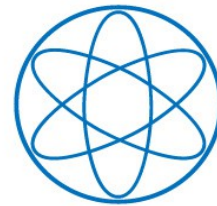


Neutrino Masses in the Two Higgs Doublet Model

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Technische Universität München



Based on: AI, C. Simonetto, JHEP 1111 (2011) 022

D. Hehn, AI, arXiv:1208.3162

J.A. Casas, AI, F. Jimenez-Alburquerque JHEP 0704 (2007) 064

Vienna
6 December 2012

Outline

- Introduction.
- Neutrino masses in the presence of right-handed neutrinos.
- Neutrino masses in the presence of right-handed neutrinos and *extra* Higgs doublets.
- The dark matter connection.
- Conclusions

Introduction

Present status in the determination of neutrino parameters:

parameter	best fit	1σ range	2σ range	3σ range
Δm_{21}^2 [10^{-5}eV^2]	7.62	7.43–7.81	7.27–8.01	7.12–8.20
$ \Delta m_{31}^2 $ [10^{-3}eV^2]	2.55	2.46 – 2.61	2.38 – 2.68	2.31 – 2.74
	2.43	2.37 – 2.50	2.29 – 2.58	2.21 – 2.64
$\sin^2 \theta_{12}$	0.320	0.303–0.336	0.29–0.35	0.27–0.37
$\sin^2 \theta_{23}$	0.613 (0.427) ^a	0.400–0.461 & 0.573–0.635	0.38–0.66	0.36–0.68
	0.600	0.569–0.626	0.39–0.65	0.37–0.67
$\sin^2 \theta_{13}$	0.0246	0.0218–0.0275	0.019–0.030	0.017–0.033
	0.0250	0.0223–0.0276	0.020–0.030	
δ	0.80π -0.03π	$0 - 2\pi$	$0 - 2\pi$	$0 - 2\pi$

Forero, Tortola, Valle
arXiv::1205.4018

WMAP, $0\nu 2\beta \rightarrow m_\nu \lesssim 0.5 \text{ eV}$

No information about CP violation or about the neutrino mass spectrum

Even with this limited information about the neutrino sector, we can already notice some features:

- Neutrino masses are tiny, $m_\nu \lesssim O(0.1 \text{ eV})$
- Two large mixing angles ($\theta_{\text{atm}} \simeq \pi/4$, $\theta_{\text{sol}} \simeq \pi/6$)

One small mixing angle ($\theta_{13} \simeq 0$)

$$U_{lep} \simeq \begin{pmatrix} \sqrt{2/3} & \sqrt{1/3} & 0 \\ -\sqrt{1/6} & \sqrt{1/3} & -\sqrt{1/2} \\ -\sqrt{1/6} & \sqrt{1/3} & \sqrt{1/2} \end{pmatrix}$$

- The two heaviest neutrinos present a mild mass hierarchy

$$\Delta m_{\text{atm}}^2 = m_3^2 - m_1^2 \longrightarrow m_3 = \sqrt{\Delta m_{\text{atm}}^2 + m_1^2}$$

$$\Delta m_{\text{sol}}^2 = m_2^2 - m_1^2 \longrightarrow m_2 = \sqrt{\Delta m_{\text{sol}}^2 + m_1^2}$$

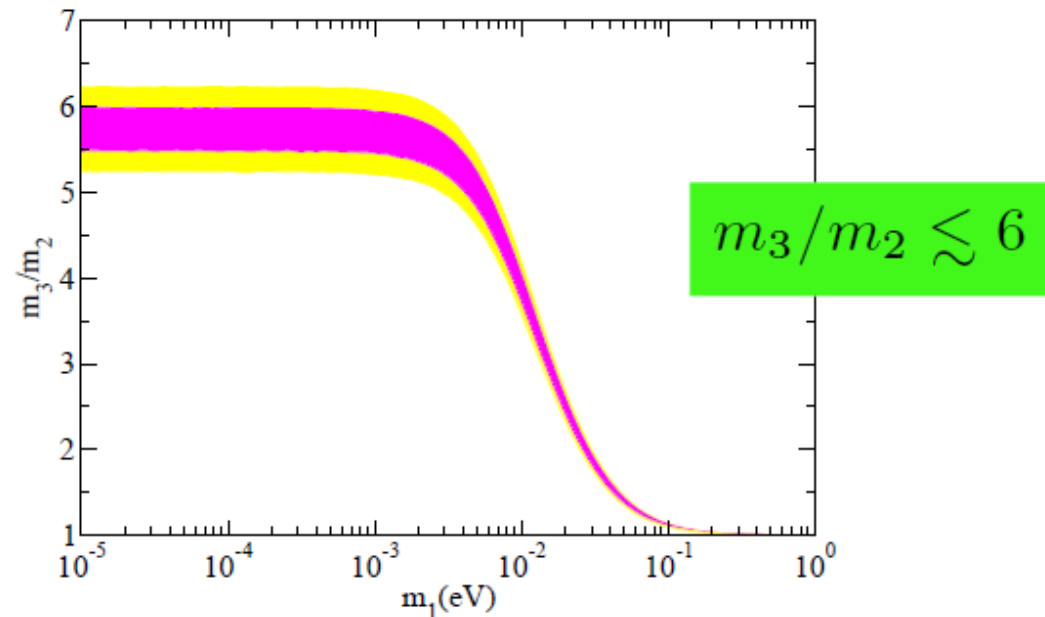
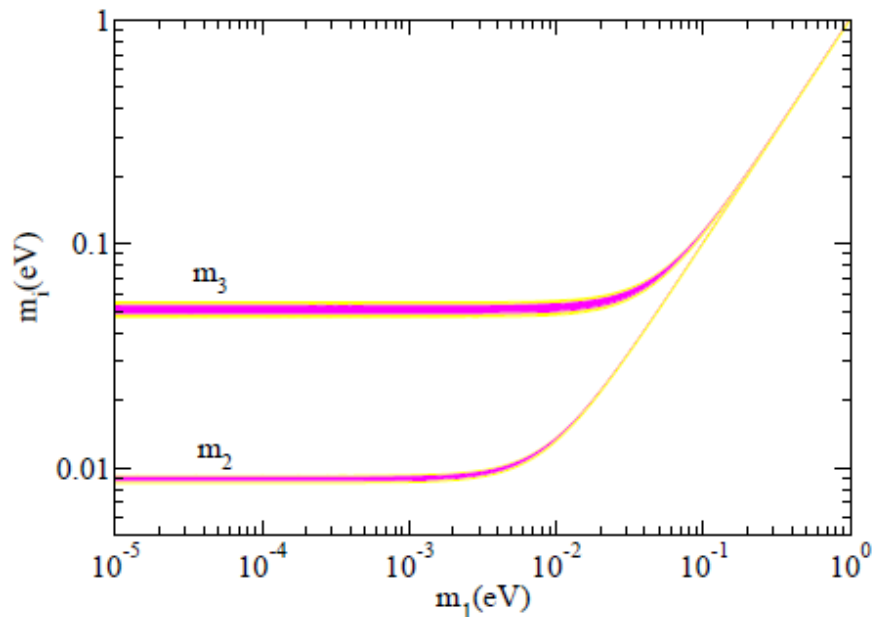
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Compare to the quark sector

$$\left. \begin{array}{l} m_u = 1.7 \text{ to } 3.8 \text{ MeV} \\ m_c = 1.27_{-0.09}^{+0.07} \text{ GeV} \\ m_t = 172.0 \pm 0.9 \pm 1.3 \text{ GeV} \end{array} \right\} \begin{array}{l} m_t/m_c \simeq 140 \\ m_c/m_d \simeq 500 \end{array}$$

$$\text{vs. } m_3/m_2 \lesssim 6$$

$$\left. \begin{array}{l} m_d = 4.1 \text{ to } 5.8 \text{ MeV} \\ m_s = 101_{-21}^{+29} \text{ MeV} \\ m_b = 4.19_{-0.09}^{+0.07} \text{ GeV} \end{array} \right\} \begin{array}{l} m_b/m_s \simeq 41 \\ m_s/m_d \simeq 20 \end{array}$$

$$|U_{\text{CKM}}| = \begin{pmatrix} 0.97 & 0.23 & 0.004 \\ 0.23 & 0.973 & 0.04 \\ 0.008 & 0.04 & 1 \end{pmatrix} \quad \text{vs. } |U_{\text{lep}}| \simeq \begin{pmatrix} 0.82 & 0.56 & 0 \\ 0.41 & 0.56 & 0.71 \\ 0.41 & 0.56 & 0.71 \end{pmatrix}$$

Compare also to the charged lepton sector

$$\left. \begin{array}{l} m_e = 0.51 \text{ MeV} \\ m_\mu = 106 \text{ MeV} \\ m_\tau = 1.78 \text{ GeV} \end{array} \right\} \begin{array}{l} m_\tau/m_\mu \simeq 17 \\ m_\mu/m_e \simeq 208 \end{array}$$

The neutrino sector presents a completely different pattern

Any model of neutrino masses should address the following questions:

- **Why tiny masses?**
- **Why mild mass hierarchy?**
- **Why large mixing angles?**

And **preferably**, the model should be testable

A very popular neutrino mass model: the (type I) see-saw model

Add to the Standard Model at least two right-handed neutrinos

$$-\mathcal{L}^\nu = (Y_\nu)_{ij} \bar{l}_{Li} \nu_{Rj} \tilde{\Phi} - \frac{1}{2} M_{Mij} \bar{\nu}_{Ri}^C \nu_{Rj} + \text{h.c.}$$



$$M_{\text{Maj}} \gg M_Z$$

$$-\mathcal{L}^{\nu, \text{eff}} = \frac{1}{2} \kappa_{ij} (\bar{l}_{Li} \tilde{\Phi}) (\tilde{\Phi}^T l_{Lj}^C) + \text{h.c.}$$

$$\kappa = (Y_\nu M_M^{-1} Y_\nu^T) \quad \Rightarrow \quad \mathcal{M}_\nu = \frac{v^2}{2} \kappa$$

Very compelling explanation
to the small neutrino masses

Furthermore, this model predicts charged lepton flavour violation:

$\text{BR}(\mu \rightarrow e \gamma) \sim 10^{-57}$, in *excellent* agreement with experiments.

Can the type I see-saw mechanism accommodate a mild mass hierarchy?

The high energy theory, spanned by $\{Y_\nu, M_{\text{maj}}\}$, depends on 18 parameters

The low energy theory, spanned by $\{\mathcal{M}_\nu\}$, depends on 9 parameters

There is a lot of freedom at high energies

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It would not be surprising if the see-saw mechanism could accommodate $m_3/m_2 < 6$.

The answer is yes. In fact the see-saw mechanism can accommodate anything

$$Y_\nu = \frac{1}{\langle \Phi^0 \rangle} U_{\text{lep}}^* \sqrt{D_m} R^T \sqrt{D_M} \quad \text{Casas, AI}$$

$$R = \begin{pmatrix} \hat{c}_2 \hat{c}_3 & -\hat{c}_1 \hat{s}_3 - \hat{s}_1 \hat{s}_2 \hat{c}_3 & \hat{s}_1 \hat{s}_3 - \hat{c}_1 \hat{s}_2 \hat{c}_3 \\ \hat{c}_2 \hat{s}_3 & \hat{c}_1 \hat{c}_3 - \hat{s}_1 \hat{s}_2 \hat{s}_3 & -\hat{s}_1 \hat{c}_3 - \hat{c}_1 \hat{s}_2 \hat{s}_3 \\ \hat{s}_2 & \hat{s}_1 \hat{c}_2 & \hat{c}_1 \hat{c}_2 \end{pmatrix} \quad D_M = \text{diag}(M_1, M_2, M_3)$$

But there is a price...

The price is that the resulting Yukawa coupling could be “weird”

For example, taking $M_1=10^9$ GeV, $M_2=10^{11}$ GeV, $M_3=10^{13}$ GeV and $R(z_1=2i, z_2=0, z_3=0)$, one obtains the matrix

$$Y_\nu = \begin{pmatrix} 1.9 \times 10^{-4} & 0.011 & 0.11i \\ -8.6 \times 10^{-5} & 0.012 - 0.031i & 0.32 + 0.12i \\ 8.6 \times 10^{-5} & -0.012 - 0.031i & 0.32 - 0.12i \end{pmatrix}$$

Which reproduces, *by construction*, the low energy neutrino data ($m_3=0.05$ eV, $m_2=0.0083$ eV, $\sin^2\theta_{12}=0.3$, $\sin^2\theta_{23}=1$, and $m_1=m_2/6$, $\theta_{13}=0$ and no CP violation)

However, the eigenvalues are

$$\left. \begin{array}{l} y_3 = 0.50 \\ y_2 = 1.3 \times 10^{-3} \\ y_1 = 2.2 \times 10^{-4} \end{array} \right\} \begin{array}{l} y_3/y_2 = 379 \\ y_2/y_1 = 6 \end{array}$$

This Yukawa coupling does not seem to be generated by the same mechanism that generates Y_u , Y_d , Y_e (whatever it is...)

A more interesting question is not whether the see-saw can accommodate the data, but whether the see-saw can accommodate the data *with our present (very limited) understanding of the origin of flavour*.

Can the see-saw mechanism accommodate the oscillation data when the neutrino Yukawa couplings are hierarchical?

