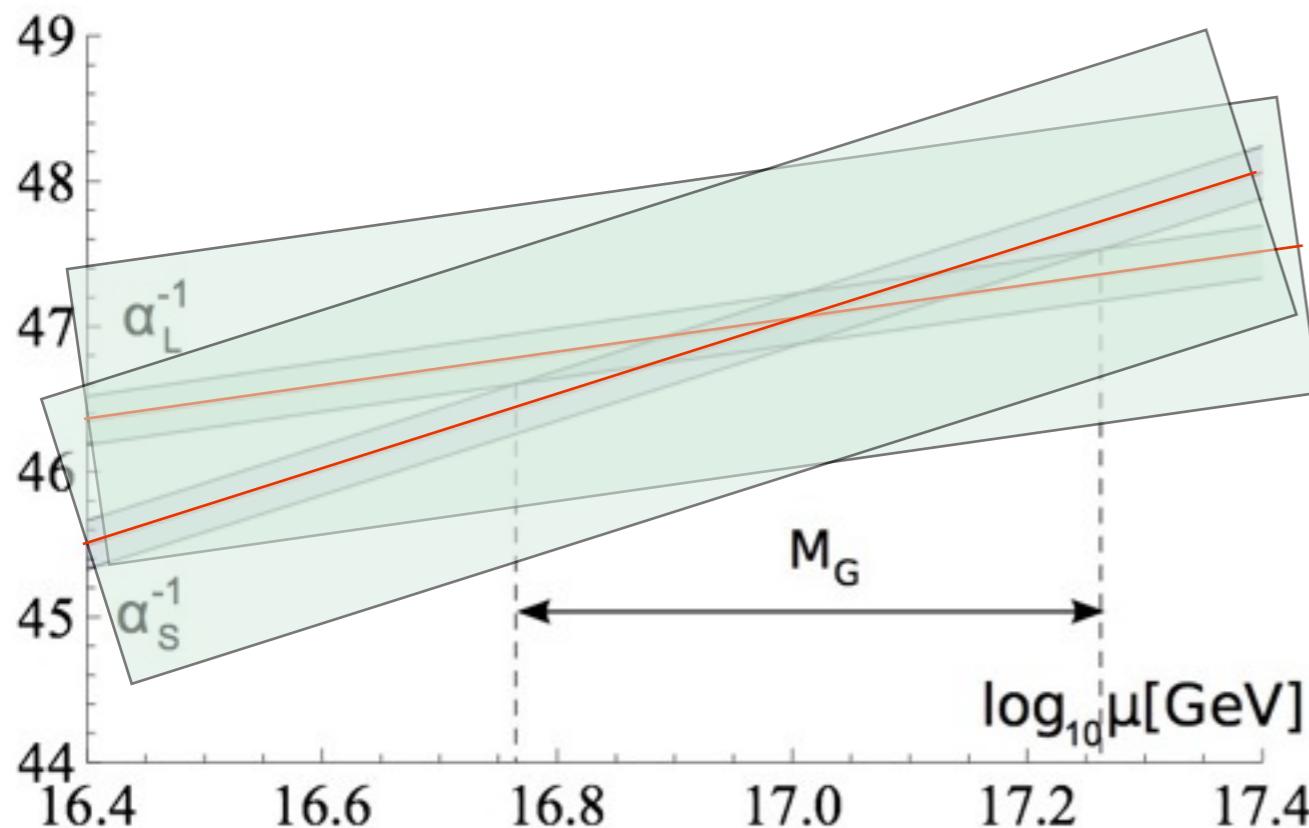
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- uncontrolled + **inhomogeneous** shifts in the gauge matching, $\Delta \alpha_i^{-1} \sim 1$



in principle orders
of magnitude uncertainty in M_G !

**No point in trying @ NLO
without taming these!!!**

What to do about the Planck-scale effects (in matching)?

$$\mathcal{L} \ni \frac{\kappa}{\Lambda} F^{\mu\nu} \langle \Phi \rangle F_{\mu\nu}$$

- absent @ d=5 if, e.g., Φ is not in $(Adj. \otimes Adj.)_{sym}$

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SU(5) GUTs:

$$(24 \otimes 24)_{sym} = 24 \oplus 75 \oplus 200$$

not many options - the rank should not get reduced...

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SU(5) GUTs:

$$(24 \otimes 24)_{sym} = 24 \oplus 75 \oplus 200$$

not many options - the rank should not get reduced...

SO(10) GUTs:

$$(45 \otimes 45)_{sym} = 54 \oplus 210 \oplus 770$$

these, however, are the “usual” choices (**though not minimal**)...

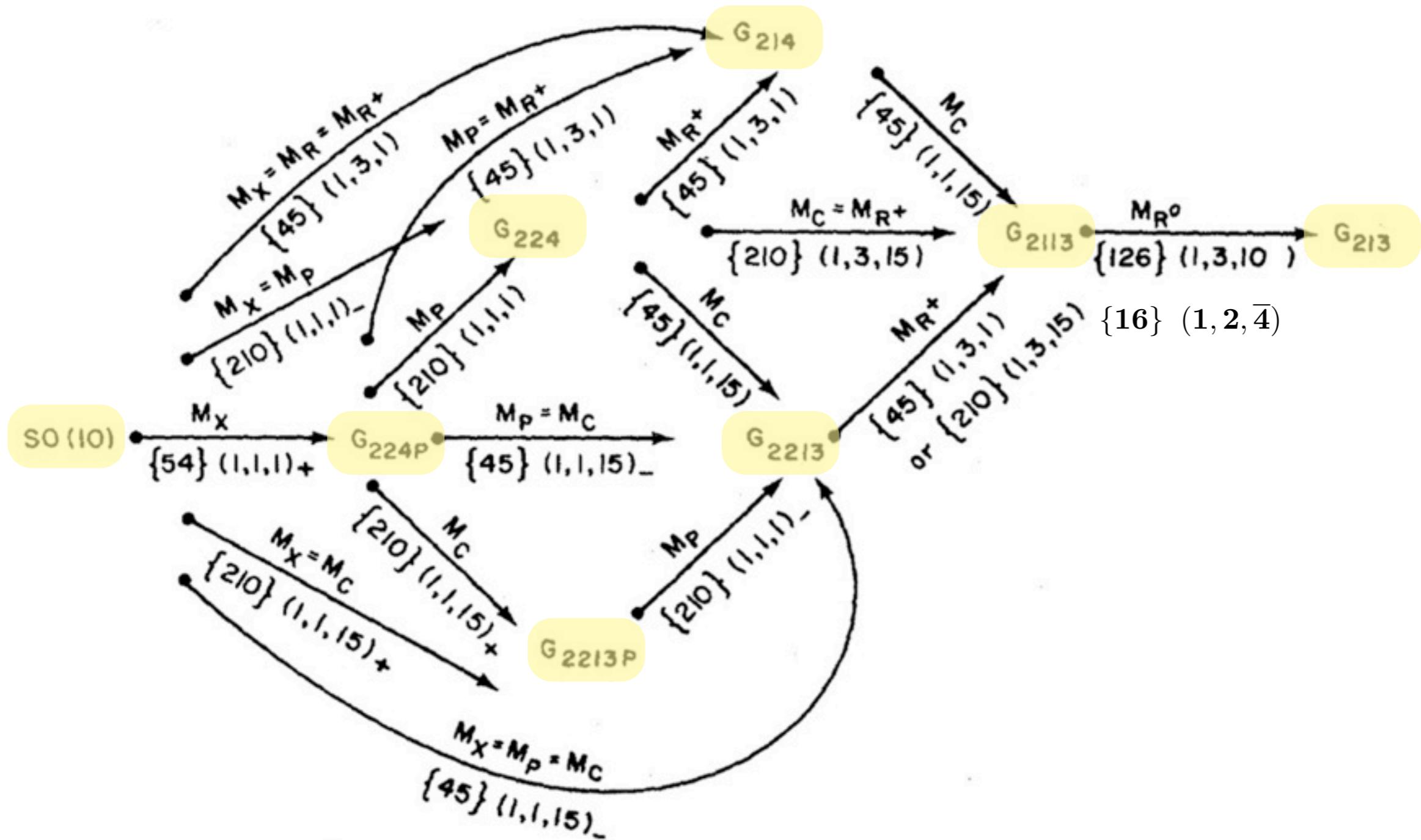
Minimal “reasonably calculable” unifications

The minimal SO(10) GUT

The minimal SO(10) Higgs model

Chang, Mohapatra, Gipson, Marshak, Parida 1985

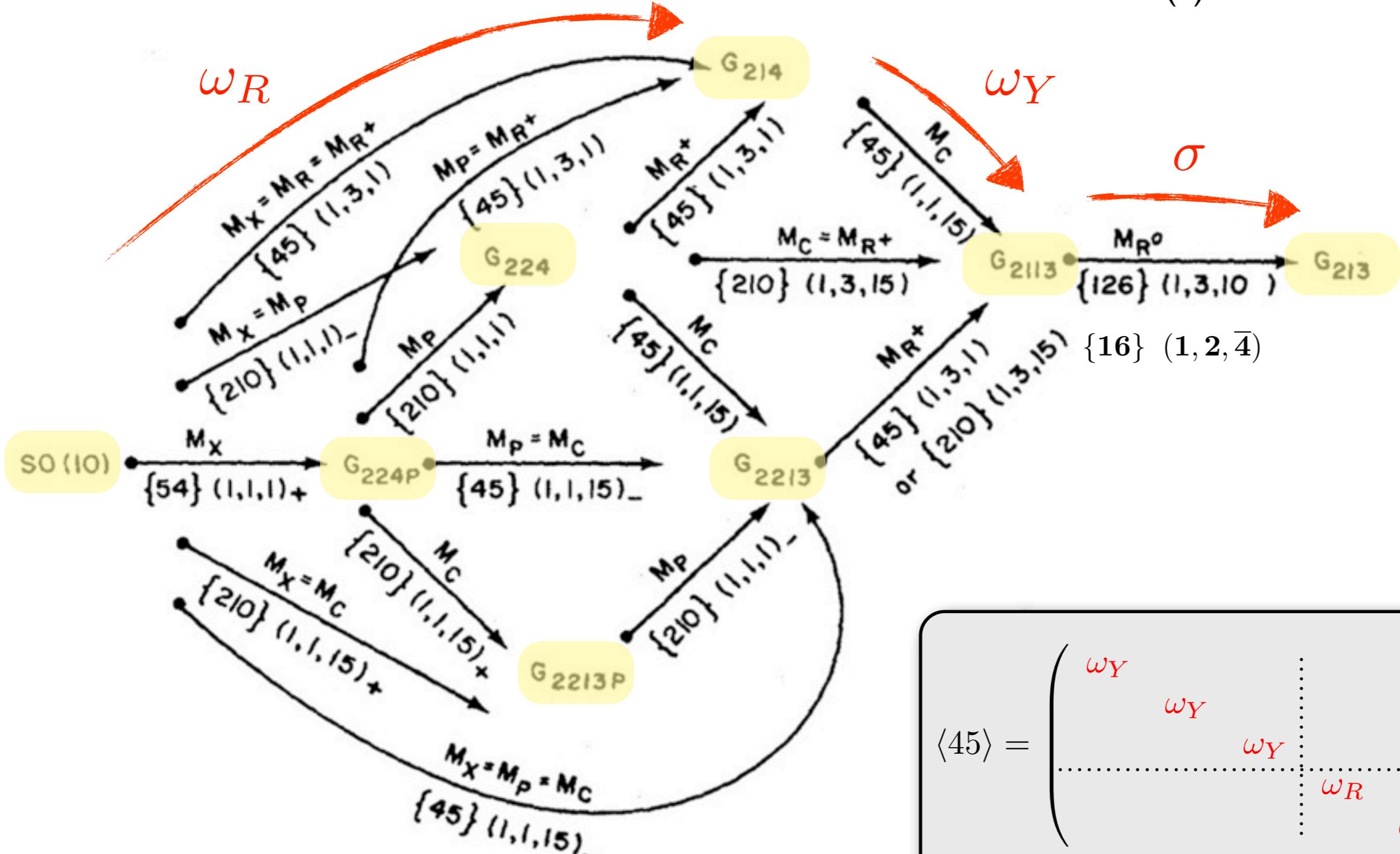
SU(5) branches omitted



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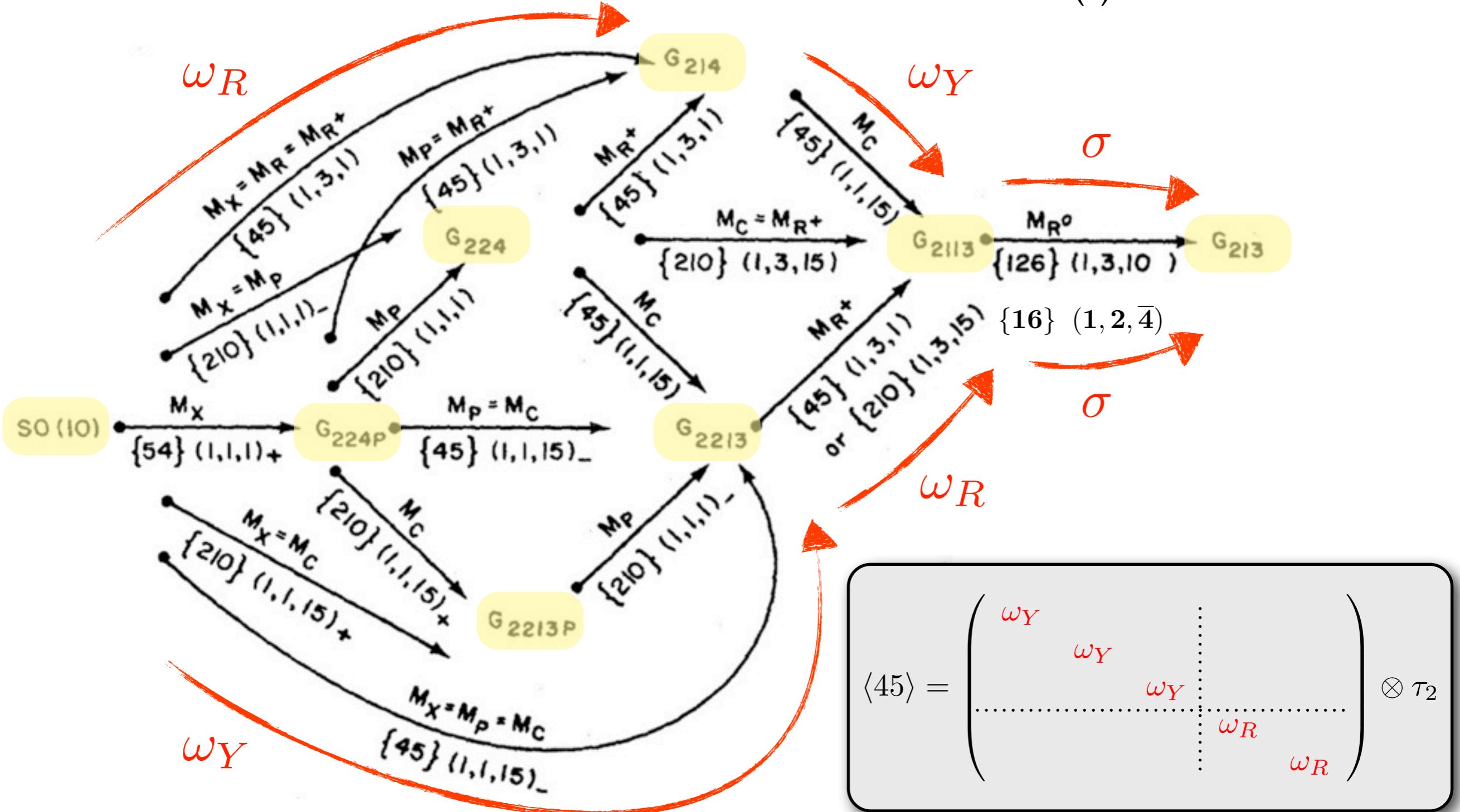


$$\langle 45 \rangle = \begin{pmatrix} \omega_Y & & & & \\ & \omega_Y & & & \\ & & \ddots & & \\ & & & \omega_Y & \\ & & & & \omega_R \end{pmatrix} \otimes \tau_2$$

The minimal SO(10) Higgs model

Chang, Mohapatra, Gipson, Marshak, Parida 1985

SU(5) branches omitted



Taming Planck effects in gauge matching in minimal SO(10)

$$\mathcal{L} \ni \frac{\kappa}{\Lambda} F^{\mu\nu} \langle 45 \rangle F_{\mu\nu} = 0$$

The leading Planck-scale effects in gauge matching
absent from SO(10) GUTs broken by 45!