Not so easy... The see-saw mechanism tends to produce very large neutrino mass hierarchies

Casas, AI, Jimenez-Alburquerque

“Naïve see-saw” (no mixing)

$$m_1 \sim \frac{y_1^2}{M_1} \langle \Phi^0 \rangle^2, \quad m_2 \sim \frac{y_2^2}{M_2} \langle \Phi^0 \rangle^2, \quad m_3 \sim \frac{y_3^2}{M_3} \langle \Phi^0 \rangle^2 \quad \frac{m_3}{m_2} \sim \frac{y_3^2}{y_2^2} \frac{M_2}{M_3}$$

- Assume hierarchical Yukawa couplings $y_1 : y_2 : y_3 \sim 1 : 20 : 20^2$ (down-type quark Yukawas)
 $y_1 : y_2 : y_3 \sim 1 : 300 : 300^2$ (up-type quark Yukawas)

- For the right-handed neutrino masses, we don't know

Hierarchy in ν_R as in Y_ν	Degenerate ν_R	
$\frac{m_3}{m_2} \sim 20 - 300$	$\frac{m_3}{m_2} \sim 400 - 90000$	far from $\frac{m_3}{m_2} \lesssim 6$

A more rigorous analysis shows that **generically**

$\frac{m_3}{m_2} \gtrsim \frac{y_3^2}{y_2^2} \frac{M_3}{M_2}$	Hierarchical ν_R	$\frac{m_3}{m_2} \gtrsim \mathcal{O}(10^{3-7})$	far from $\frac{m_3}{m_2} \lesssim 6$
	Degenerate ν_R	$\frac{m_3}{m_2} \gtrsim \mathcal{O}(10^{2-5})$	

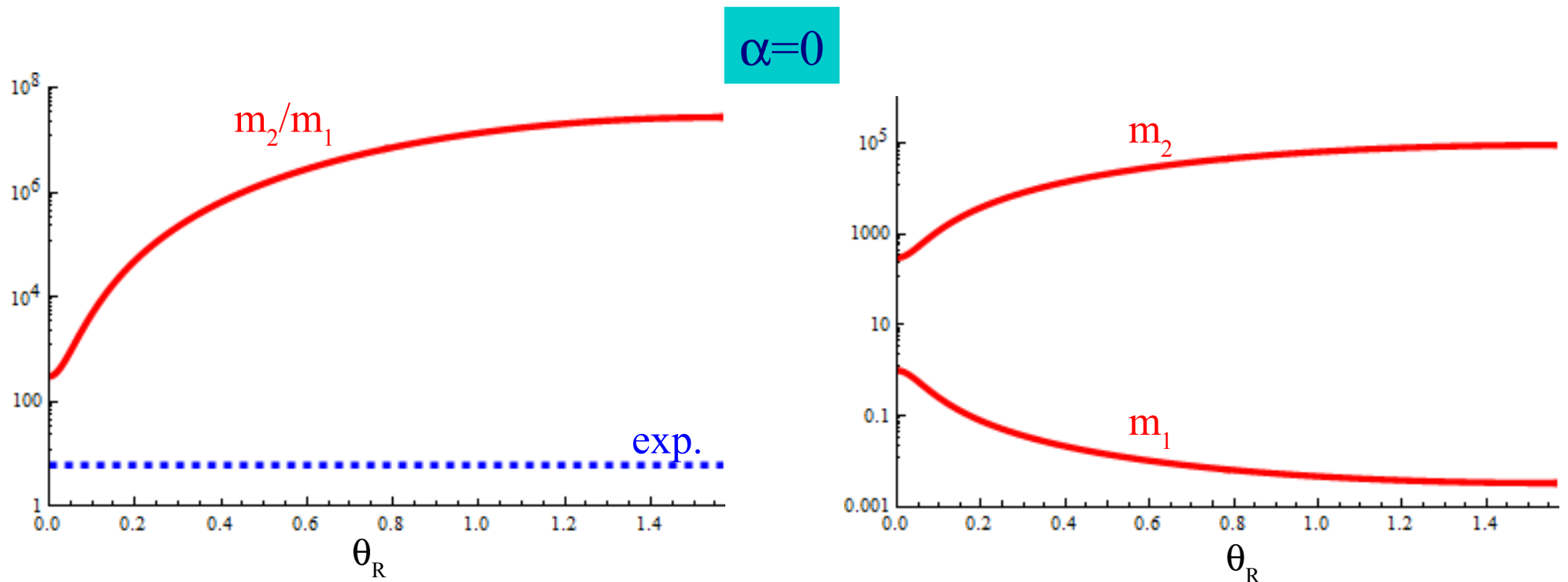
Consider a model with just two right-handed neutrinos

Assume

$$\begin{aligned} y_1 : y_2 &= 1 : 300 \\ M_1 : M_2 &= 1 : 300 \end{aligned}$$

(inspired by the hierarchy
in the up-quark sector)

The neutrino mass hierarchy depends just on the mixing angle in the right-handed sector, θ_R , and on the Majorana phase α .