The minimal SO(10) Higgs model

SO(10) broken by 45, rank reduced by 126

Scalar potential: $V = V_{45} + V_{126} + V_{\text{mix}}$

$$V_{45} = -\frac{\mu^2}{2}(\phi\phi)_0 + \frac{a_0}{4}(\phi\phi)_0(\phi\phi)_0 + \frac{a_2}{4}(\phi\phi)_2(\phi\phi)_2,$$

$$\begin{aligned} V_{126} = & -\frac{\nu^2}{5!}(\Sigma\Sigma^*)_0 \\ & + \frac{\lambda_0}{(5!)^2}(\Sigma\Sigma^*)_0(\Sigma\Sigma^*)_0 + \frac{\lambda_2}{(4!)^2}(\Sigma\Sigma^*)_2(\Sigma\Sigma^*)_2 \\ & + \frac{\lambda_4}{(3!)^2(2!)^2}(\Sigma\Sigma^*)_4(\Sigma\Sigma^*)_4 + \frac{\lambda'_4}{(3!)^2}(\Sigma\Sigma^*)_{4'}(\Sigma\Sigma^*)_{4'} \\ & + \frac{\eta_2}{(4!)^2}(\Sigma\Sigma)_2(\Sigma\Sigma)_2 + \frac{\eta_2^*}{(4!)^2}(\Sigma^*\Sigma^*)_2(\Sigma^*\Sigma^*)_2, \end{aligned}$$

$$\begin{aligned} V_{\text{mix}} = & \frac{i\tau}{4!}(\phi)_2(\Sigma\Sigma^*)_2 + \frac{\alpha}{2 \cdot 5!}(\phi\phi)_0(\Sigma\Sigma^*)_0 \\ & + \frac{\beta_4}{4 \cdot 3!}(\phi\phi)_4(\Sigma\Sigma^*)_4 + \frac{\beta'_4}{3!}(\phi\phi)_{4'}(\Sigma\Sigma^*)_{4'} \\ & + \frac{\gamma_2}{4!}(\phi\phi)_2(\Sigma\Sigma)_2 + \frac{\gamma_2^*}{4!}(\phi\phi)_2(\Sigma^*\Sigma^*)_2. \end{aligned}$$

- $(\phi\phi)_0(\phi\phi)_0 \equiv \phi_{ij}\phi_{ij}\phi_{kl}\phi_{kl}$
- $(\phi\phi)_2(\phi\phi)_2 \equiv \phi_{ij}\phi_{ik}\phi_{lj}\phi_{lk}$
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- $(\Sigma\Sigma^*)_4(\Sigma\Sigma^*)_4 \equiv \Sigma_{ijklm}\Sigma_{ijkno}^*\Sigma_{pqrlm}\Sigma_{pqrn}^*$
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- $(\Sigma\Sigma)_2(\Sigma\Sigma)_2 \equiv \Sigma_{ijklm}\Sigma_{ijkln}\Sigma_{opqrm}\Sigma_{opqrn}$
- $(\phi)_2(\Sigma\Sigma^*)_2 \equiv \phi_{ij}\Sigma_{klmnij}\Sigma_{klmnj}^*$
- $(\phi\phi)_0(\Sigma\Sigma^*)_0 \equiv \phi_{ij}\phi_{ij}\Sigma_{klmno}\Sigma_{klmno}^*$
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- $(\phi\phi)_{4'}(\Sigma\Sigma^*)_{4'} \equiv \phi_{ij}\phi_{kl}\Sigma_{mnoik}\Sigma_{mnojl}^*$
- $(\phi\phi)_2(\Sigma\Sigma)_2 \equiv \phi_{ij}\phi_{ik}\Sigma_{lmnoj}\Sigma_{lmnok}$
- $(\phi\phi)_2(\Sigma^*\Sigma^*)_2 \equiv \phi_{ij}\phi_{ik}\Sigma_{lmnoj}^*\Sigma_{lmnok}^*$

The minimal SO(10) Higgs model ~~nightmare~~

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The minimal SO(10) Higgs model ~~model~~^{nightmare}

“Ruled out” in 1980’s

$$\begin{aligned} m_{(8,1,0)}^2 &= 2a_2(\omega_R - \omega_Y)(\omega_R + 2\omega_Y) \\ m_{(1,3,0)}^2 &= 2a_2(\omega_Y - \omega_R)(\omega_Y + 2\omega_R) \end{aligned}$$

Yasuè 1981, Anastaze, Derendinger, Buccella 1983, Babu, Ma 1985

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Aaarrgggh... tachyonic spectrum unless $\frac{1}{2} < |\omega_Y/\omega_R| < 2$



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SU(5)-like vacua only, not far from the “SM running”!

The minimal SO(10) Higgs model ~~model~~^{nightmare}

“Ruled out” in 1980’s

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$$m_{(1,3,0)}^2 = 2a_2(\omega_Y - \omega_R)(\omega_Y + 2\omega_R)$$

Yasuè 1981, Anastaze, Derendinger, Buccella 1983, Babu, Ma 1985

Aaarrgggh... tachyonic spectrum unless $\frac{1}{2} < |\omega_Y/\omega_R| < 2$

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The minimal SO(10) Higgs model ~~model~~^{nightmare}

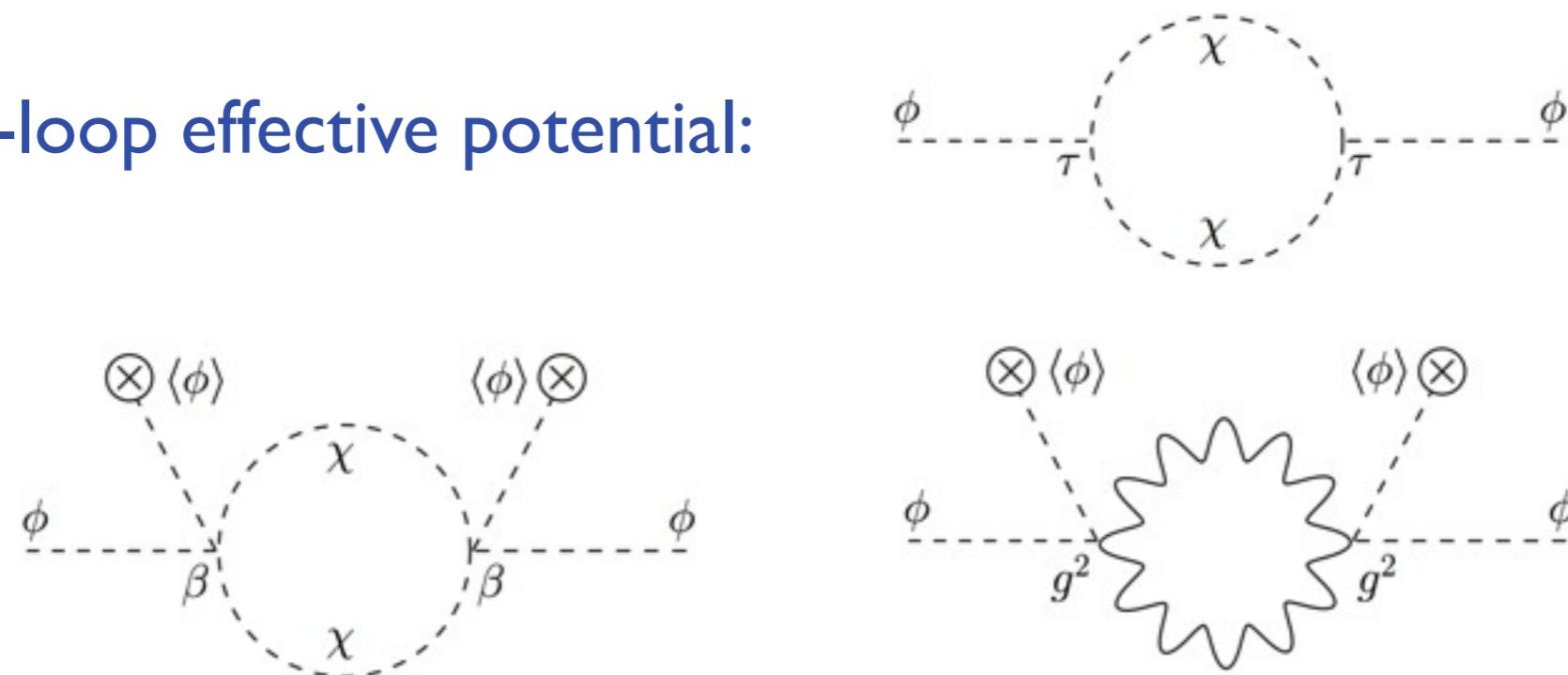
Quantum salvation of the 45-broken SO(10) Higgs model

Bertolini, Di Luzio, MM, PRD 81, 035015 (2010)

The minimal SO(10) Higgs model ~~nightmare~~

Quantum salvation of the 45-broken SO(10) Higgs model

One-loop effective potential:

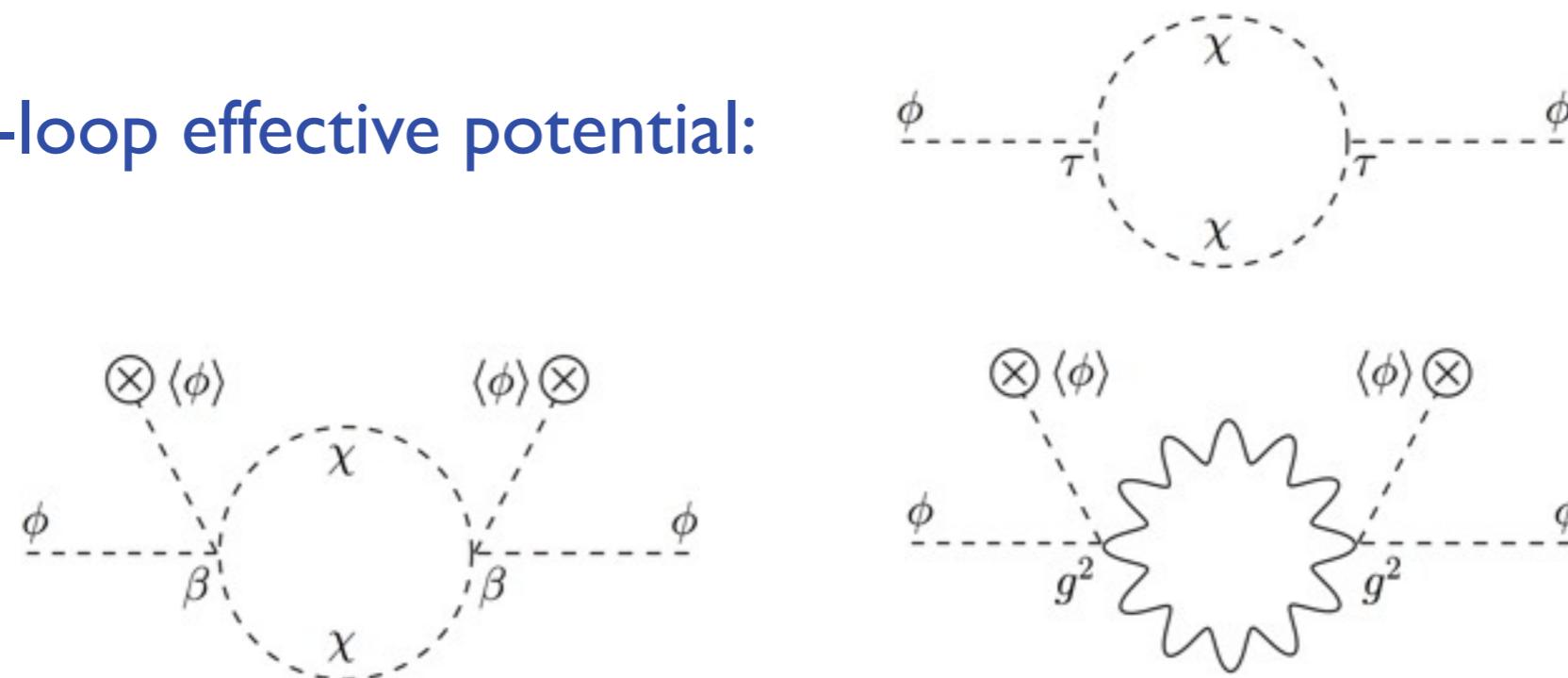


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Quantum salvation of the 45-broken SO(10) Higgs model

One-loop effective potential:



$$\Delta m_{(1,3,0)}^2 = \frac{1}{4\pi^2} [\tau^2 + \beta^2(2\omega_R^2 - \omega_R\omega_Y + 2\omega_Y^2) + g^4 (16\omega_R^2 + \omega_Y\omega_R + 19\omega_Y^2)] + \text{logs},$$