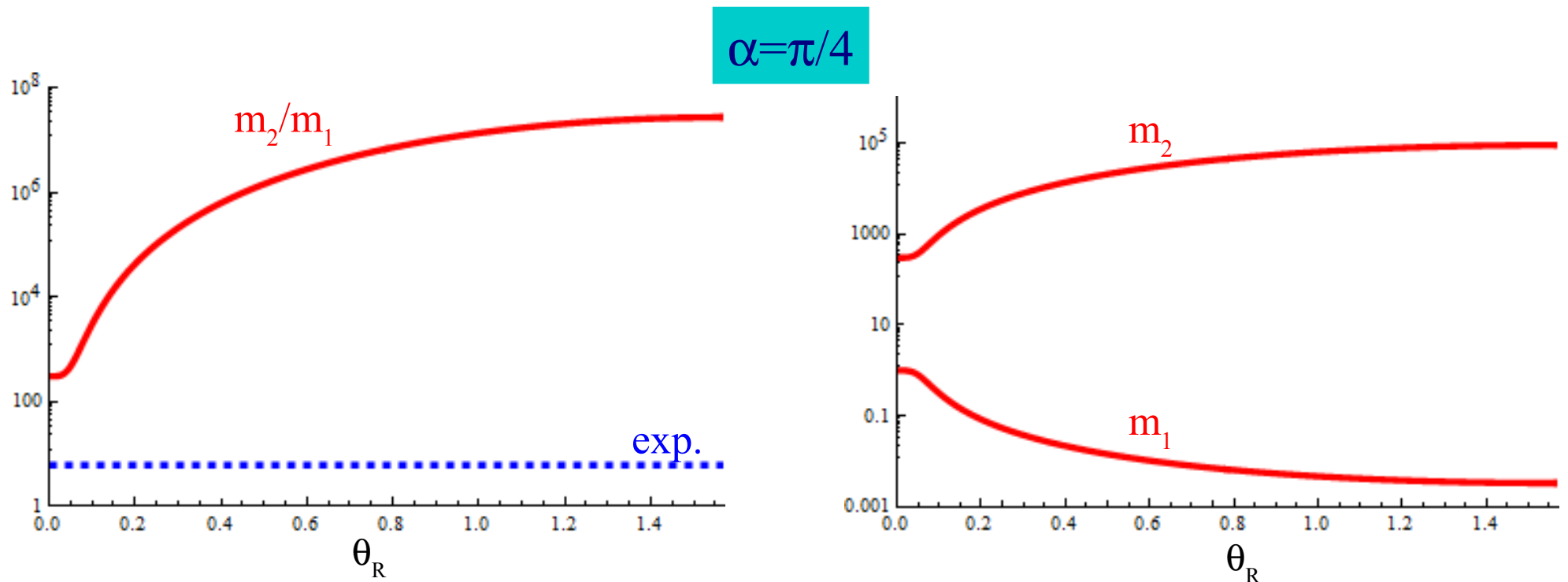
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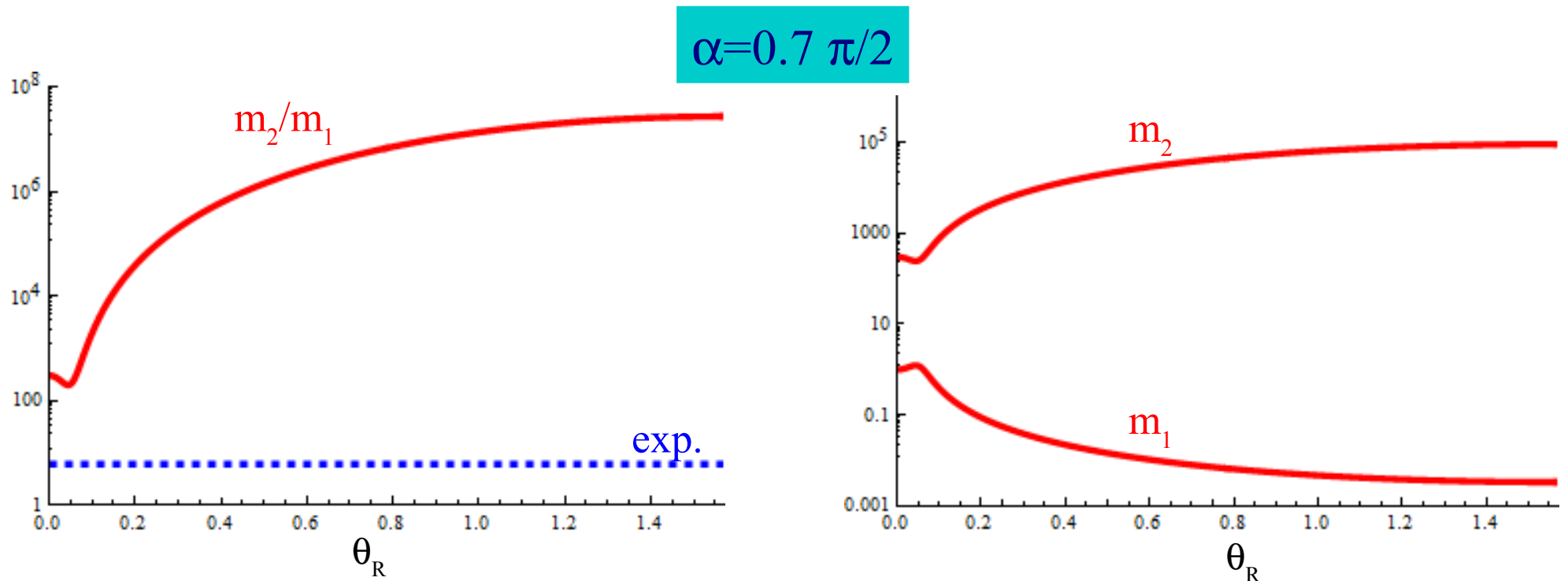
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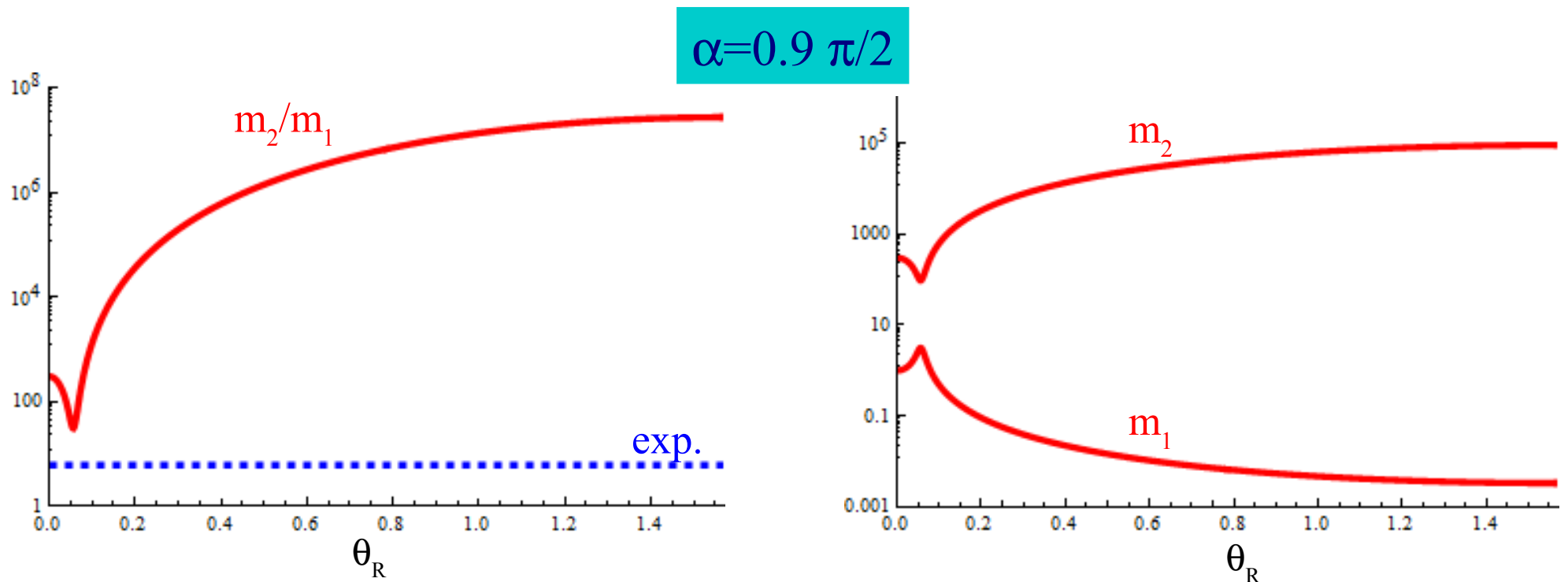
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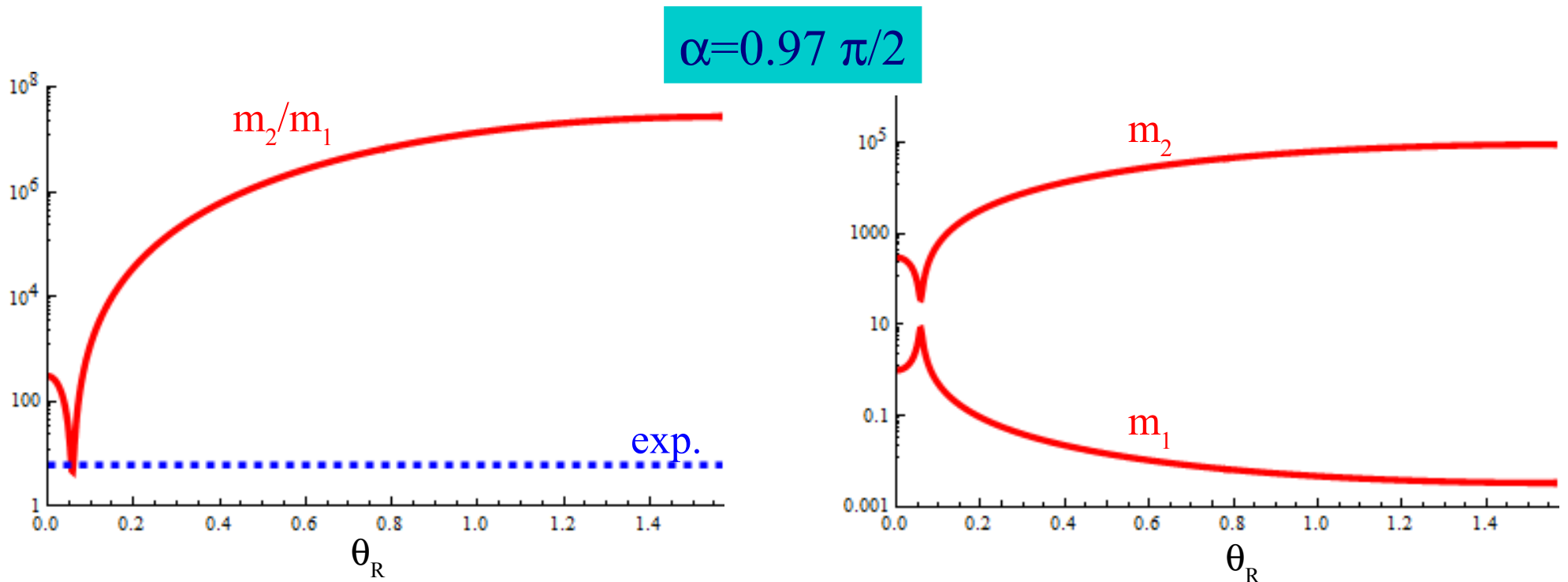
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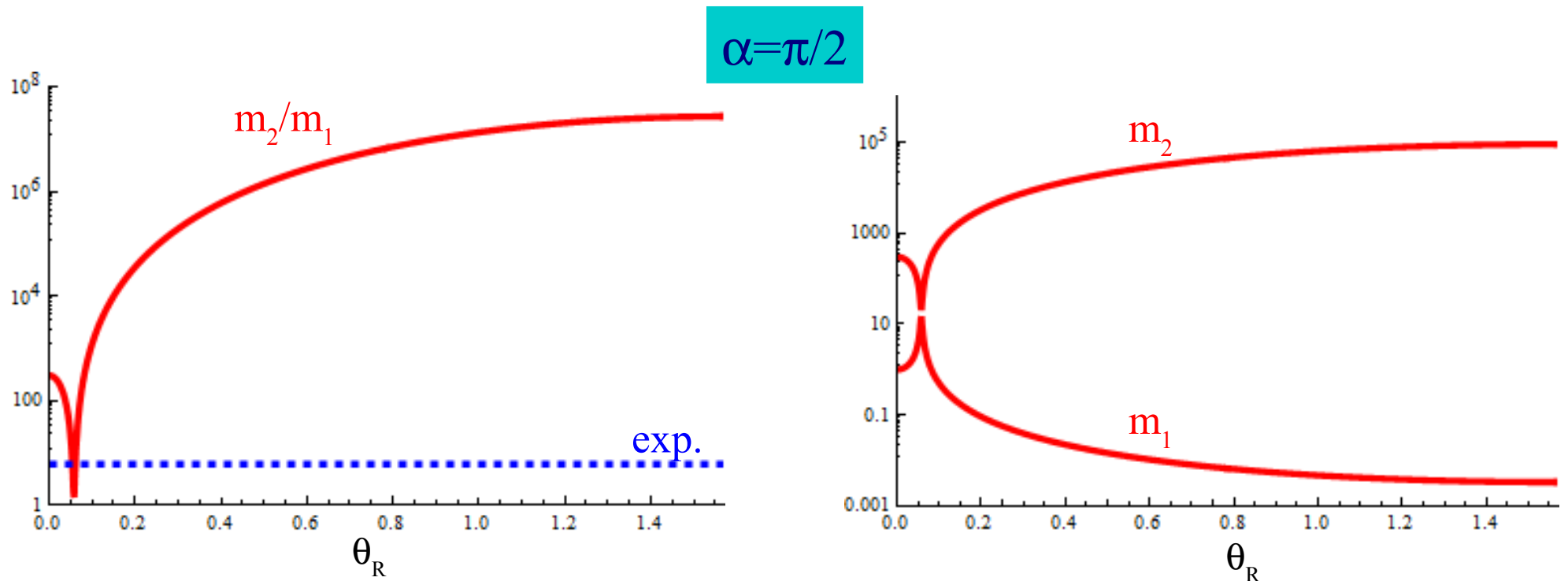
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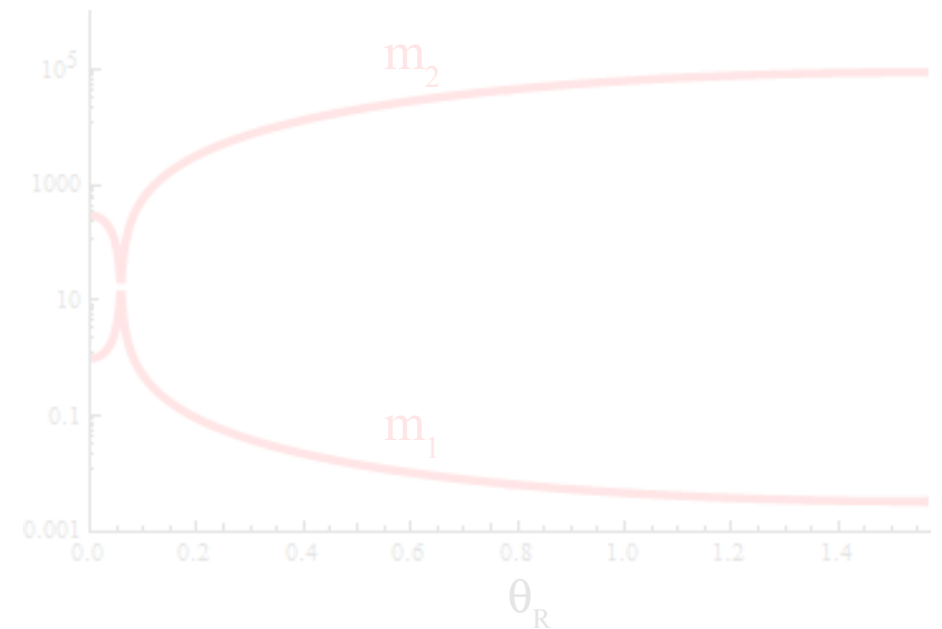
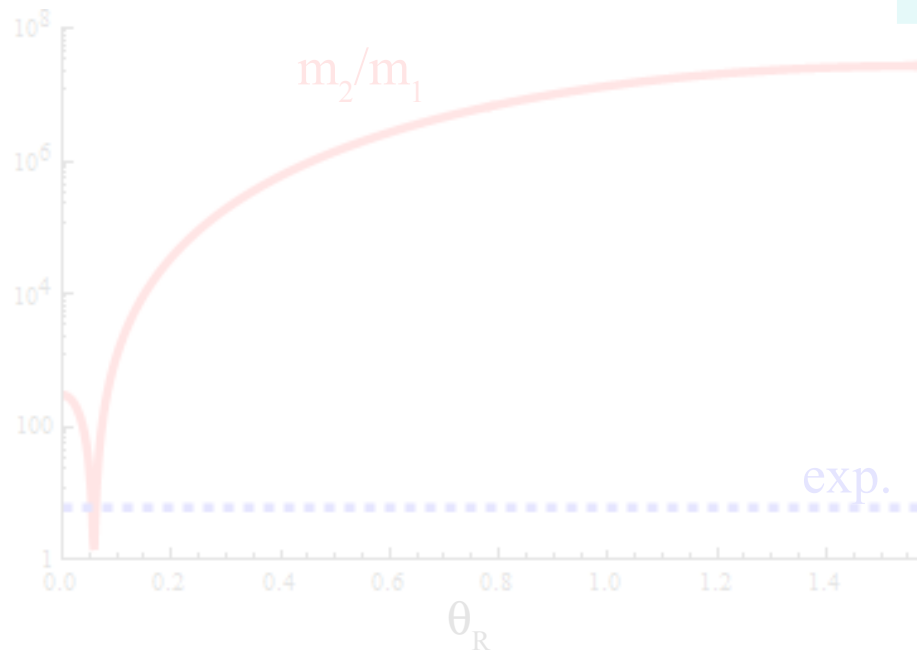
C The see-saw mechanism (with two right-handed neutrinos) with hierarchical Yukawa eigenvalues and RH masses can accommodate the observed neutrino mass hierarchy, but *only for very special choices of parameters*.

The
the r

$$\cos^2 \theta_R \simeq \frac{M_2 y_2^2 - M_1 y_1^2}{(M_1 + M_2)(y_2^2 - y_1^2)} \quad \text{and} \quad \alpha \simeq \pi/2$$

ngle in

$$\alpha = \pi/2$$



There are two situations where the see-saw mechanism can naturally generate a mild neutrino mass hierarchy (without tunings):

“naive see-saw” $\frac{m_2}{m_1} \sim \frac{y_2^2}{y_1^2} \frac{M_1}{M_2} \lesssim 6$

Very mild hierarchies

$$y_1 \simeq y_2$$

$$M_1 \simeq M_2$$

$$y_1 : y_2 = 1 : 2$$

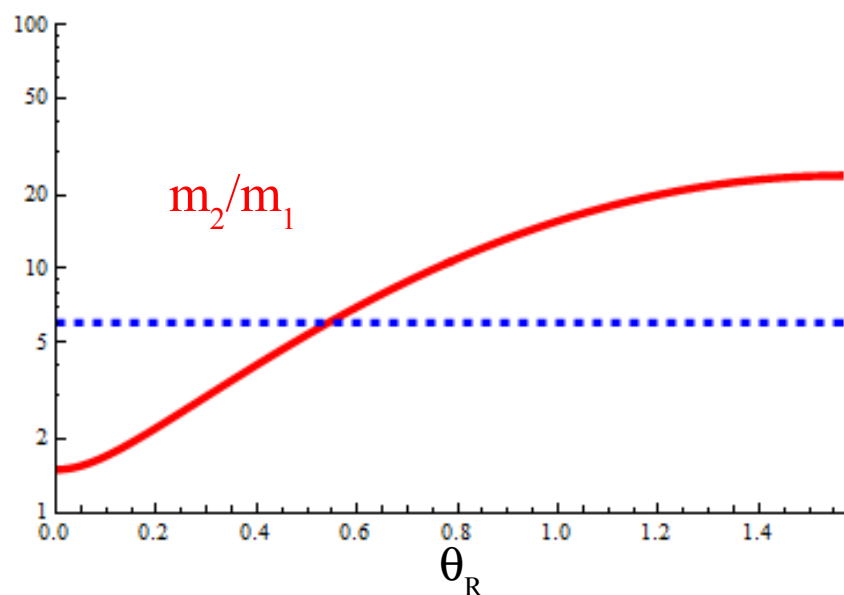
$$M_1 : M_2 = 1 : 6$$

Very strong hierarchy in RH masses

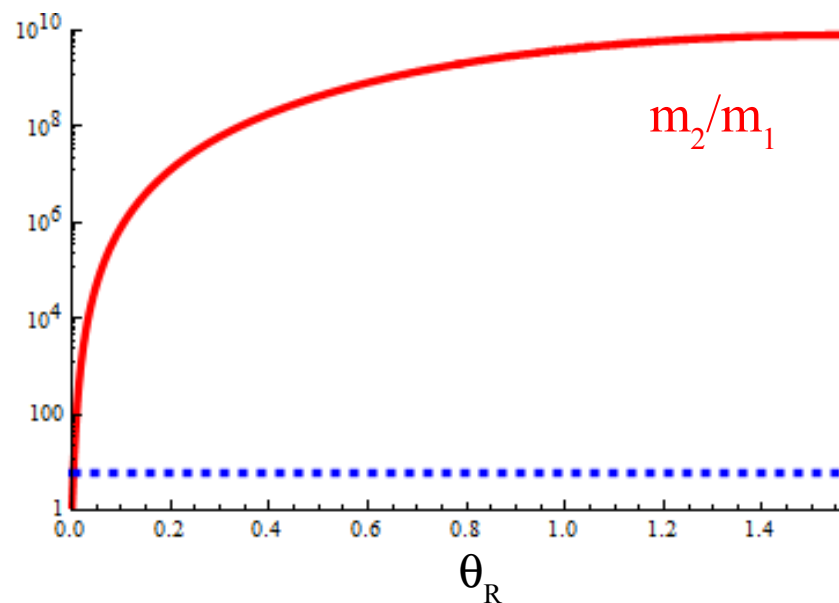
$$M_1 : M_2 \simeq y_1^2 : y_2^2$$

$$y_1 : y_2 = 1 : 300$$

$$M_1 : M_2 = 1 : 90000$$



$\alpha=0$



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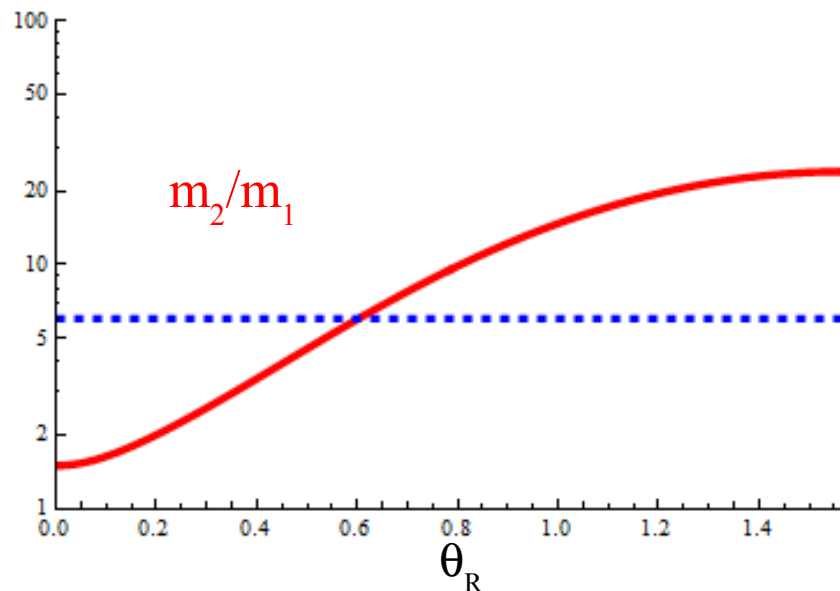
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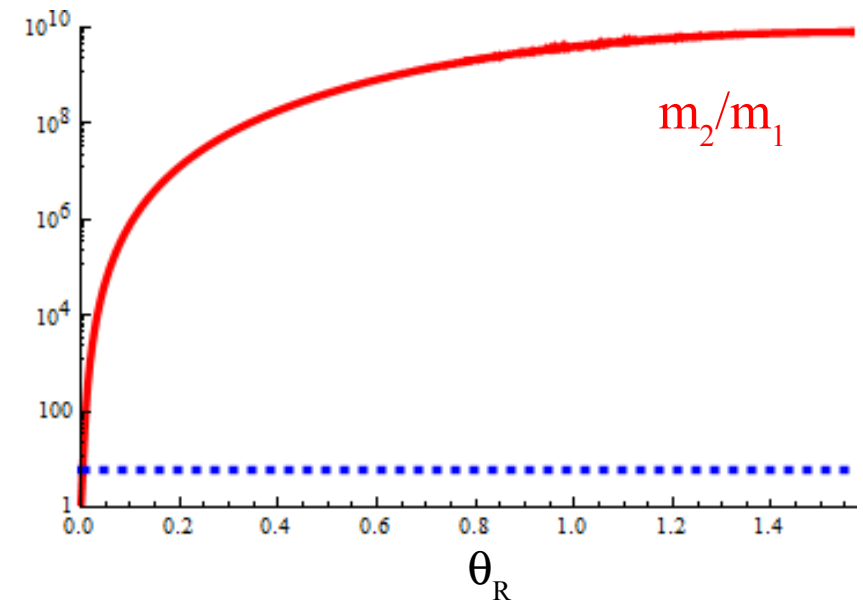
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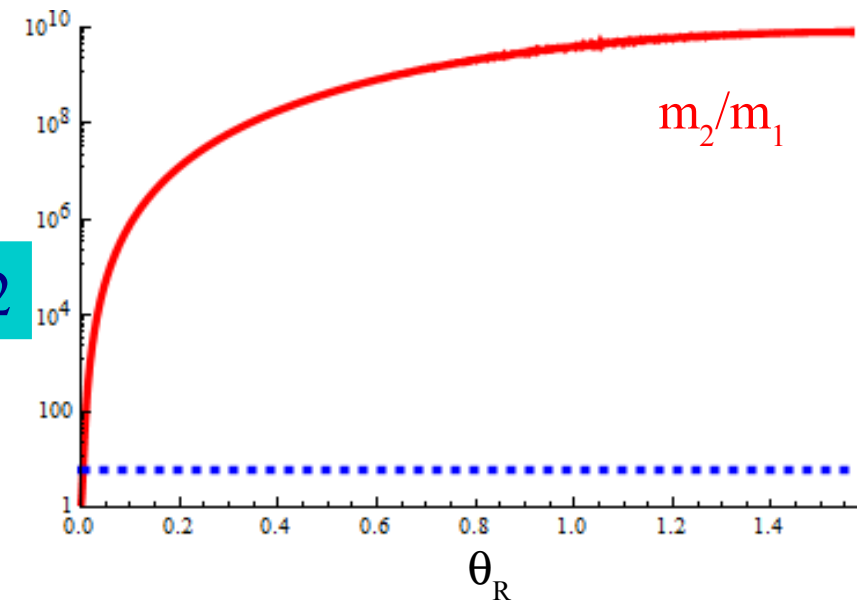
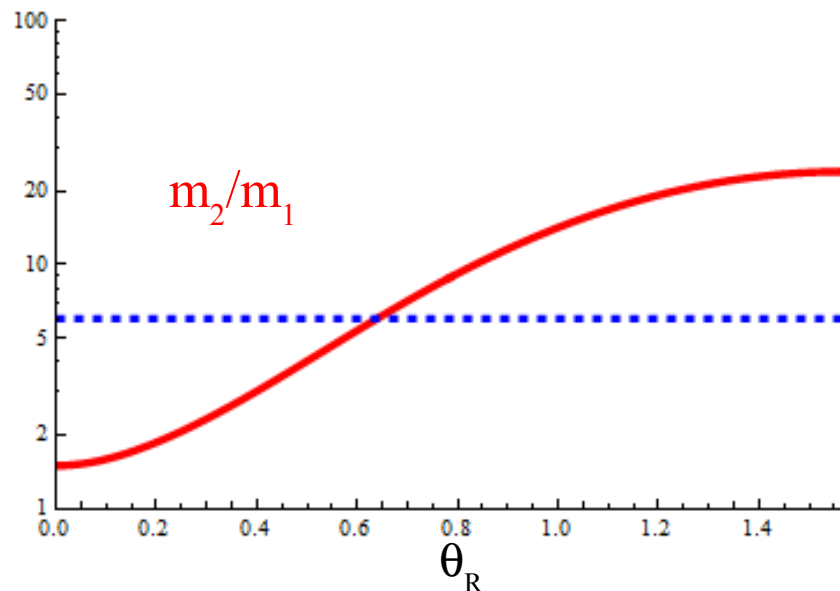
$$M_1 : M_2 = 1 : 6$$

Very strong hierarchy in RH masses

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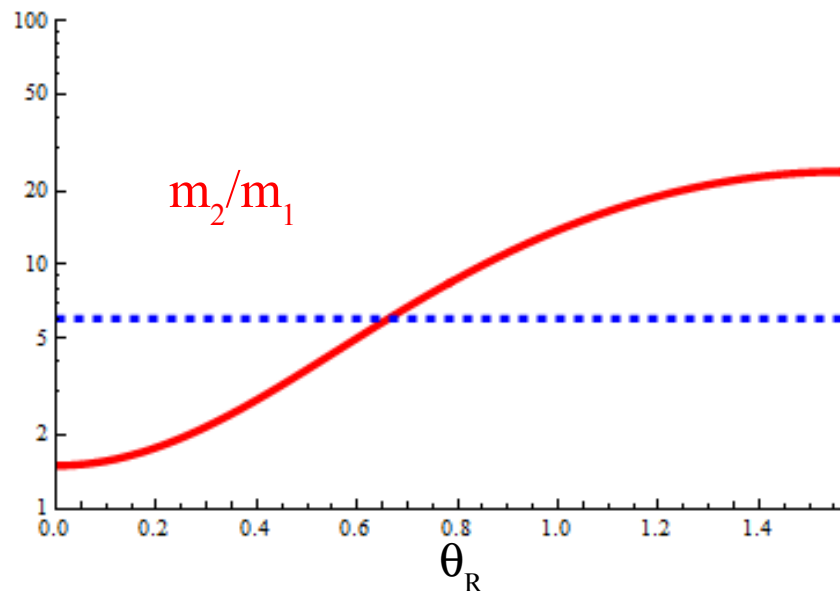
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Very strong hierarchy in RH masses

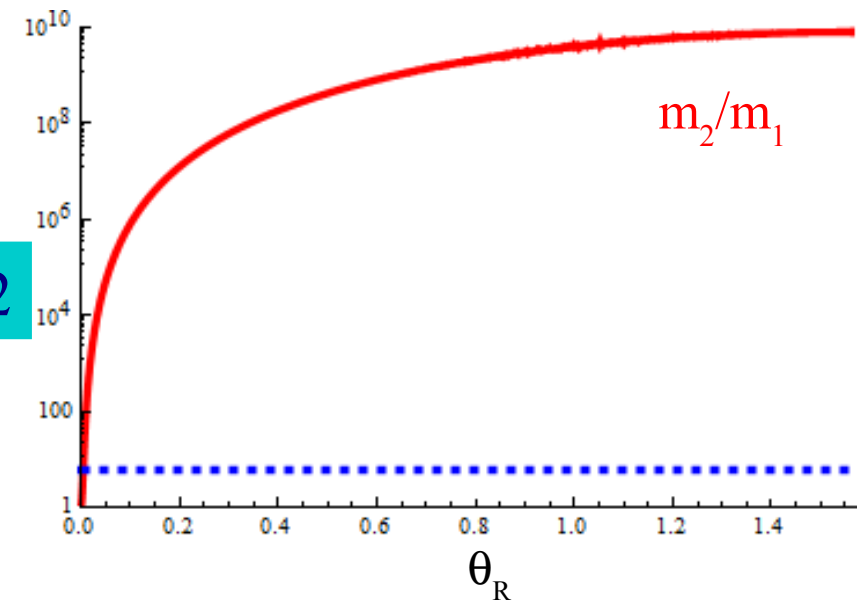
$$M_1 : M_2 \simeq y_1^2 : y_2^2$$

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$\alpha = 0.9 \pi/2$



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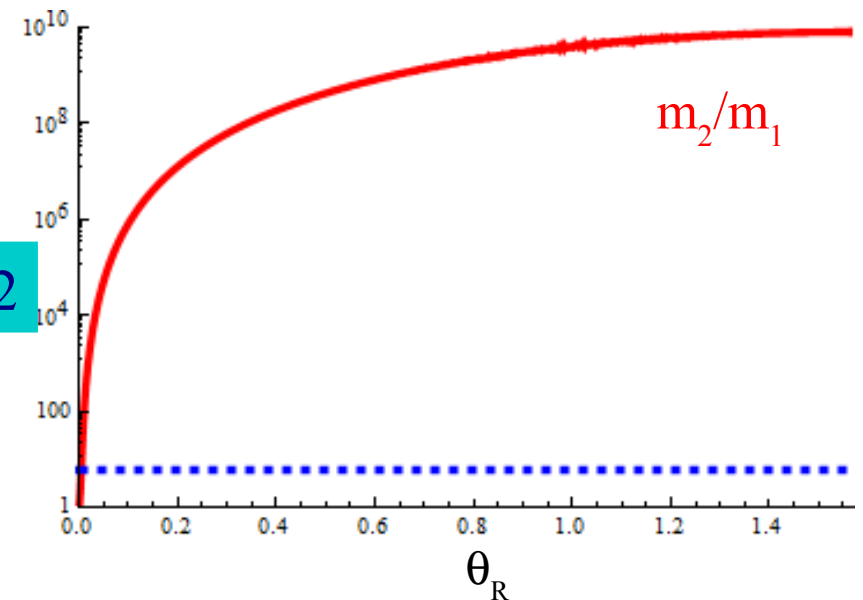
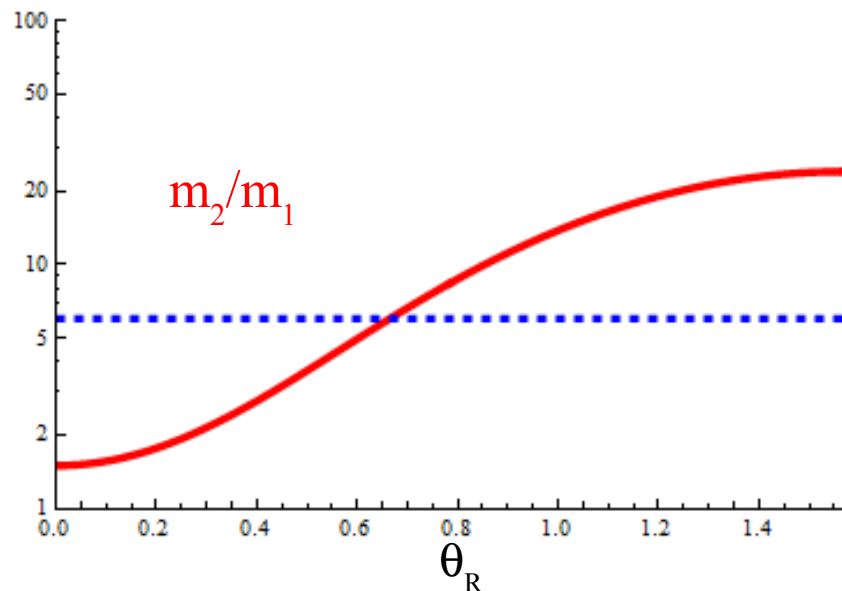
$$M_1 : M_2 = 1 : 6$$