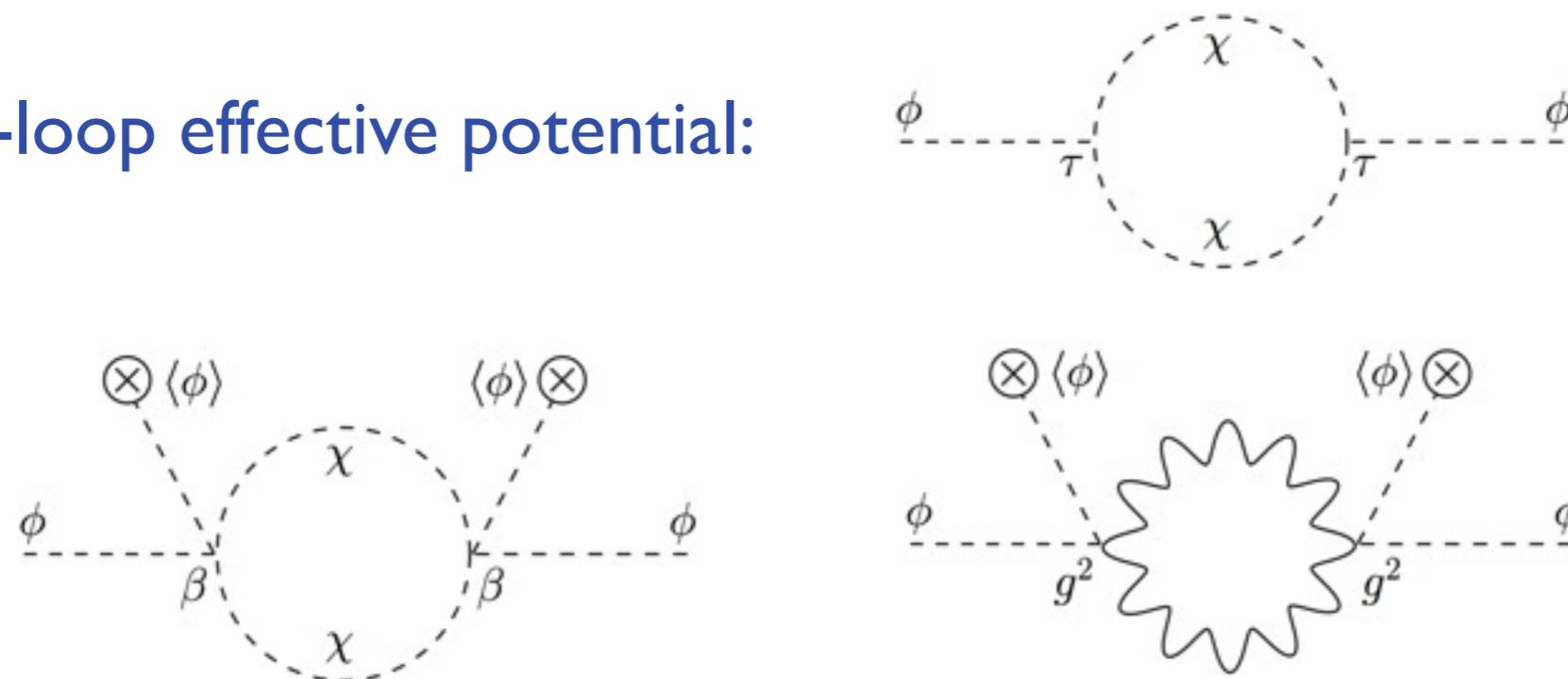
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Bertolini, Di Luzio, MM, PRD 81, 035015 (2010)

The minimal SO(10) Higgs model

Quantum salvation of the 45-broken SO(10) Higgs model

One-loop effective potential:



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Towards a consistent & potentially realistic SO(10) scenario

**“Consistency is the last refuge
of people without imagination”**

Oscar Wilde



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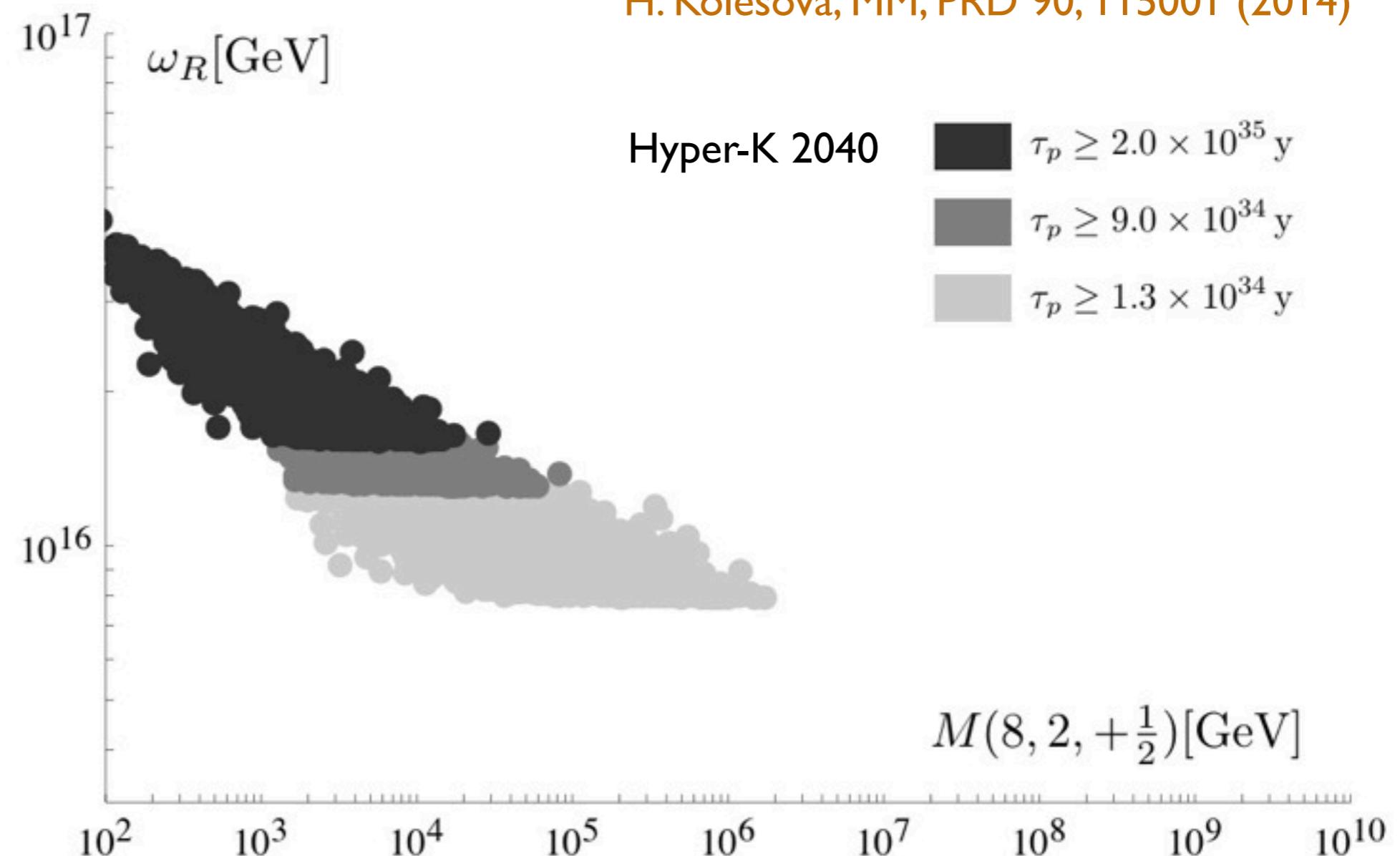


**Two other potentially realistic minimally fine-tuned
& consistent scenarios with “light” scalars in the desert**

Bertolini, Di Luzio, MM, PRD85 095014 2012

Towards a consistent & potentially realistic SO(10) scenario

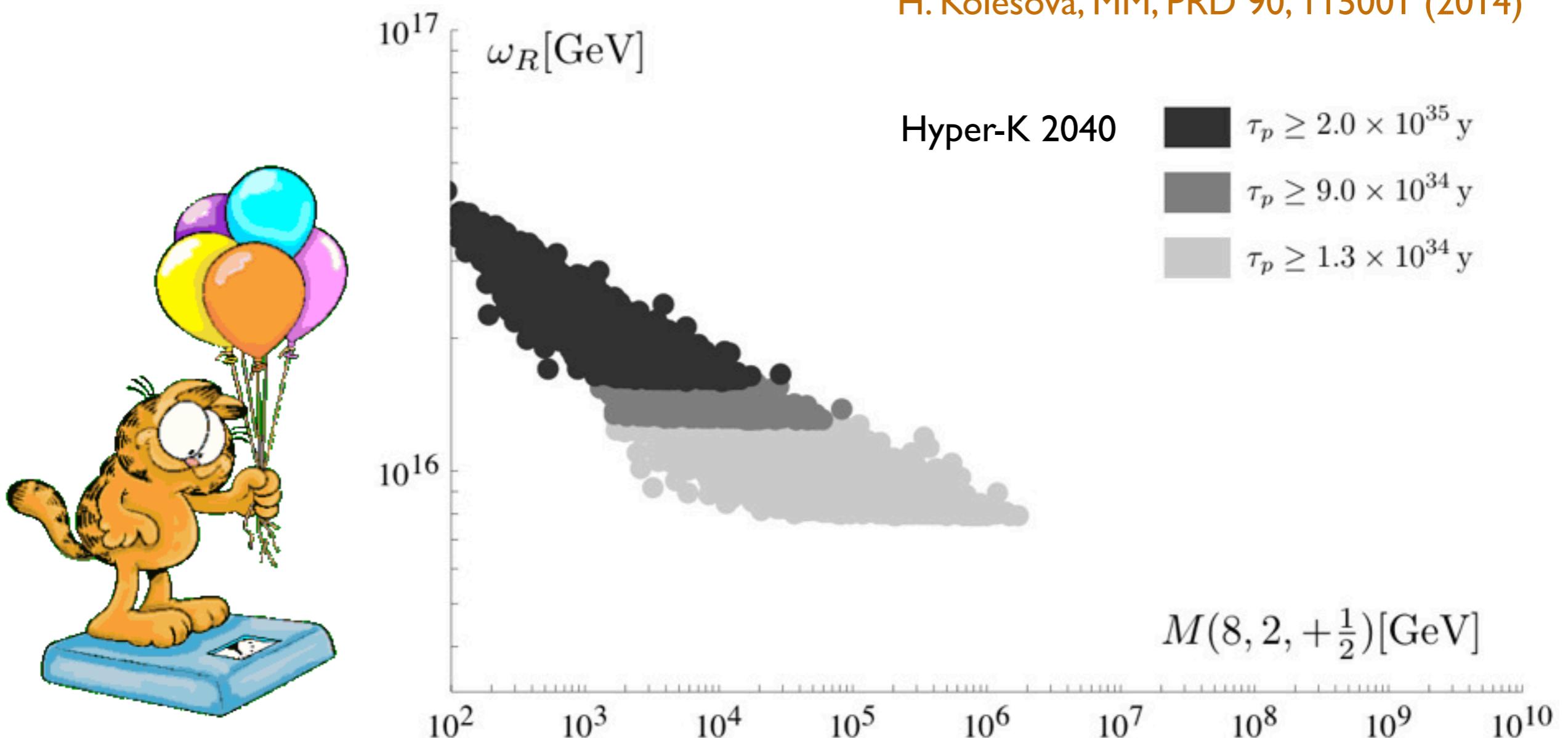
Example: light $(8, 2, +\frac{1}{2})$ @ NLO



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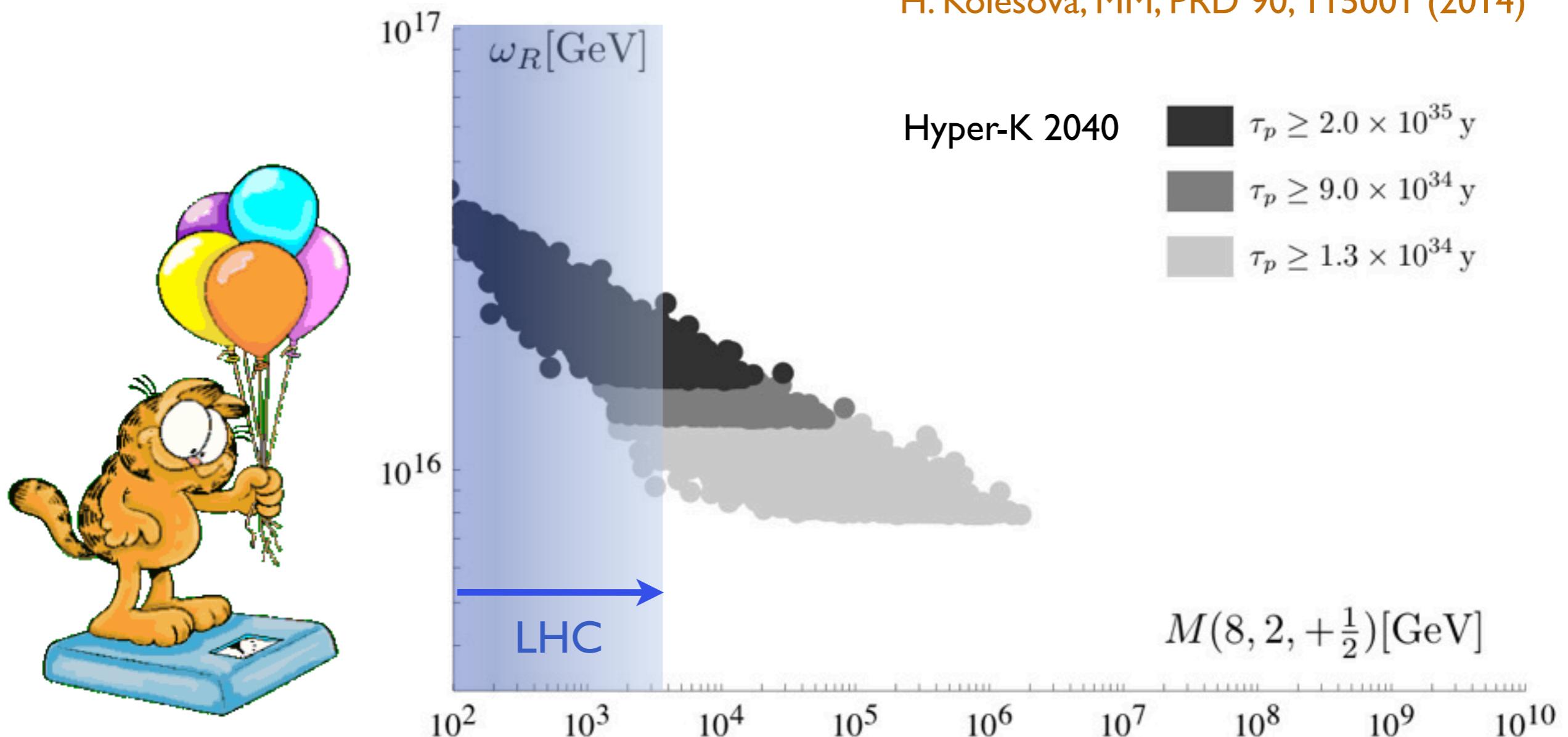
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Bertolini, Di Luzio, MM, PRD 85, 095014 (2012)
H. Kolešová, MM, PRD 90, 115001 (2014)



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Bertolini, Di Luzio, MM, PRD 85, 095014 (2012)
H. Kolešová, MM, PRD 90, 115001 (2014)

Minimal flipped SU(5) UT

a case for radiative neutrino mass generation

A brief flipped SU(5) recap

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$\text{SO}(10)$

\supset

$\text{SU}(5) \times \text{U}(1)_Z$

$$16_M \ni (10, +1)_M \oplus (\bar{5}, -3)_M \oplus (1, +5)_M$$

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X', Y'