Very strong hierarchy in RH masses

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$$y_1 : y_2 = 1 : 300$$

$$M_1 : M_2 = 1 : 90000$$



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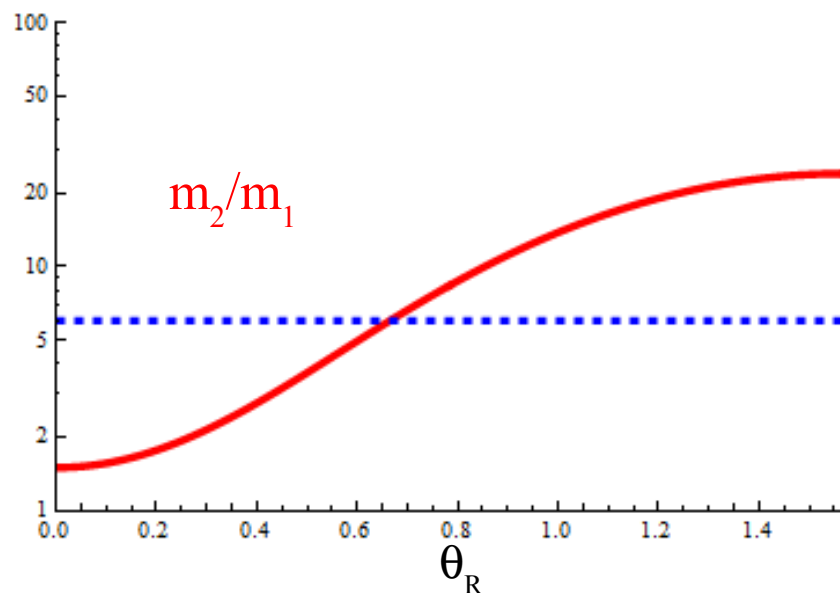
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Very strong hierarchy in RH masses

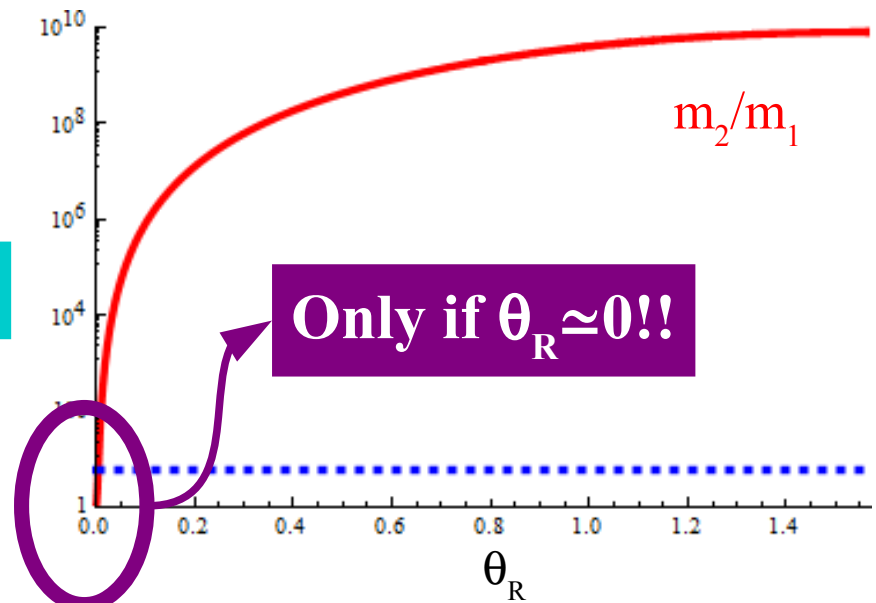
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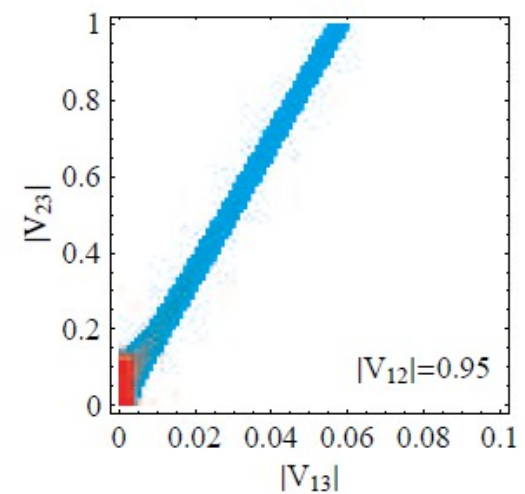
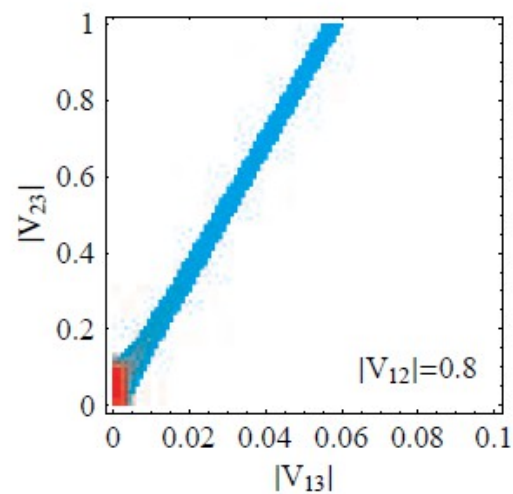
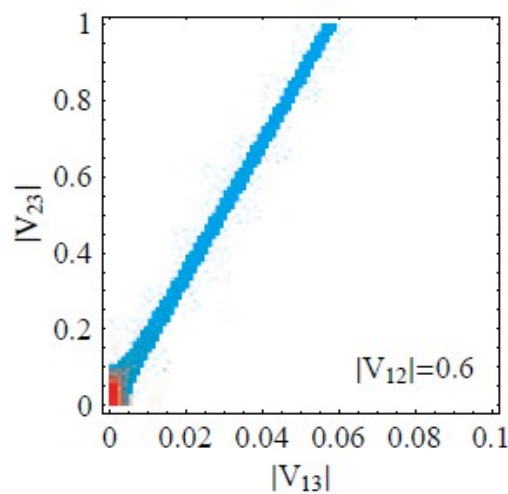
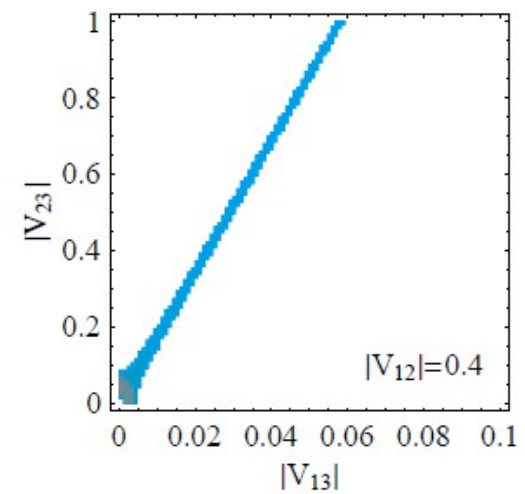
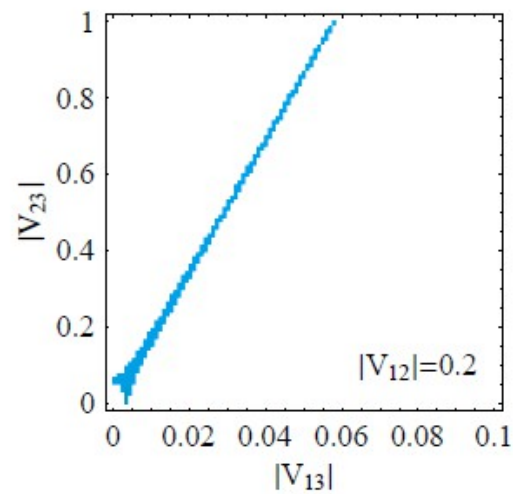
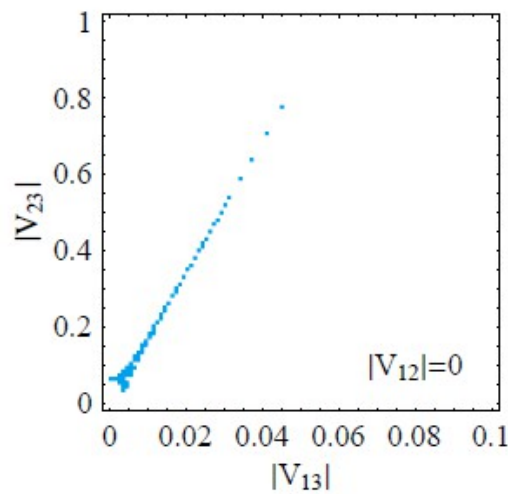


Only if $\theta_R \simeq 0!!$

The case with **three** right-handed neutrinos

$$y_1 : y_2 : y_3 = 1 : 300 : 300^2$$

$$M_1 : M_2 : M_3 = 1 : 300 : 300^2$$



No tuning

fine tuning

The see-saw mechanism generates a neutrino mass hierarchy much larger than the observed experimentally, except:

- When the Yukawa eigenvalues and right-handed masses present a mild mass hierarchy.
- In the case of hierarchical Yukawa eigenvalues, for very special choices of the parameters.

The see-saw mechanism provides a very compelling explanation to the smallness of neutrino masses, while keeping all the successes of the Standard Model. However, it fails to provide a compelling explanation to why the neutrino mass hierarchy is so mild.

A possible solution: Introduce a second higgs doublet

With a second higgs doublet, quantum corrections can soften the neutrino mass hierarchy.

Even if at tree level m_3/m_2 is very large, as generically expected in the (standard) see-saw mechanism, the quantum corrections can generate $m_3/m_2 \sim 6$.

Grimus, Neufeld
AI, Simonetto

Neutrino masses in the see-saw model extended with one extra Higgs

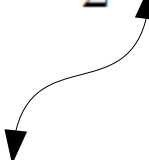
Consider the Standard Model extended by right-handed neutrinos and at least one extra Higgs doublet (no ad-hoc discrete symmetries)

$$-\mathcal{L}^\nu = (Y_\nu^a)_{ij} \bar{l}_{Li} \nu_{Rj} \tilde{\Phi}_a - \frac{1}{2} M_{Mij} \bar{\nu}_{Ri}^C \nu_{Rj} + \text{h.c.}$$



$$M_{Maj} \gg m_H, M_Z$$

$$-\mathcal{L}^{\nu, \text{eff}} = \frac{1}{2} \kappa_{ij}^{ab} (\bar{l}_{Li} \tilde{\Phi}_a) (\tilde{\Phi}_b^T l_{Lj}^C) + \text{h.c.}$$


$$\kappa^{ab}(M_1) = (Y_\nu^a M_M^{-1} Y_\nu^{bT})(M_1)$$

Work in the basis where only Φ_1 acquires a vev

$$\mathcal{M}_\nu(M_1) = \frac{v^2}{2} \kappa^{11}(M_1)$$

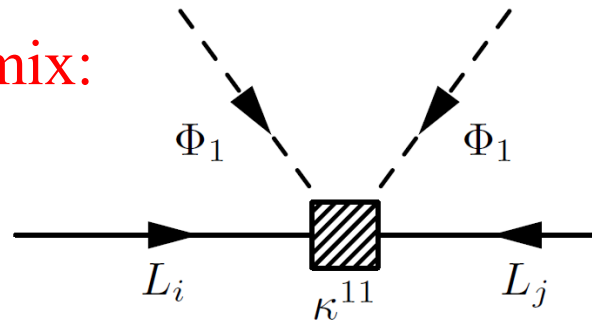
The neutrino mass matrix is affected by quantum corrections below M_1

RGE effects

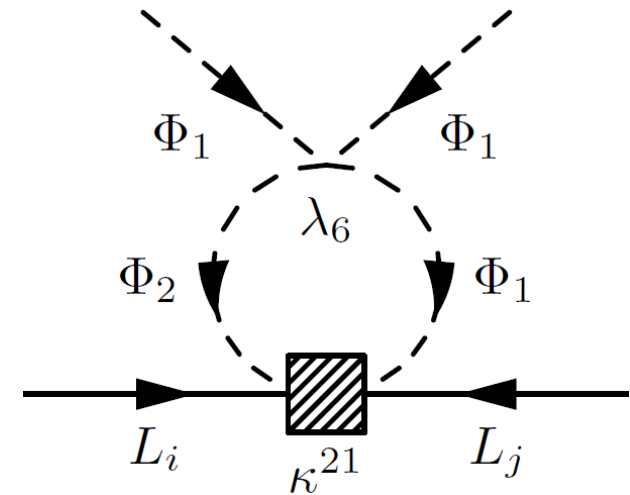
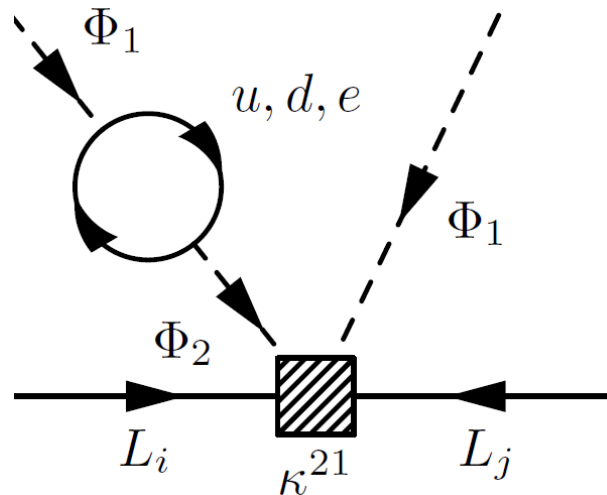
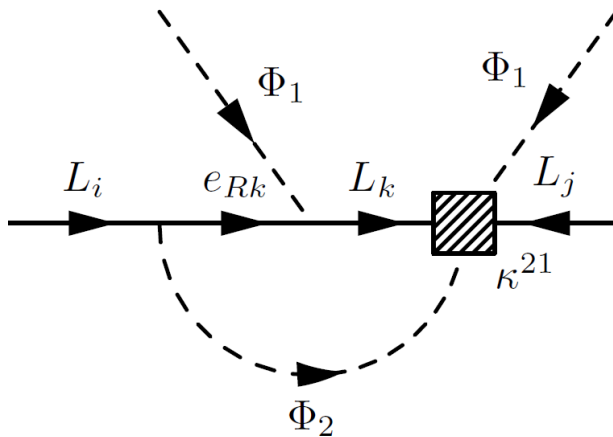
Quantum effects generate a correction to the coefficient of the dimension 5 operator which generates neutrino masses:

$$\delta\kappa^{11} \simeq B_{1a}\kappa^{a1} + \kappa^{1a}B_{1a}^T + b\kappa^{22} \quad \text{Grimus, Lavoura}$$

Different operators mix:



Is corrected by $B_{12}\kappa^{21}$

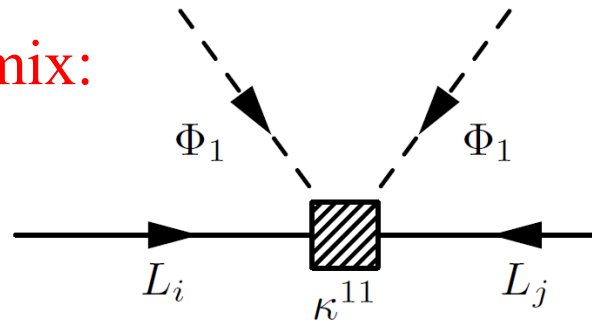


RGE effects

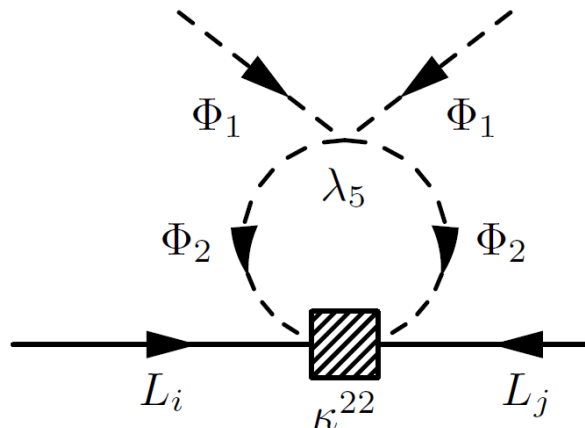
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Different operators mix.

Compare to the correction in the “one Higgs doublet model”:

$$\delta\kappa \simeq B\kappa + \kappa B^T$$

New qualitative features?

To highlight the new features, consider a model with one right-handed neutrino and two Higgs doublets (no ad-hoc discrete symmetries imposed):

$$-\mathcal{L}^\nu = (Y_\nu^1)_i \bar{l}_{Li} \nu_R \tilde{\Phi}_1 + (Y_\nu^2)_i \bar{l}_{Li} \nu_R \tilde{\Phi}_2 - \frac{1}{2} M_{\text{Maj}} \bar{\nu}_R^C \nu_R + \text{h.c.}$$



$$M_{\text{Maj}} \gg m_H, M_Z$$

$$-\mathcal{L}^{\nu, \text{eff}} = \frac{1}{2} \kappa_{ij}^{ab} (\bar{l}_{Li} \tilde{\Phi}_a) (\tilde{\Phi}_b^T l_{Lj}^C) + \text{h.c.}$$

Work in the basis where only Φ_1 acquires a vev

$$\mathcal{M}_\nu(M_{\text{Maj}}) = \frac{v^2}{2} \kappa^{11}(M_{\text{Maj}})$$

Rank 1. At tree level

$$m_3 = \frac{|Y_\nu^1|^2 v^2}{2M_{\text{Maj}}}$$

$$m_2, m_1 = 0$$

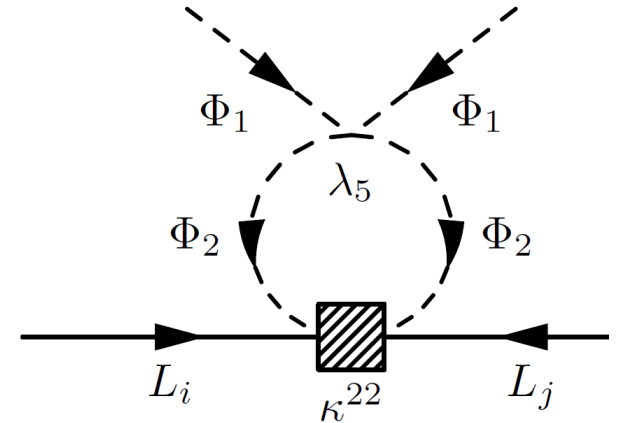
RGE effects

$$\delta\kappa^{11} \simeq B_{1a}\kappa^{a1} + \kappa^{1a}B_{1a}^T + b\kappa^{22}$$

$$m_3 = \frac{|Y_\nu^1|^2 v^2}{2M_{\text{maj}}} + \text{small corrections}$$

$$m_2 = \frac{1}{16\pi^2} \frac{|\lambda_5| v^2}{M_{\text{maj}}} \left[|Y_\nu^2|^2 - \frac{|Y_\nu^{2\dagger} Y_\nu^1|^2}{|Y_\nu^1|^2} \right] \log \frac{M_{\text{maj}}}{m_H}$$

$$m_1 = 0$$



A second neutrino mass is generated from the same right-handed neutrino mass scale $M_{\text{maj}} \rightarrow$ **a mild mass hierarchy might be naturally accommodated.**

$$m_3 = \frac{|Y_\nu^1|^2 v^2}{2M_{\text{maj}}}$$

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Neutrino mass hierarchy:

Assume:

- M_{maj} large, to implement the see-saw mechanism
 $m_H \ll M_{\text{maj}}$ (e.g $m_H = 100 \text{ GeV} - 1 \text{ TeV}$)
- Neutrino Yukawa couplings misaligned (new sources of flavour violation are required)
- $|Y_\nu^1| \sim |Y_\nu^2|$
- $\lambda_5 \sim \mathcal{O}(1)$

$$\left| \frac{m_2}{m_3} \right| \simeq \frac{|\lambda_5|}{8\pi^2} \frac{|Y_\nu^2|^2}{|Y_\nu^1|^2} \log \left(\frac{M_{\text{maj}}}{m_H} \right) \simeq 0.2$$

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$$m_2 = -\frac{1}{16\pi^2} \frac{|\lambda_5| v^2}{M_{\text{maj}}} \left[|Y_\nu^2|^2 - \frac{|Y_\nu^{2\dagger} Y_\nu^1|^2}{|Y_\nu^1|^2} \right] \log \left(\frac{M_{\text{maj}}}{m_H} \right)$$

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Yukawa couplings to the same generation of right-handed neutrinos (more details later)

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$$m_3 = \frac{|Y_\nu^1|^2 v^2}{2M_{\text{maj}}}$$

$$m_2 = -\frac{1}{2} \frac{|\lambda_5| v^2}{M_{\text{maj}}} \left[\frac{|Y_\nu^2|^2}{|Y_\nu^1|^2} \right] \left(\frac{M_{\text{maj}}}{m_H} \right)$$

**LEPTON FLAVOUR VIOLATION?
ELECTRIC DIPOLE MOMENTS?**

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**Logarithmic dependence with m_H ,
while the rate for $\mu \rightarrow e\gamma$ decreases as m_H^4**

$$\left| \frac{m_2}{m_3} \right| \simeq \frac{|\lambda_5|}{8\pi^2} \frac{|Y_\nu^2|^2}{|Y_\nu^1|^2} \log \left(\frac{M_{\text{maj}}}{m_H} \right) \simeq 0.2$$

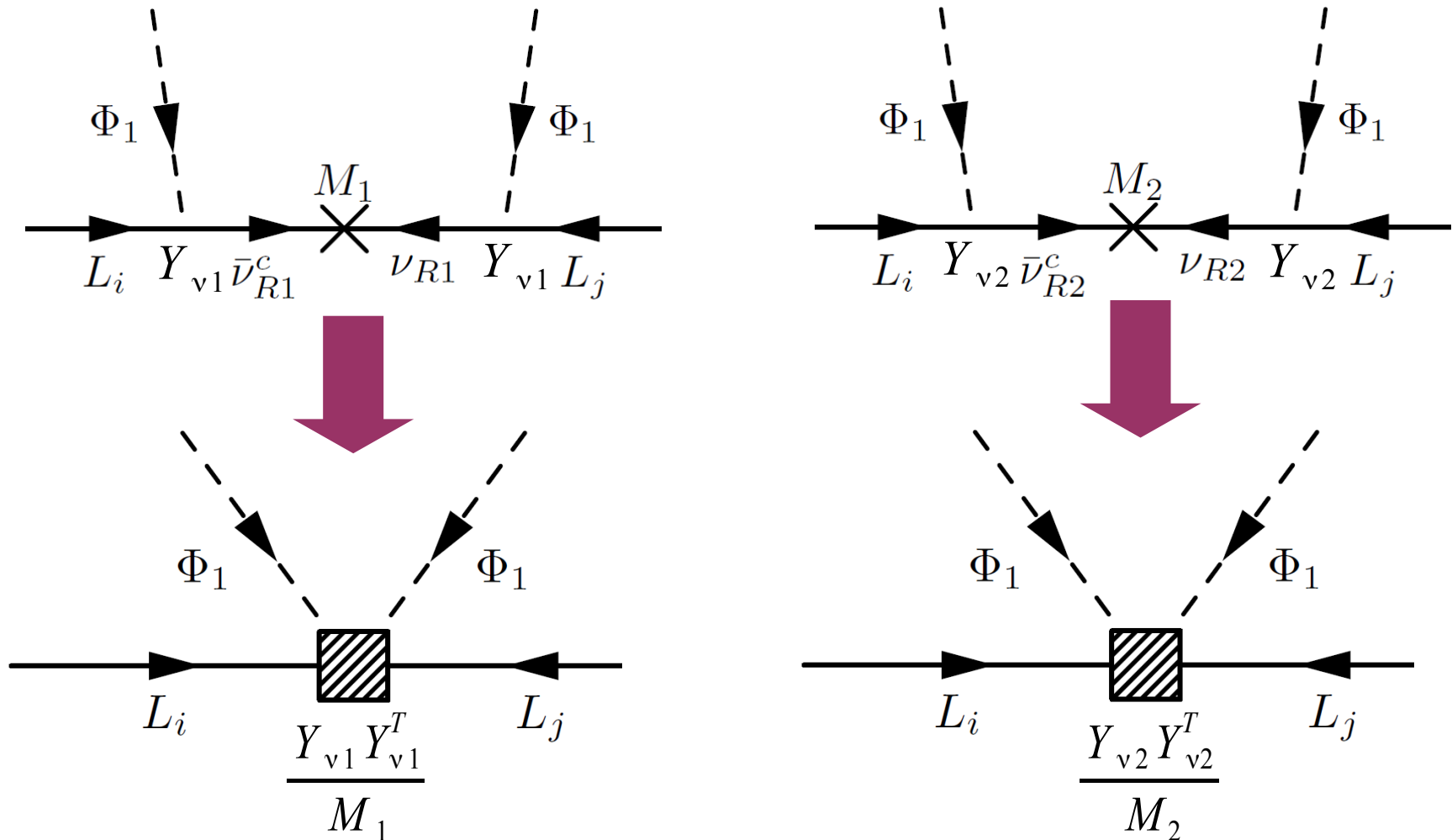
Messages to take home:

The Standard Model extended with ≥ 1 right-handed neutrino and ≥ 1 Higgs doublet can naturally explain the smallness of neutrino masses and the existence of a mild mass hierarchy, **without jeopardizing any of the successes of the Standard Model, since all extra particles decouple at low energies.**

No need to introduce flavour symmetries to explain the intergenerational mass differences in the neutrino sector, although they might be necessary to explain the observed pattern of mixing angles.