A brief flipped SU(5) recap

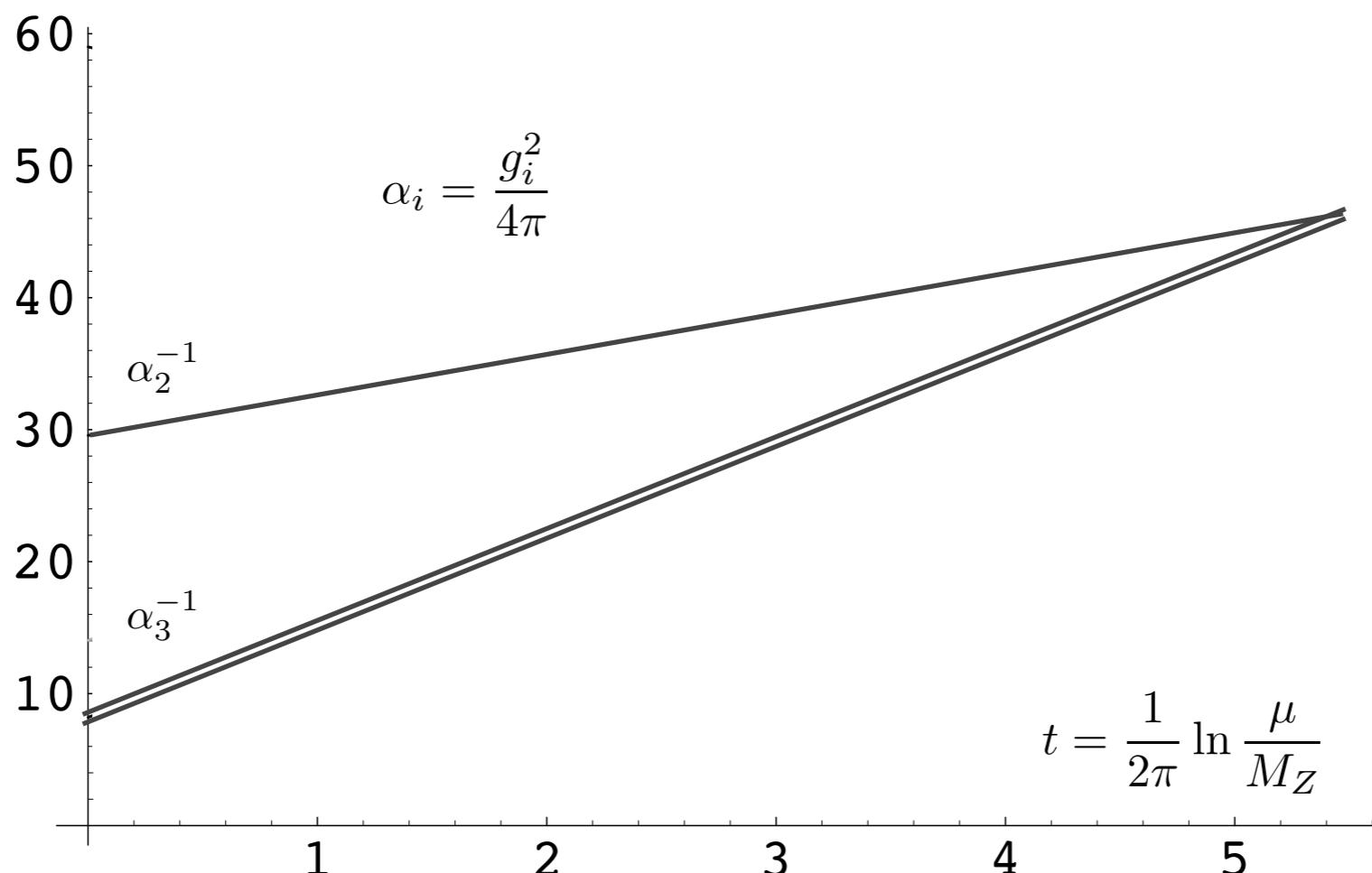
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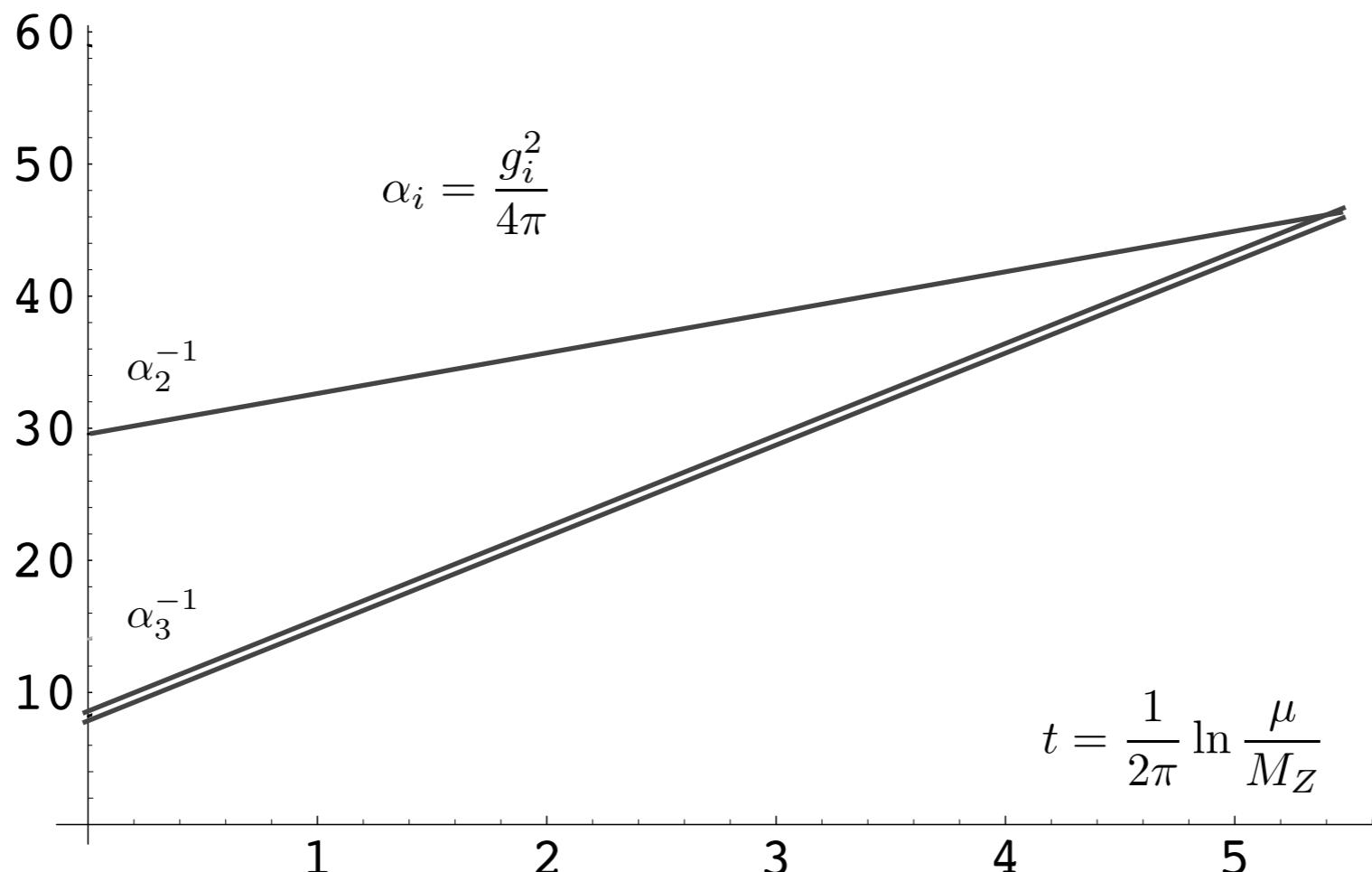
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- monopoles absent

$$\begin{aligned}\pi_2(SU(5) \otimes U(1)/SU(3) \otimes SU(2) \otimes U(1)) \\= \pi_2(SU(5)/SU(3) \otimes SU(2)) \\= \pi_1(SU(3) \otimes SU(2)) = 0\end{aligned}$$

Taming Planck effects in gauge matching in the flipped SU(5)

$$\mathcal{L} \not\ni \frac{\omega}{M_{Pl}} F_{\mu\nu} \langle \Phi \rangle F^{\mu\nu}$$

The leading Planck-scale effects in gauge matching
absent from the flipped SU(5) UT broken by (10,+1)!

The minimal flipped SU(5) flavor structure

rather different from the standard SU(5) one

$$\mathcal{L} \ni Y_{10} 10_M 10_M 5_H + Y_{\bar{5}} 10_M \bar{5}_M 5_H^* + Y_1 \bar{5}_M 1_M 5_H + h.c.$$

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down-quark mass matrix is independent - unlike in SU(5) - and **symmetric!**

$$\Gamma(p \rightarrow K^+ \bar{\nu}) = 0$$

$$\Gamma(p \rightarrow \pi^+ \bar{\nu}) = \frac{m_p}{8\pi f_\pi^2} A_L^2 |\alpha|^2 (1 + D + F)^2 \left(\frac{g_G}{M_G} \right)^4$$

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clearly incomplete: neutrinos massive, but **heavy & Dirac**

The minimal flipped SU(5) flavor structure

50_H usually added to generate RH neutrino masses/seesaw at tree level...

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$$\frac{\Gamma(p \rightarrow \pi^0 e_\alpha^+)}{\Gamma(p \rightarrow \pi^+ \bar{\nu})} = \frac{1}{2} |(V_{CKM})_{11}|^2 |(U_{MNS} \mathcal{U}_\nu)_{\alpha 1}|^2$$

$m_{LL}^\nu = \mathcal{U}_\nu^T D_\nu \mathcal{U}_\nu$ in the up-diagonal basis

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- in this approach \mathcal{U}_ν is an independent structure
- little grip on the charged lepton channels

Witten's loop in the SO(10) GUTs

NEUTRINO MASSES IN THE MINIMAL O(10) THEORY [☆]

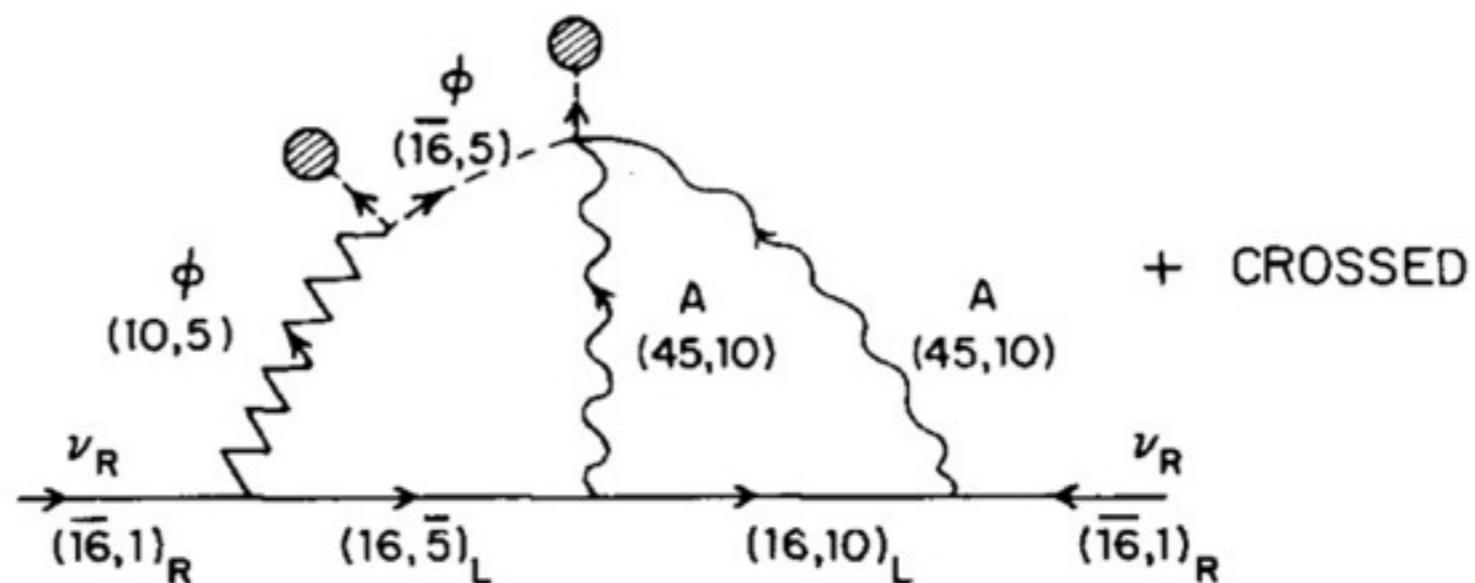
Phys. Lett. B91 (1980) 81

Edward WITTEN ¹

Lyman Laboratory of Physics, Harvard University, Cambridge, MA 02138, USA

Received 6 December 1979

Neutrino masses are discussed in the context of the O(10) grand unified theory. In the “minimal” form of this theory, with minimal Higgs and fermion content, the right-handed neutrinos acquire masses at the two loop level. The left-handed neutrino masses are correspondingly *larger* by a factor roughly $(\alpha/\pi)^{-2}$ than they would be if the right-handed neutrino could acquire mass at the tree level. In the simplest form of this theory, the neutrino mass matrix is proportional to the up quark mass matrix, and the neutrino mixing angles equal the usual Cabibbo angles. The neutrino masses will be roughly in the range $10^{0 \pm 2}$ eV depending on the strength of O(10) symmetry breaking, and on certain unknown ratios of masses and couplings of superheavy particles.



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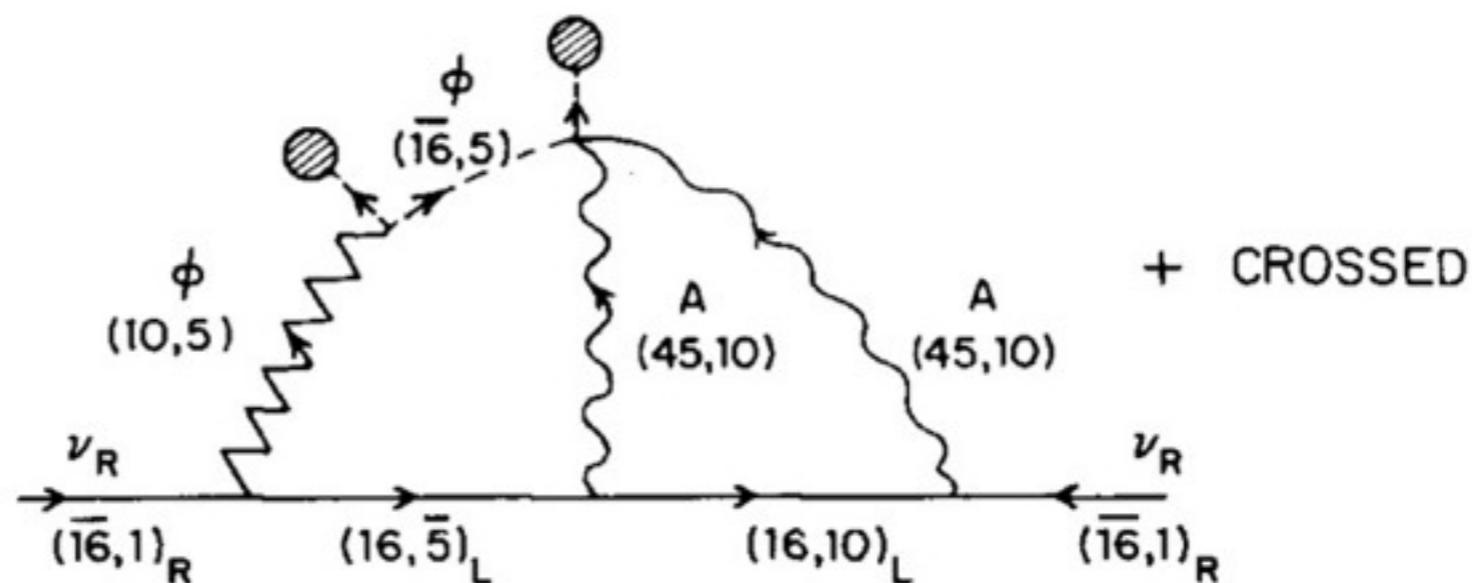
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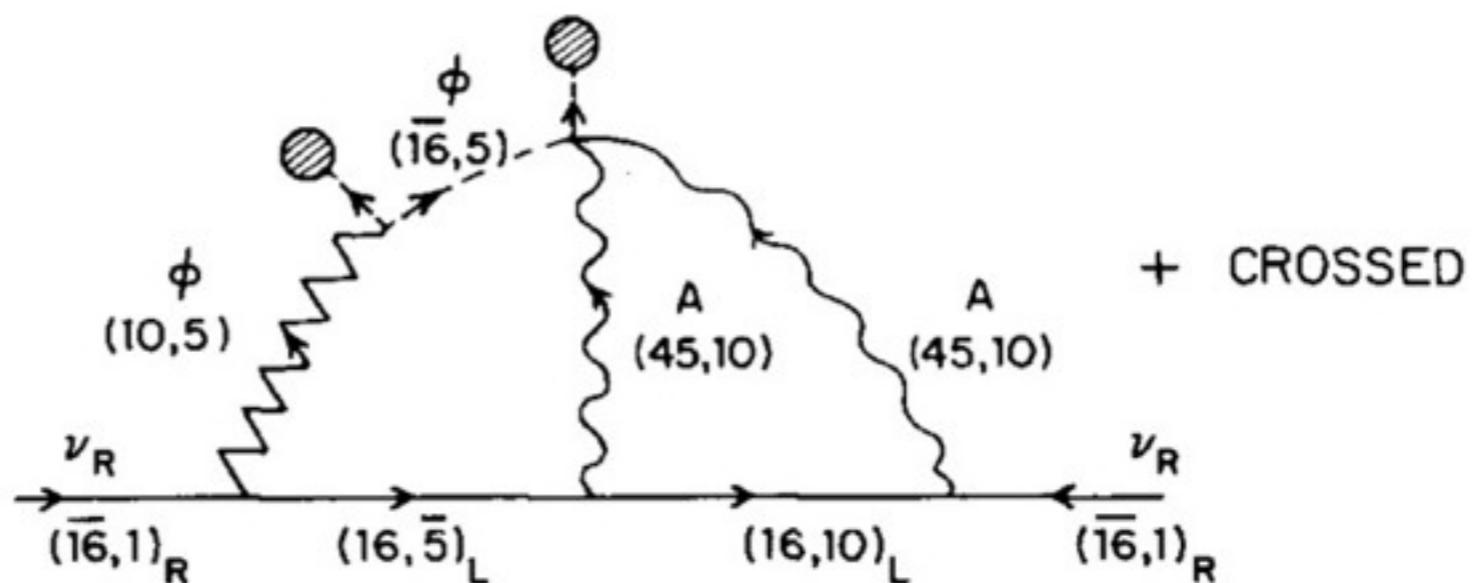
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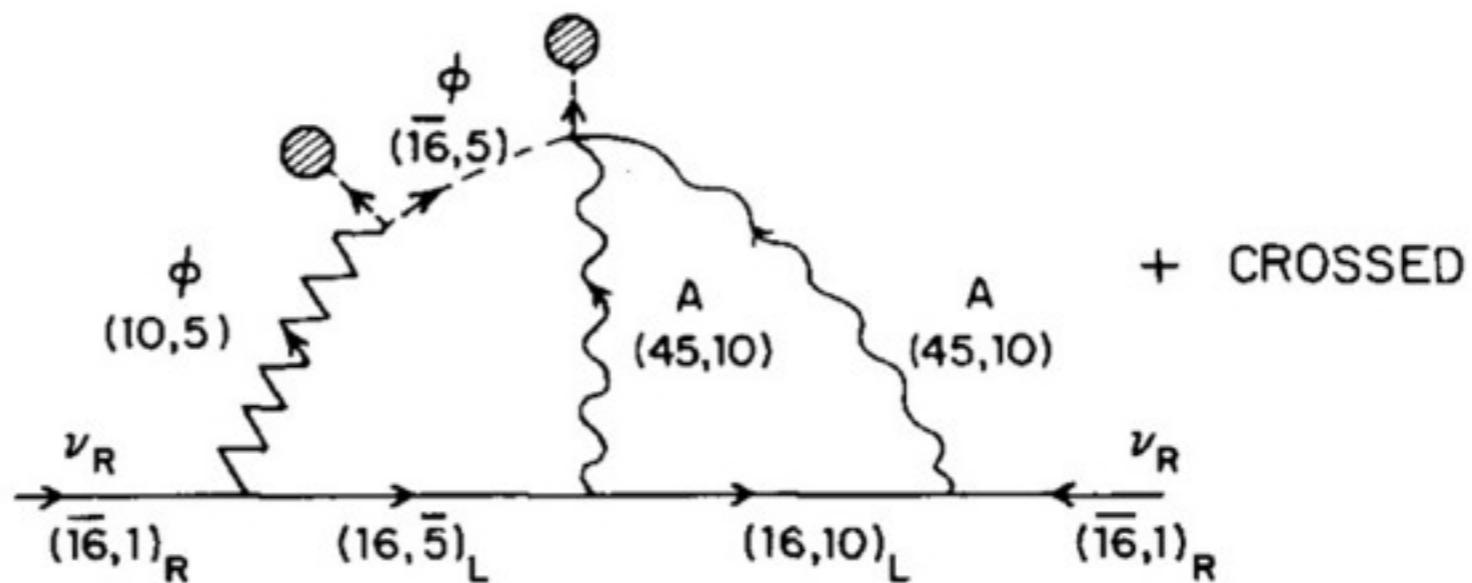
Witten's loop in the SO(10) GUTs

- the structure is pretty unique:

need to mimic 126_H , i.e., 5-index tensor with fields coupled to 16_M

these are 10_H , 45_G , the former has 1 and the latter has 2 indices

$10_H \times 45_G \times 45_G$



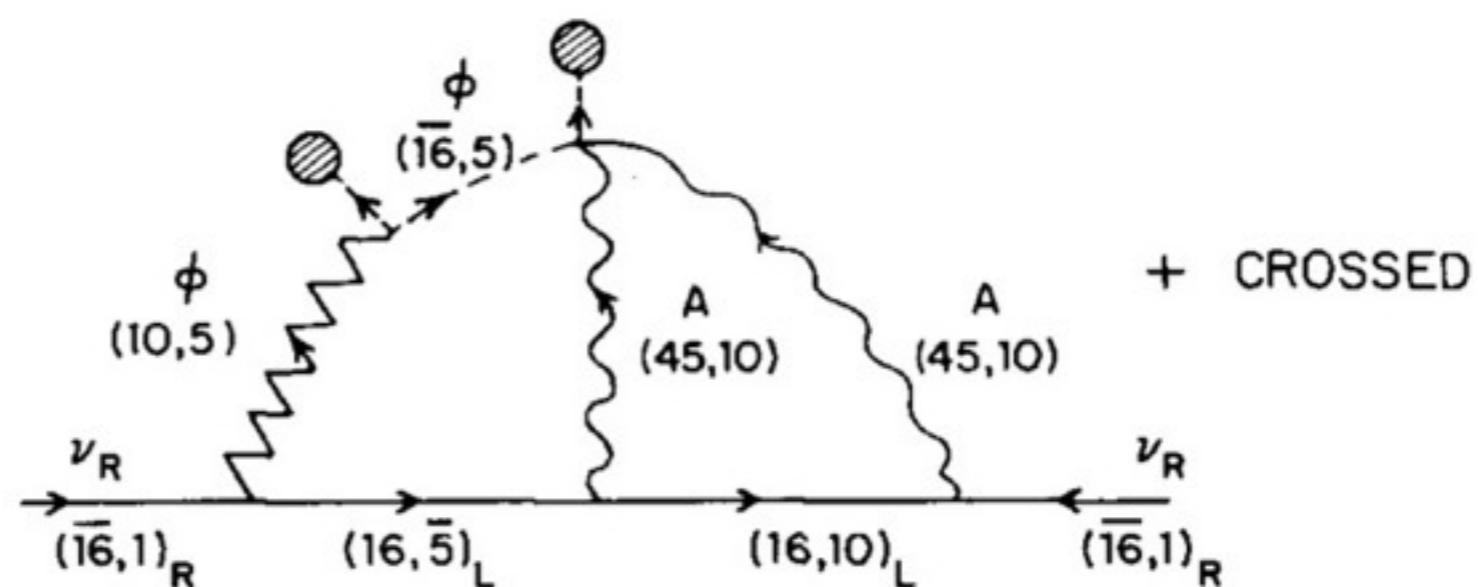
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1980: GUT scale known to be well above 10^{14} GeV
one-step unification OK

mid 1980's: one-step unification failure

TeV-scale SUSY comes to rescue



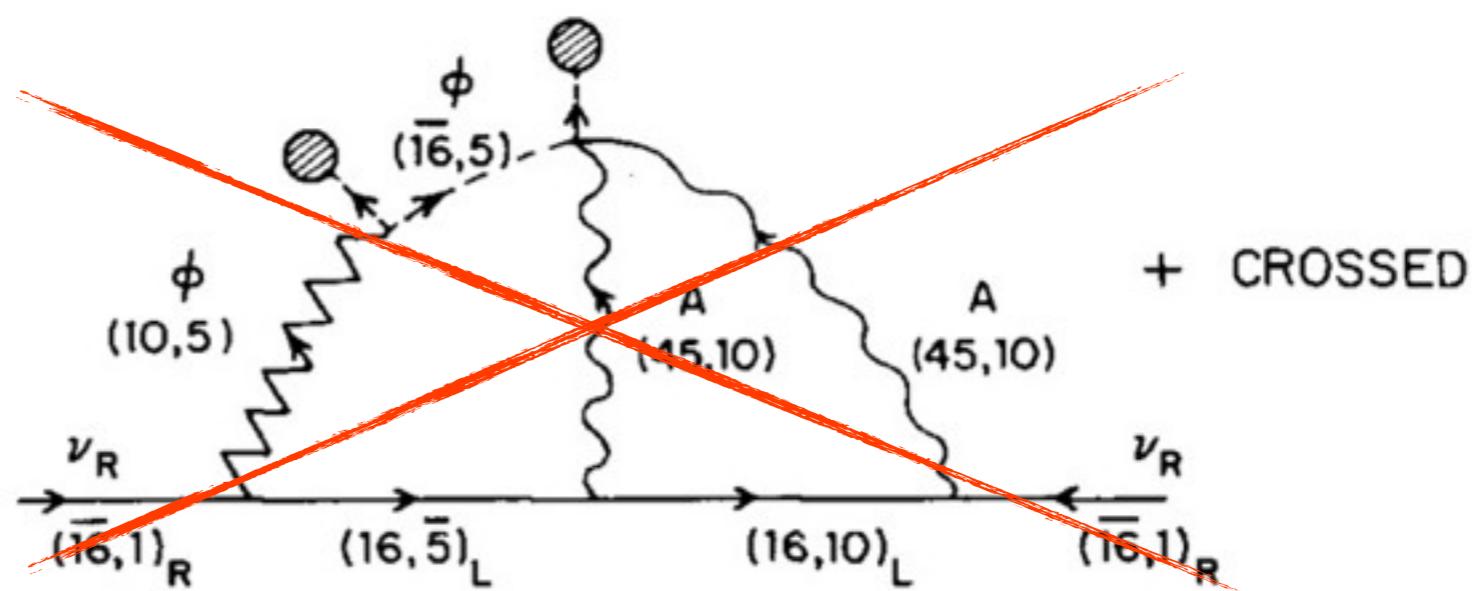
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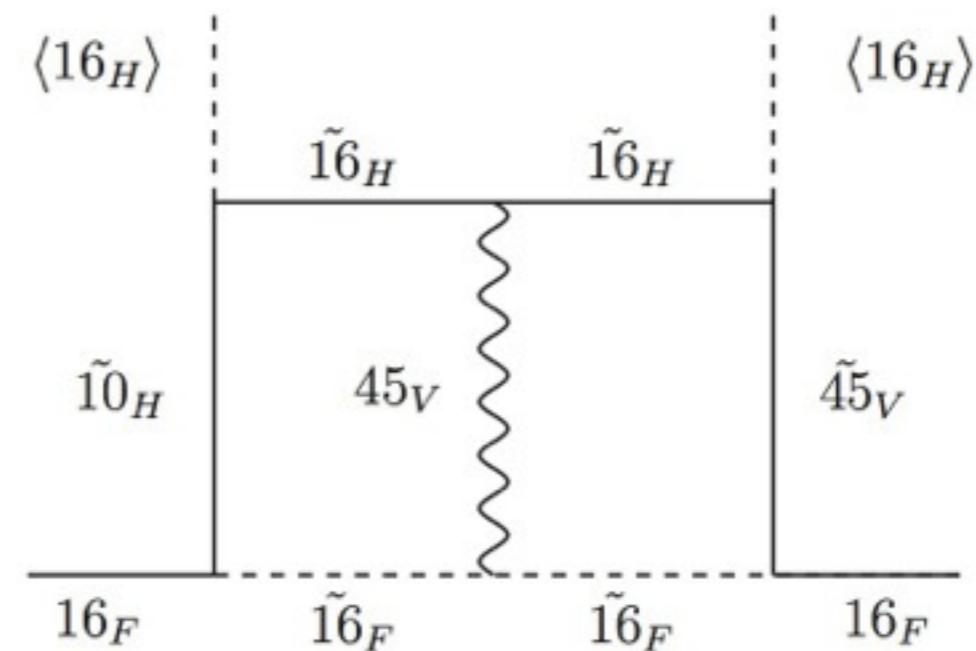
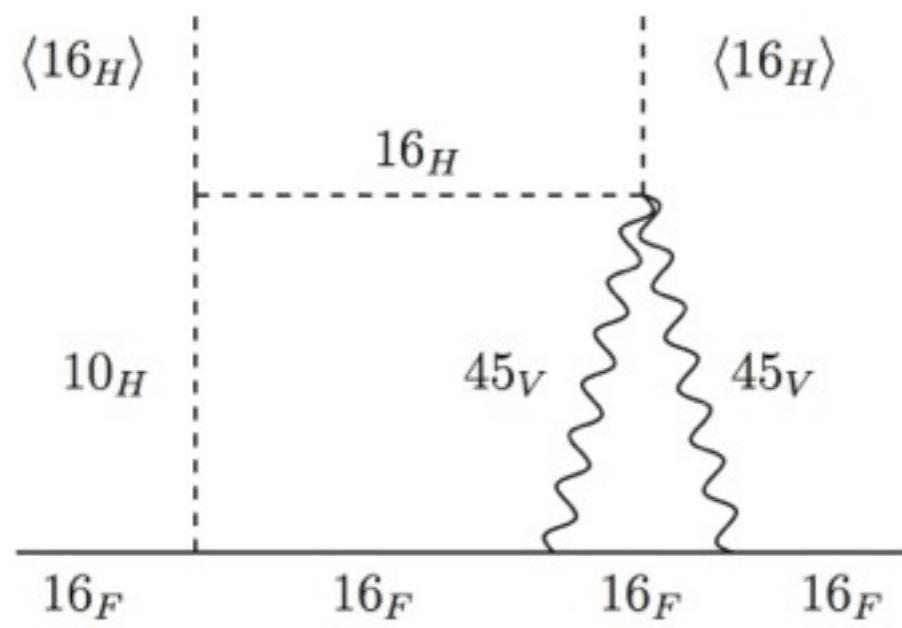
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Extremely split SUSY: SUSY scalars at the GUT scale

one-step unification

loops not killed by SUSY

Bajc, Senjanovic, Phys. Lett.B610 (2005) 80



Witten's loop in the flipped SU(5)