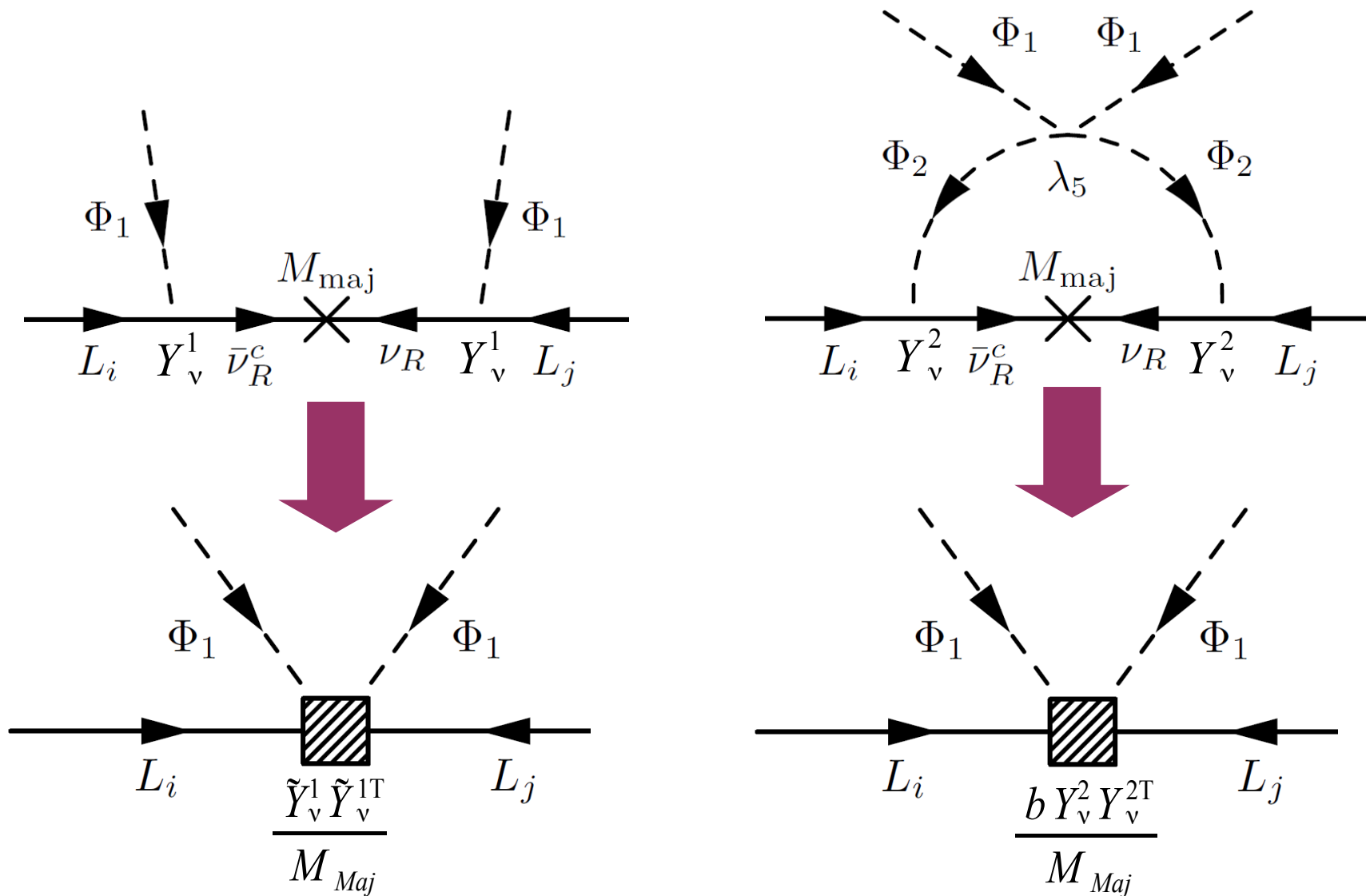
Comparison to the two right-handed neutrino model

Effective theory of the 2RHN-1HDM



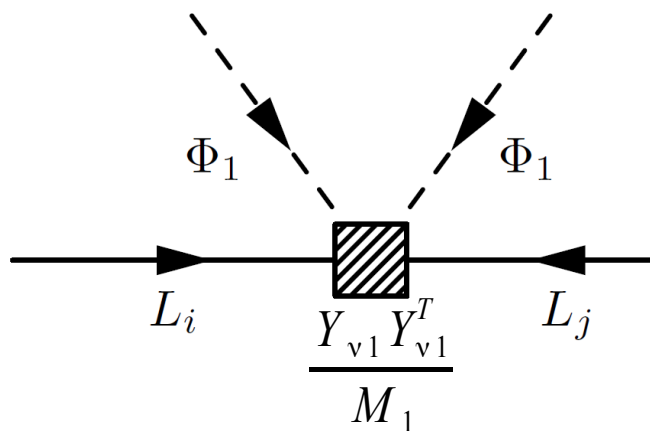
Comparison to the two right-handed neutrino model

Effective theory of the 1RHN-2HDM

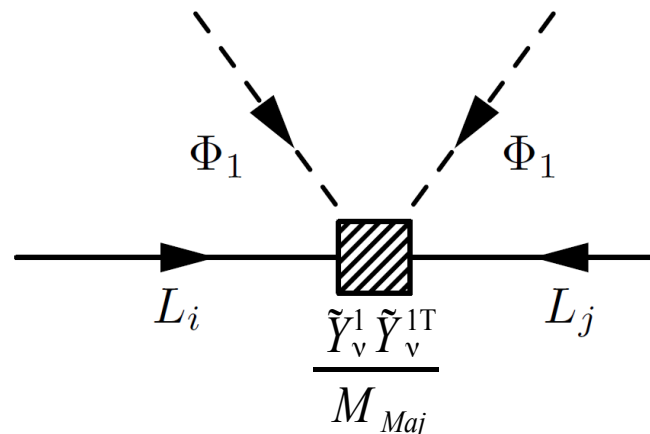
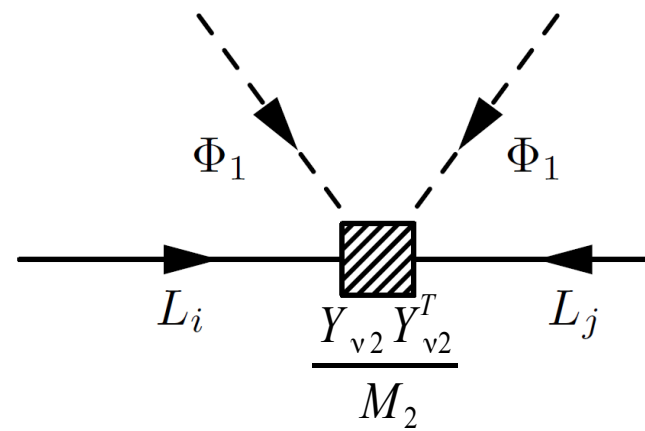


$$\tilde{Y}_v^1 = Y_v^1 + B_{1a} Y_v^a$$

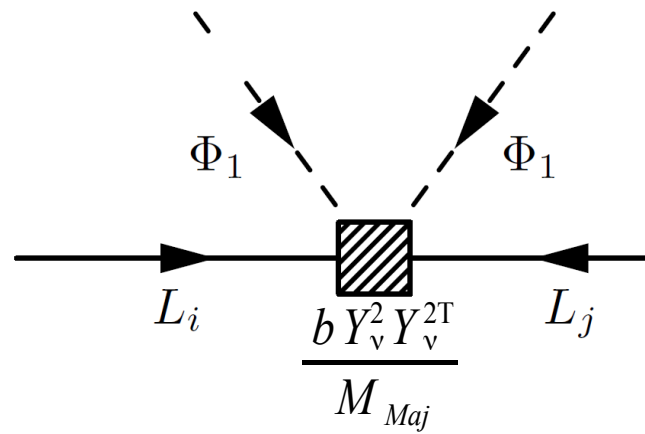
The effective theories are identical



2RHN-1HDM



1RHN-2HDM



The effective theories are identical



$$\{Y_{\nu 1}, Y_{\nu 2}, M_1, M_2\} \leftrightarrow \{\tilde{Y}_{\nu}^1, Y_{\nu}^2, M_{Maj}, M_{Maj}/b\}$$



However, there are important differences in the way the can generate the mild neutrino mass hierarchy.


First part of the talk: the 2RHN-1HDM can generate a neutrino mass hierarchy in agreement with experiments when:

- When the Yukawa eigenvalues *and* right-handed masses present a mild hierarchy.
- When there are hierarchical Yukawa eigenvalues, only for very special choices of the parameters.

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2RHN-1HDM

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Yukawa couplings to *different* generation of RH neutrinos.
Possibly hierarchical eigenvalues

Two different right-handed neutrino masses.
Hierarchy completely unknown

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implausible

tuned?

2RHN-1HDM

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2RHN-1HDM

1RHN-2HDM

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$$b = -\frac{\lambda_5}{8\pi^2} \log \left(\frac{M_{Maj}}{m_H} \right)$$

Yukawa couplings to *the same* generation of RH neutrinos.
Eigenvalues expected to be similar

The “equivalent” right-handed neutrino masses naturally have a mild hierarchy.

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←
Generic
situation in
1RHN-2HDM

2RHN-1HDM

1RHN-2HDM

$$\{Y_{\nu 1}, Y_{\nu 2}, M_1, M_2\} \leftrightarrow \{\underbrace{\tilde{Y}_{\nu}^1, Y_{\nu}^2}_{\text{Yukawa couplings}}, \underbrace{M_{\text{Maj}}, M_{\text{Maj}}/b}_{\text{right-handed masses}}\}$$

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Yukawa couplings to *the same* generation of RH neutrinos.
Eigenvalues expected to be similar

The “equivalent” right-handed neutrino masses naturally have a mild hierarchy.

A remarkable difference with respect to the two right-handed neutrino model:

*Possibly, new phenomena at low energies,
apart from neutrino masses*

LFV processes could be observable, if not too suppressed by m_H .

$$\text{BR}(\mu \rightarrow e \gamma) = \frac{8\alpha^3}{3\pi^3} \frac{|Y_{e12}^2|^2 + |Y_{e21}^2|^2}{|Y_{e22}^1|^2} \left| f\left(\frac{m_t^2}{m_h^2}\right) \cos \alpha - \frac{Y_{u33}^2}{Y_{u33}^1} \frac{m_t^2}{m_H^2} \log^2 \frac{m_t^2}{m_H^2} \right|^2$$

Paradisi
Hisano, Sugiyama, Yamanaka

Could be present at tree level.

If not, generated radiatively by the neutrino Yukawa couplings

Mixing angles

New flavour structures in κ^{22} and Y_e^2 modify, through quantum corrections, the flavour structure of the neutrino mass operator κ^{11} and the charged lepton Yukawa coupling Y_e^1 .

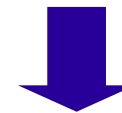
Leptonic mixing matrix



$$\delta U_\kappa = U^{(0)} T$$

Charged lepton
Yukawa coupling

$$l_L \rightarrow V_e^L l_L$$



$$\delta U_{Y_e} = (V_e^L - \mathbb{1})^T U^{(0)}$$

Summing up both contributions

$$U^{(1)} = V_e^L T U^{(0)} + U^{(0)} T$$

Mixing angles: effect on θ_{13} and θ_{23}

New flavour structures in κ^{22} and Y_e^2 can induce radiatively a non-vanishing θ_{13} and a deviation from maximal atmospheric mixing.

$$\begin{aligned}\delta U_{13} = & -\frac{1}{16\pi^2} \frac{Y_{\nu 1}^{2*}}{|Y_\nu^1|} \left[3\text{Tr}(Y_u^{1\dagger} Y_u^2 + Y_d^1 Y_d^{2\dagger}) + 2\lambda_6^* + 2\lambda_5^* \frac{Y_\nu^{2\dagger} Y_\nu^1}{|Y_\nu^1|^2} \right] \log \frac{M_{\text{maj}}}{m_H} \\ & + \frac{1}{16\pi^2} \frac{(Y_\nu^{1\dagger} (Y_e^1)^{-1} Y_e^{2\dagger})_1}{|Y_\nu^1|} \left[3\text{Tr}(Y_u^{2\dagger} Y_u^1 + Y_d^2 Y_d^{1\dagger}) \right] \log \frac{M_{\text{maj}}}{m_H}\end{aligned}$$

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Similar to $m_2/m_3 \rightarrow \delta U_{13}$ can easily be ~ 0.2

Mixing angles: effect on θ_{13} and θ_{23}

New flavour structures in κ^{22} and Y_e^2 can induce radiatively a non-vanishing θ_{13} and a deviation from maximal atmospheric mixing.

Additional effects if the cut-off Λ is larger than M_{maj} , through the quantum effects from the neutrino Yukawa couplings Y_ν^1, Y_ν^2 .