C.Arbelaez Rodrigues, H. Kolešová, MM, PRD 89, 055003 (2014)



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- the VEV cares only about the $SU(3) \times SU(2)$ unification scale
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Given U_V there would be a prediction for ALL proton decay channels!!!

$$\Gamma(p \rightarrow \pi^0 \ell_\alpha^+)$$

$$\Gamma(p \rightarrow \pi^+ \bar{\nu})$$

$$\Gamma(n \rightarrow \pi^- \ell_\alpha^+) \quad \Gamma(n \rightarrow \pi^0 \bar{\nu})$$

$$\Gamma(p \rightarrow K^0 \ell_\alpha^+)$$

$$\Gamma(p \rightarrow K^+ \bar{\nu})$$

$$\Gamma(n \rightarrow K^- \ell_\alpha^+) \quad \Gamma(n \rightarrow K^0 \bar{\nu})$$

$$\Gamma(p \rightarrow \eta \ell_\alpha^+)$$

$$\Gamma(n \rightarrow \eta \bar{\nu})$$

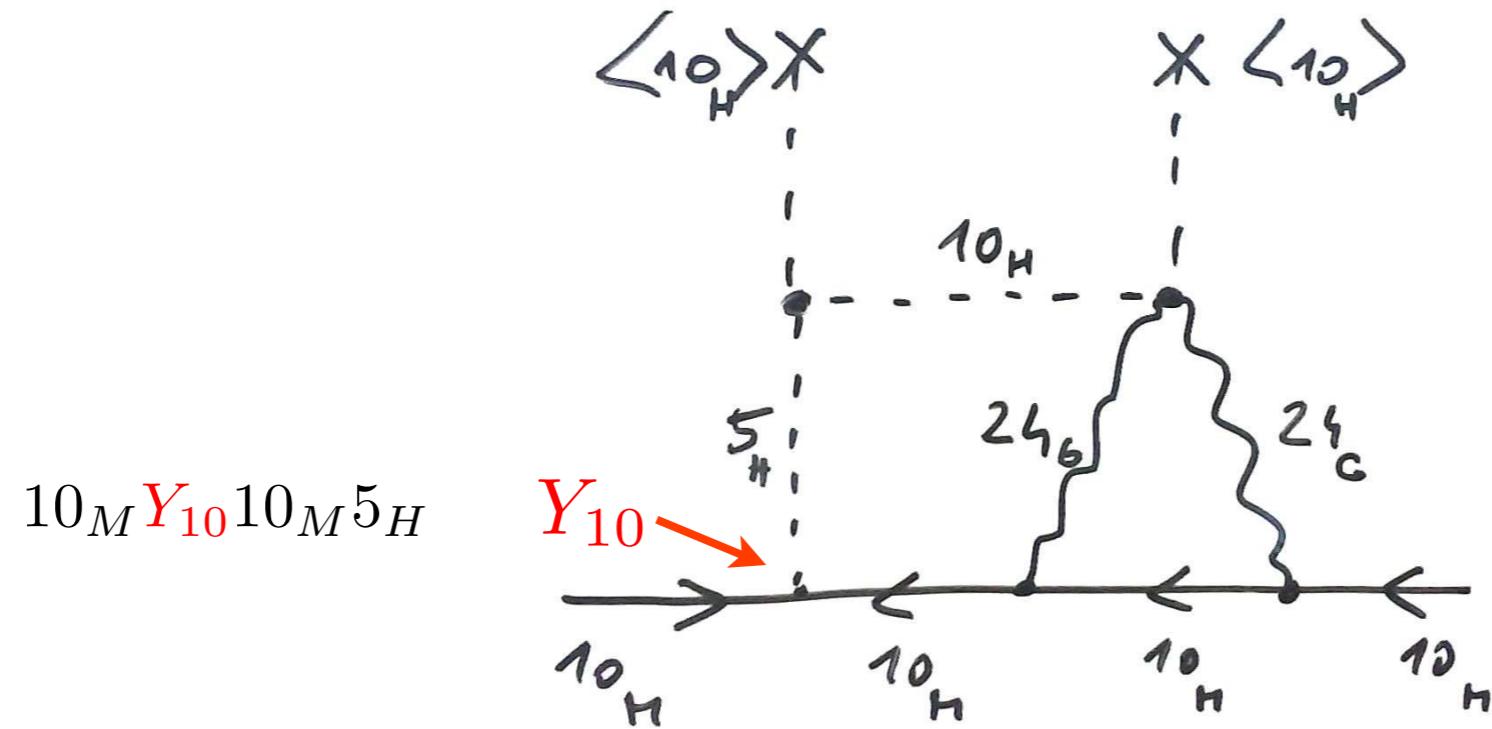
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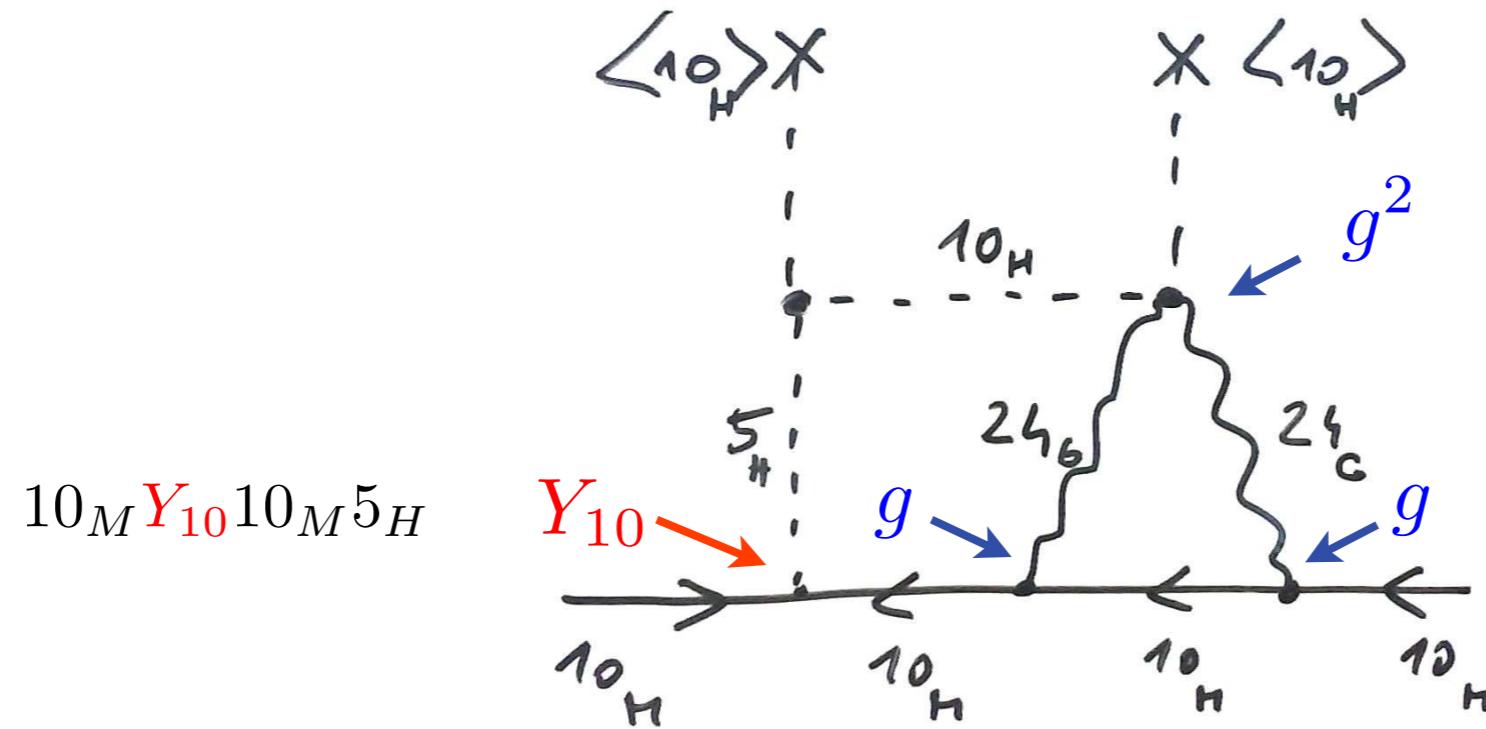
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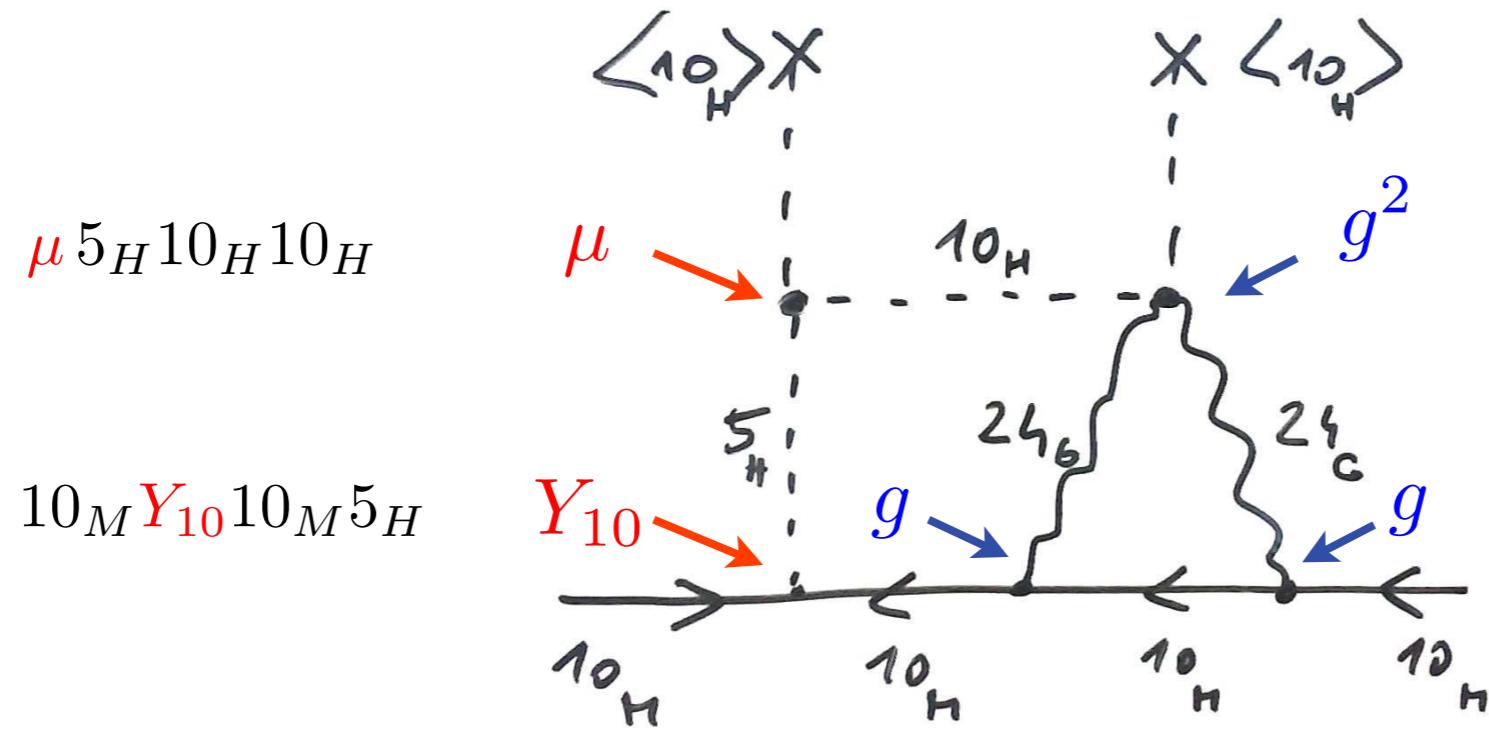
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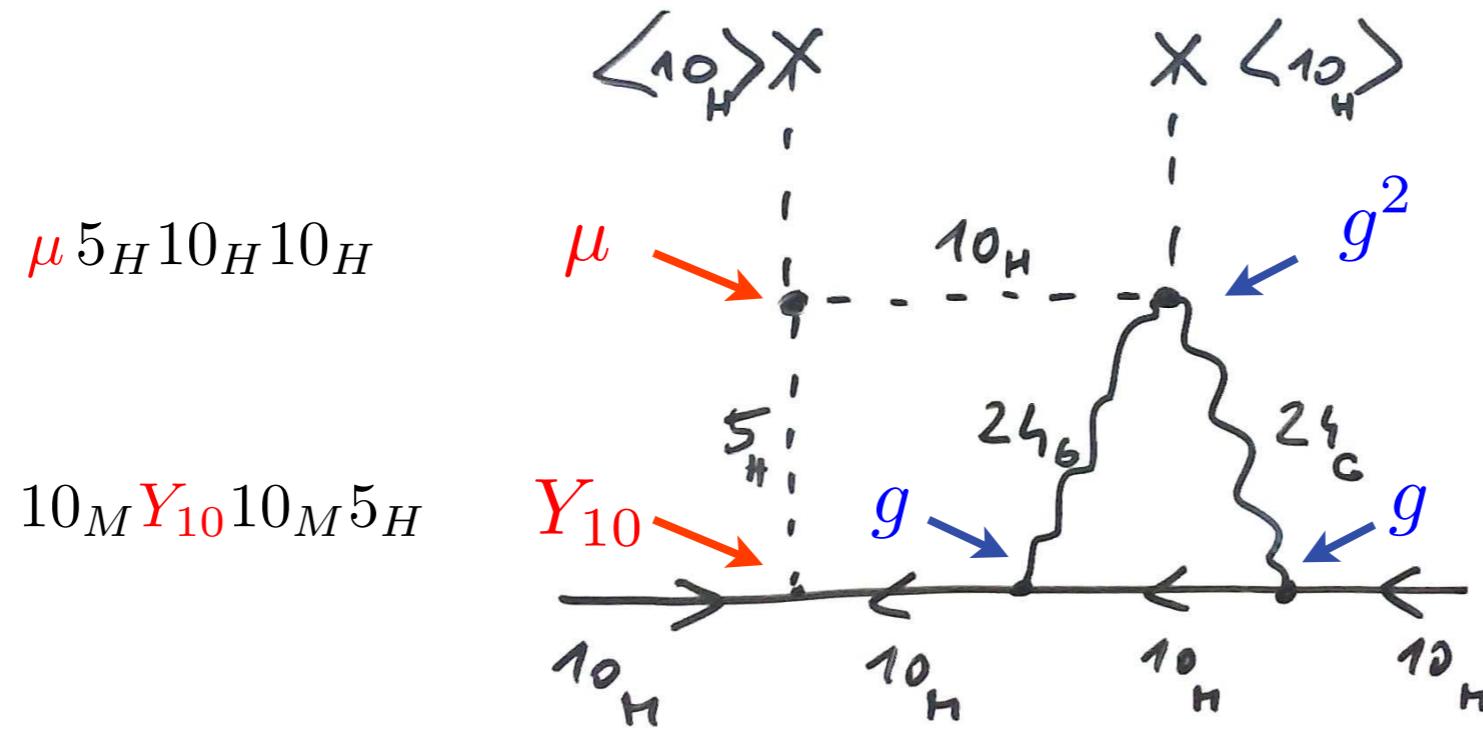
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$$M_\nu^M = \left(\frac{1}{16\pi^2}\right)^2 g^4 Y_{10} \mu \frac{\langle 10_H \rangle^2}{M_G^2} K(\dots)$$

$K(\dots)$ is an order I factor depending on the details of the heavy spectrum

MM, Catarina Simoes, work in progress

Perturbativity & stability constraints

C.Arbelaez Rodrigues, H. Kolešová, MM, PRD 89, 055003 (2014)

The scalar spectrum:

$$\begin{aligned} V = & \frac{1}{2}m_{10}^2 \text{Tr}(10_H^\dagger 10_H) + m_5^2 5_H^\dagger 5_H + \frac{1}{4}(\cancel{\mu} \varepsilon_{ijklm} 10_H^{ij} 10_H^{kl} 5^m + h.c.) + \\ & + \frac{1}{4}\lambda_1 [\text{Tr}(10_H^\dagger 10_H)]^2 + \lambda_2 \text{Tr}(10_H^\dagger 10_H 10_H^\dagger 10_H) + \lambda_3 (5_H^\dagger 5_H)^2 + \\ & + \frac{1}{2}\lambda_4 \text{Tr}(10_H^\dagger 10_H)(5_H^\dagger 5_H)^2 + \lambda_5 5_H^\dagger 10_H 10_H^\dagger 5_H \end{aligned}$$

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$$m_i^2 = 0, \quad i = 1, \dots, 16,$$

$$m_{17}^2 = \left[4\lambda_3 - \frac{(\lambda_4 + \lambda_5)^2}{\lambda_1 + 2\lambda_2} \right] v^2,$$

$$m_{18}^2 = 4(\lambda_1 + 2\lambda_2)V_G^2,$$

$$m_i^2 = -(2\lambda_2 + \frac{1}{2}\lambda_5)V_G^2 - \sqrt{(2\lambda_2 - \frac{1}{2}\lambda_5)^2 V_G^2 + 4\mu^2}, \quad i = 19, \dots, 24,$$

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C.Arbelaez Rodrigues, H. Kolešová, MM, PRD 89, 055003 (2014)

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$$\begin{aligned} V = & \frac{1}{2}m_{10}^2 \text{Tr}(10_H^\dagger 10_H) + m_5^2 5_H^\dagger 5_H + \frac{1}{4}(\mu \varepsilon_{ijklm} 10_H^{ij} 10_H^{kl} 5^m + h.c.) + \\ & + \frac{1}{4}\lambda_1 [\text{Tr}(10_H^\dagger 10_H)]^2 + \lambda_2 \text{Tr}(10_H^\dagger 10_H 10_H^\dagger 10_H) + \lambda_3 (5_H^\dagger 5_H)^2 + \\ & + \frac{1}{2}\lambda_4 \text{Tr}(10_H^\dagger 10_H)(5_H^\dagger 5_H)^2 + \lambda_5 5_H^\dagger 10_H 10_H^\dagger 5_H \end{aligned}$$

$$m_i^2 = 0, \quad i = 1, \dots, 16, \quad \xleftarrow{\hspace{1cm}} \textbf{16 real Goldstones as expected}$$

$$m_{17}^2 = \left[4\lambda_3 - \frac{(\lambda_4 + \lambda_5)^2}{\lambda_1 + 2\lambda_2} \right] v^2,$$

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Perturbativity & stability constraints

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the potential tachyon



Perturbativity & stability constraints

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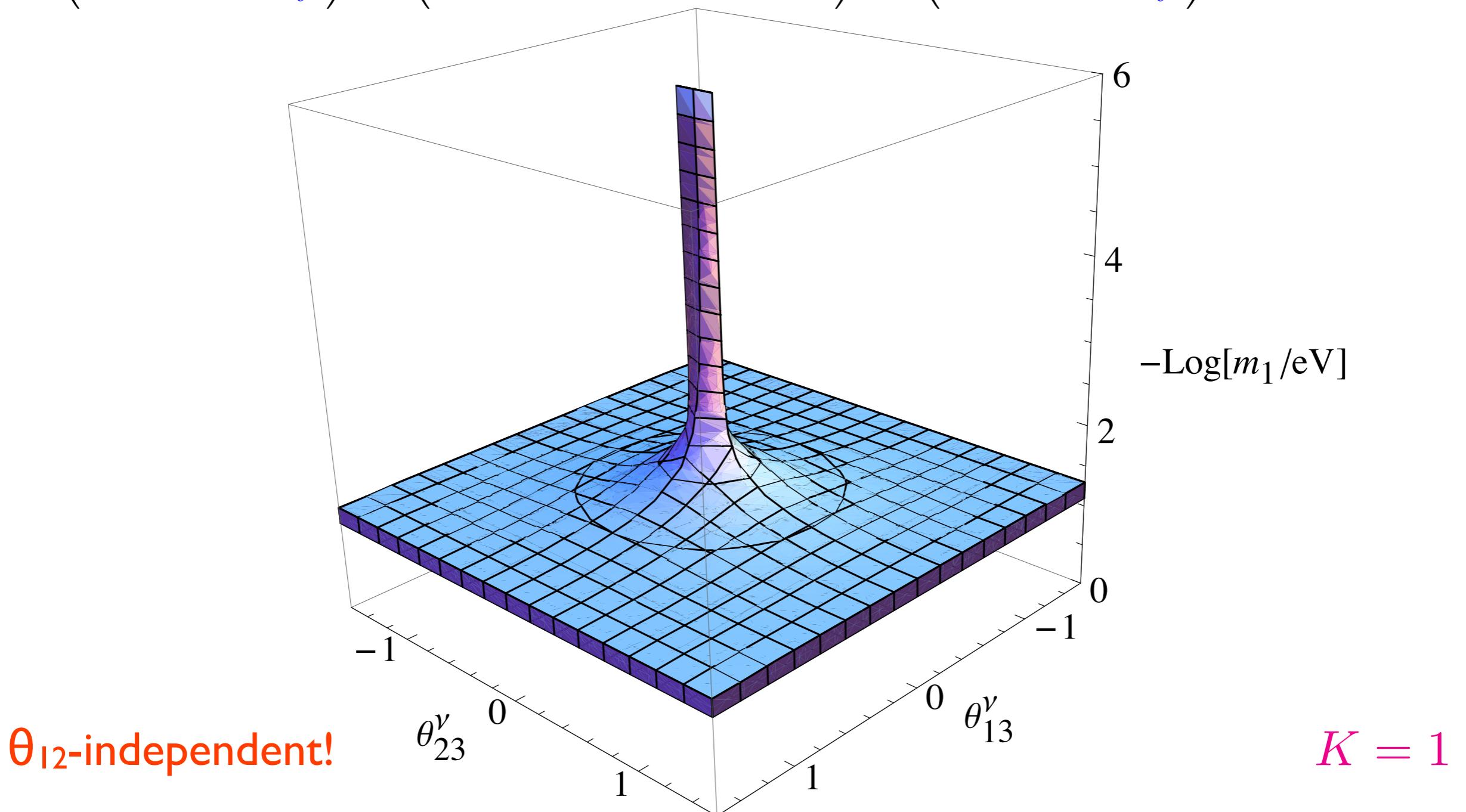
the potential tachyon



The QCD x QED vacuum is unstable unless $\mu^2 \leq \lambda_2 \lambda_5 V_G^2$

Only some U_V 's allowed!

$$\begin{pmatrix} m_u & 0 & 0 \\ 0 & m_c & 0 \\ 0 & 0 & m_t \end{pmatrix} U_\nu^\dagger \begin{pmatrix} 10^{10-\infty} & 0 & 0 \\ 0 & 10^{10-11} & 0 \\ 0 & 0 & 10^{10} \end{pmatrix} U_\nu^* \begin{pmatrix} m_u & 0 & 0 \\ 0 & m_c & 0 \\ 0 & 0 & m_t \end{pmatrix} \leq 10^{14} \text{GeV}^2 K$$



Proton decay to neutral mesons+charged leptons

This should be superimposed over the observable(s) of our interest ...

$$\Gamma(p \rightarrow \pi^0 e^+) + \Gamma(p \rightarrow \pi^0 \mu^+)$$

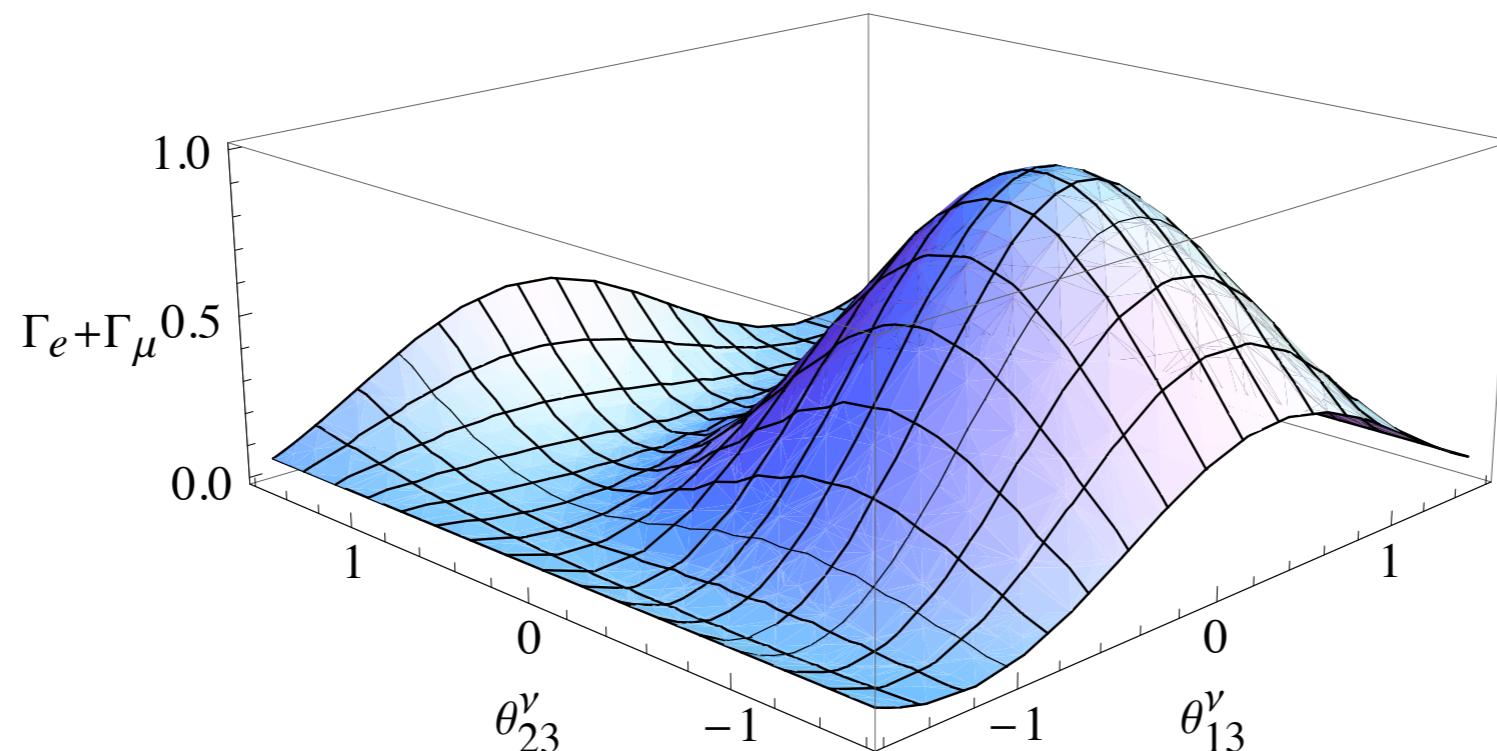
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the minima of the sum of the matrix elements

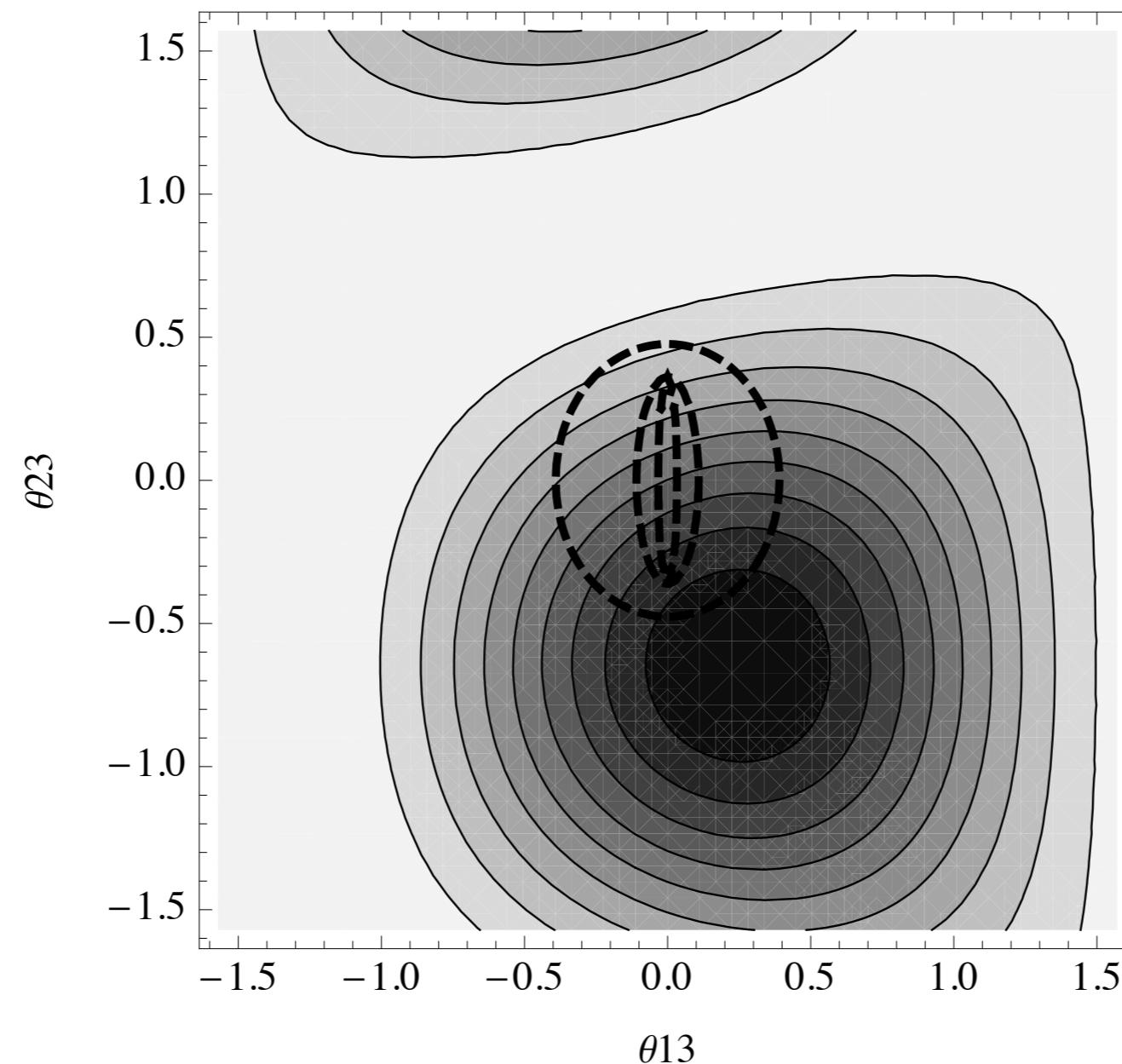
$$\Gamma(p \rightarrow \pi^0 \ell_\alpha^+) \propto |(V_{PMNS} U_\nu)_\alpha 1|^2$$



θ_{12} -dependent, analytic minimization with respect to θ_{12}

Proton decay to neutral mesons+charged leptons

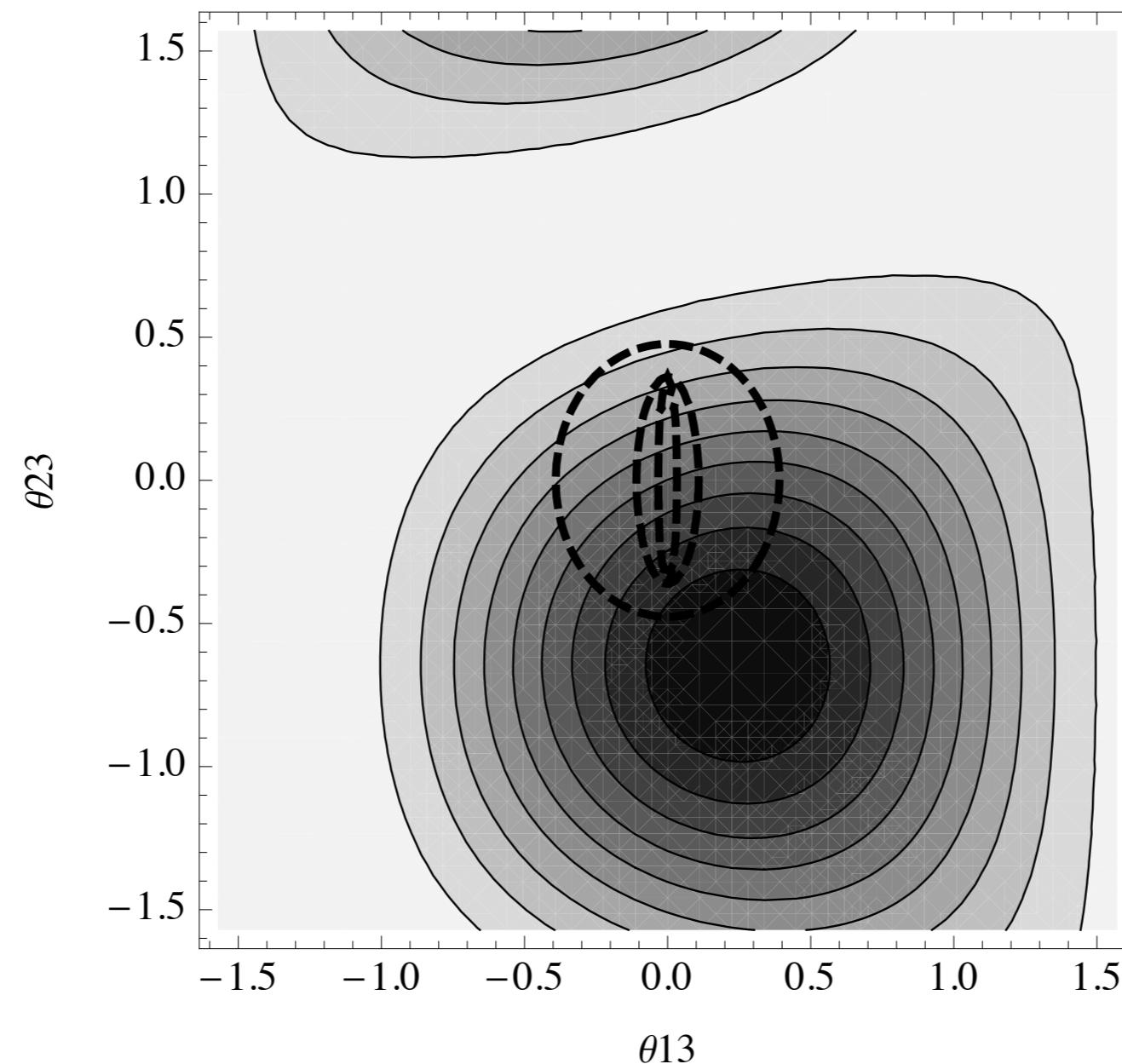
Superimposing the two: $\Gamma(p \rightarrow \pi^0 e^+) + \Gamma(p \rightarrow \pi^0 \mu^+)$ in the perturbative mode





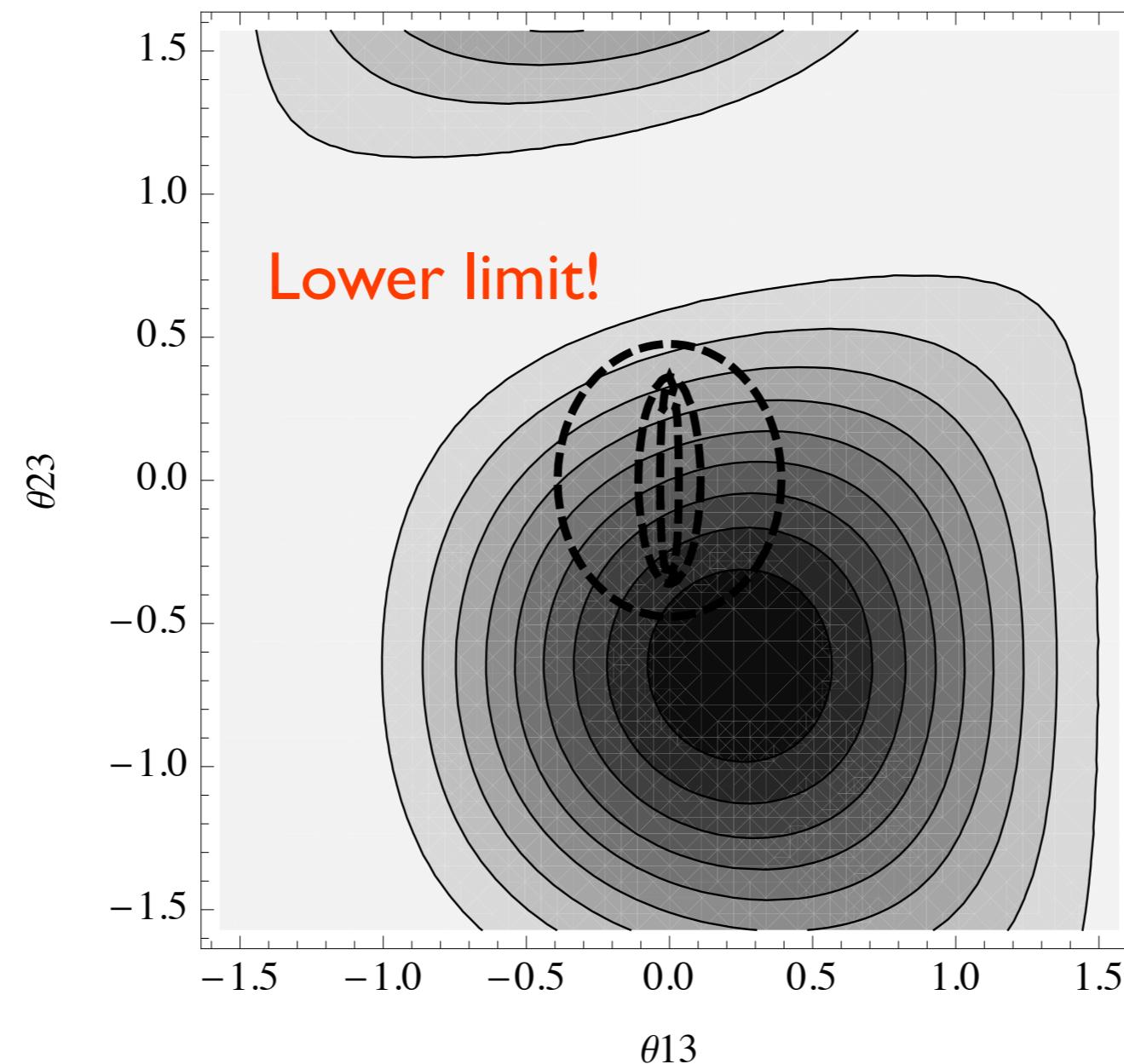
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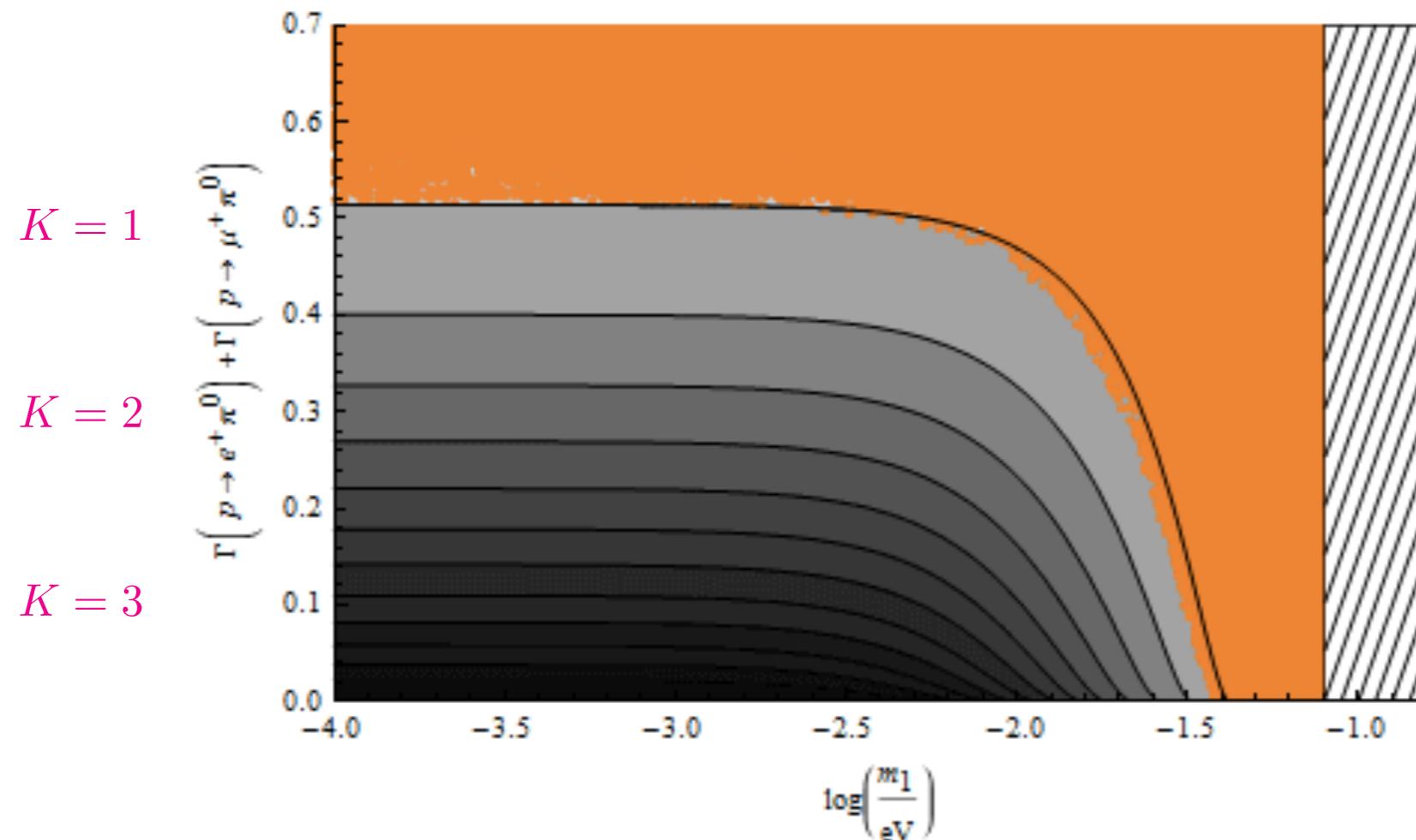
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Superimposing the two: $\Gamma(p \rightarrow \pi^0 e^+) + \Gamma(p \rightarrow \pi^0 \mu^+)$ in the perturbative mode



Proton decay to neutral mesons+charged leptons

Impossible to have both $\Gamma(p \rightarrow \pi^0 e^+)$ and $\Gamma(p \rightarrow \pi^0 \mu^+)$ arbitrarily suppressed in the perturbative regime !



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Conclusions / outlook

Proton decay is a classical yet still thrilling BSM signal

Lots of money/efforts spent in 6 decades of its searches

It's almost impossible to calculate the proton lifetime accurately enough to make a clear case...

**The long-ago cursed (but recently resurrected)
SO(10) GUT broken by the adjoint is a robust scenario!**

Flipped SU(5) may be more predictive than expected!

Thanks for your kind attention!