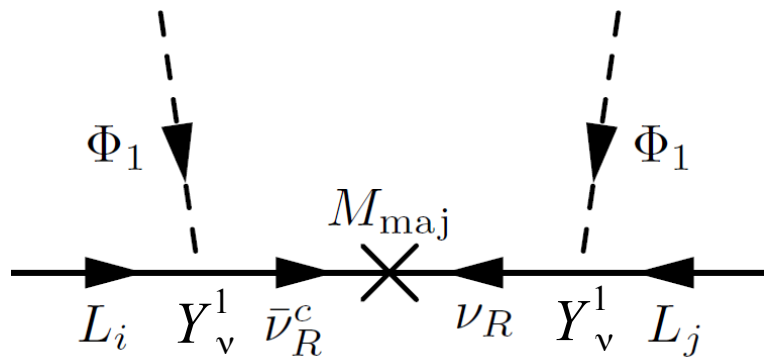
$$\begin{aligned} \delta U_{13} = & -\frac{1}{16\pi^2} \frac{Y_{\nu 1}^{2*}}{|Y_\nu^1|} \left\{ \left[3\text{Tr}(Y_u^{1\dagger} Y_u^2 + Y_d^1 Y_d^{2\dagger}) + \text{Tr}(Y_\nu^2 Y_\nu^{1\dagger}) + 2Y_\nu^{1\dagger} (Y_e^1)^{-1} Y_e^{2\dagger} Y_\nu^1 \right] \log \frac{\Lambda}{M_{\text{maj}}} \right. \\ & \left. + \left[3\text{Tr}(Y_u^{1\dagger} Y_u^2 + Y_d^1 Y_d^{2\dagger}) + 2\lambda_6^* + 2\lambda_5^* \frac{Y_\nu^{2\dagger} Y_\nu^1}{|Y_\nu^1|^2} \right] \log \frac{M_{\text{maj}}}{m_H} \right\} \\ & + \frac{1}{16\pi^2} \frac{(Y_\nu^{1\dagger} (Y_e^1)^{-1} Y_e^{2\dagger})_1}{|Y_\nu^1|} \left\{ \text{Tr}(Y_\nu^{2\dagger} Y_\nu^1) \log \frac{\Lambda}{M_{\text{maj}}} + 3\text{Tr}(Y_u^{2\dagger} Y_u^1 + Y_d^2 Y_d^{1\dagger}) \log \frac{\Lambda}{m_H} \right\} \end{aligned}$$

Some speculations about the mixing angles

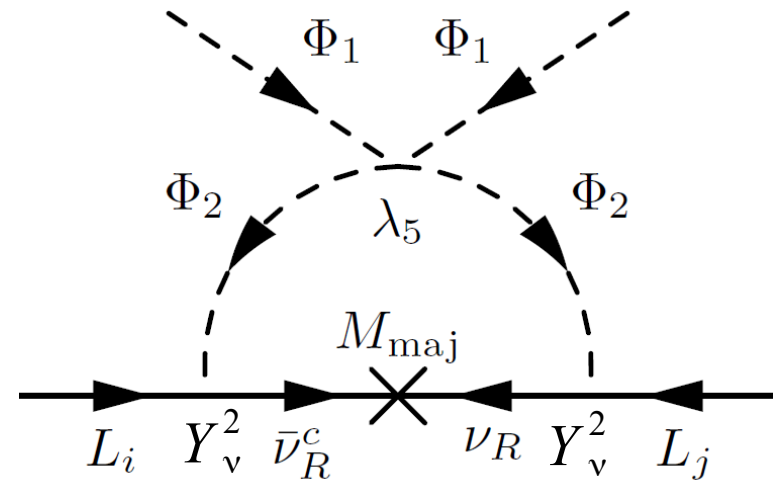
The third column of the leptonic mixing matrix seems to follow a pattern, at least at lowest order: $\theta_{13}=0$, $\theta_{23}=\pi/4$. $U_{i3} \approx \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}$

The second column does not seem to follow any pattern: the solar mixing angle is neither minimal nor maximal. $U_{i2} \approx \begin{pmatrix} O(1) \\ O(1) \\ O(1) \end{pmatrix}$

In the **1RHN-2HDM**



Third column of U_{lep}
Possibly with a pattern
(if Y_v^1 has a pattern)



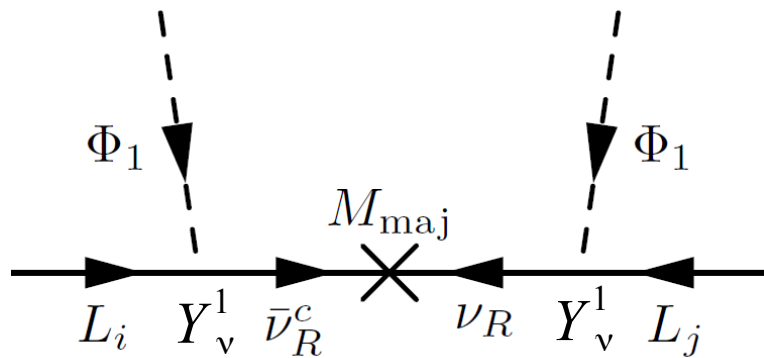
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Possibly with a pattern
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Some speculations about the mixing angles

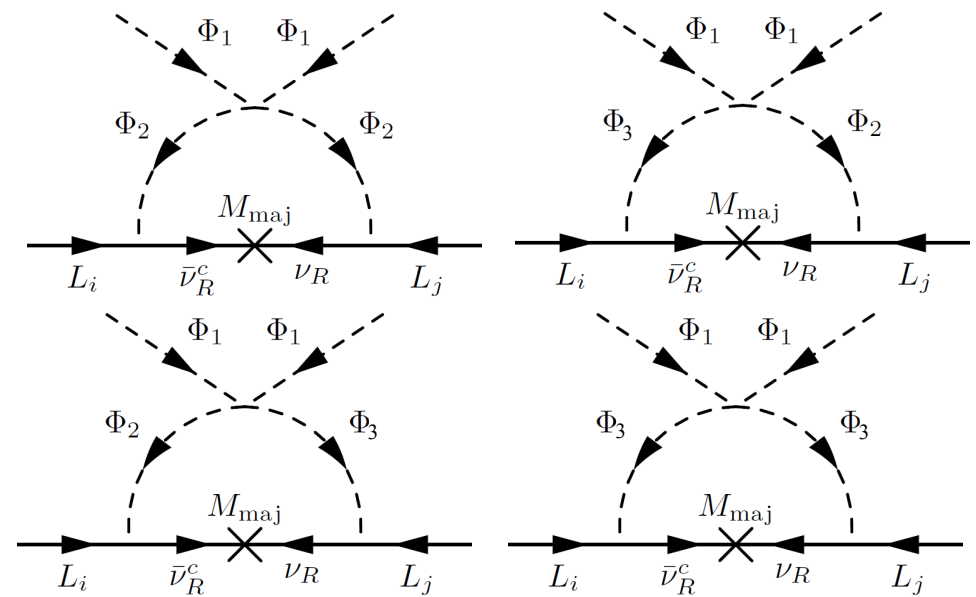
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In the **1RHN-3HDM**,
(more higgs doublets!)



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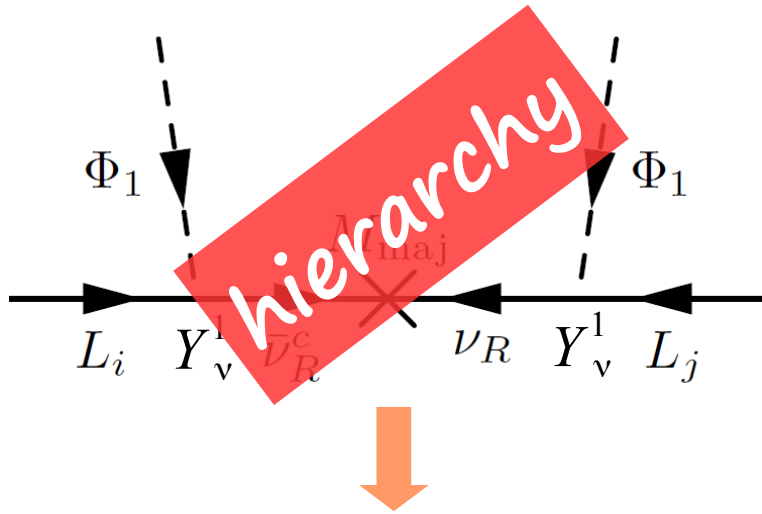
second column of U_{lep}
Even if each Yukawa coupling
had an structure, the combination
of them gives a “structureless” U_{i2} .

Some speculations about the mixing angles

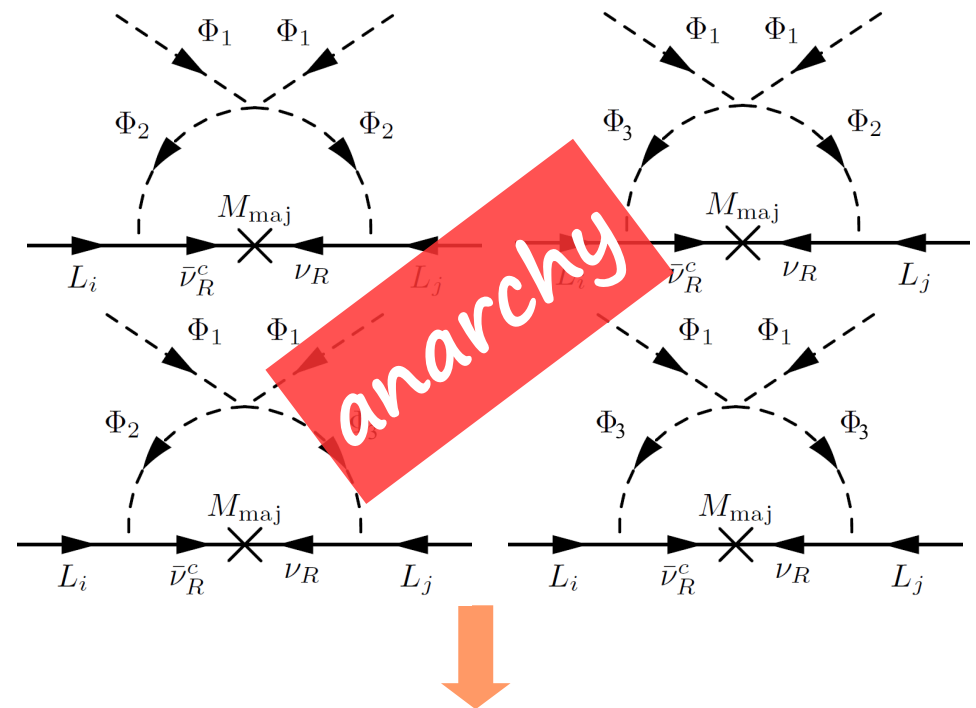
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In the **1RHN-3HDM**,
(more higgs doublets!)



Third column of U_{lep}
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(if Y_{ν}^{-1} has a pattern)



second column of U_{lep}
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The dark matter connection

The explanation of the observed neutrino flavour transitions and the nature of the dark matter of the Universe could be completely unrelated problems.

The dark matter connection

The explanation of the observed neutrino flavour transitions and the nature of the dark matter of the Universe could be completely unrelated problems.

Or perhaps not...

Ma's model

Phys.Rev. D73 (2006) 077301

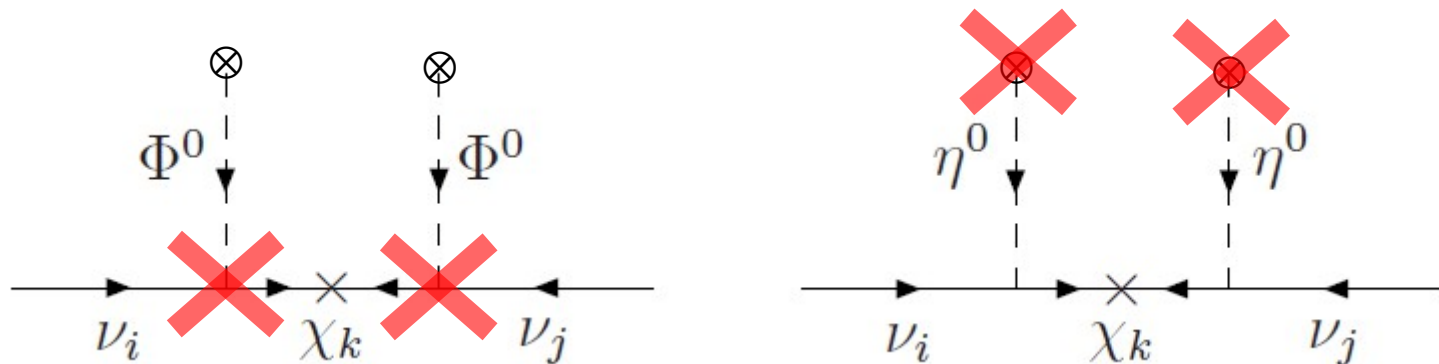
	L_1, L_2, L_3	e_{R1}, e_{R2}, e_{R3}	Φ	χ_1, χ_2, χ_3	η
spin	1/2	1/2	0	1/2	0
$SU(2)_L \times U(1)_Y$	(2, -1/2)	(1, 1)	(2, 1/2)	(1, 0)	(2, 1/2)
Z_2	+	+	+	-	-

If the Z_2 symmetry is exact (or very weakly broken) the model contains a dark matter candidate (η or χ_1).

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Z_2	+	+	+	-	-

If the Z_2 symmetry is exact (or very weakly broken) the model contains a dark matter candidate (η or χ_1).

Due to the Z_2 symmetry, η does not acquire a vev \rightarrow no neutrino mass at tree level.

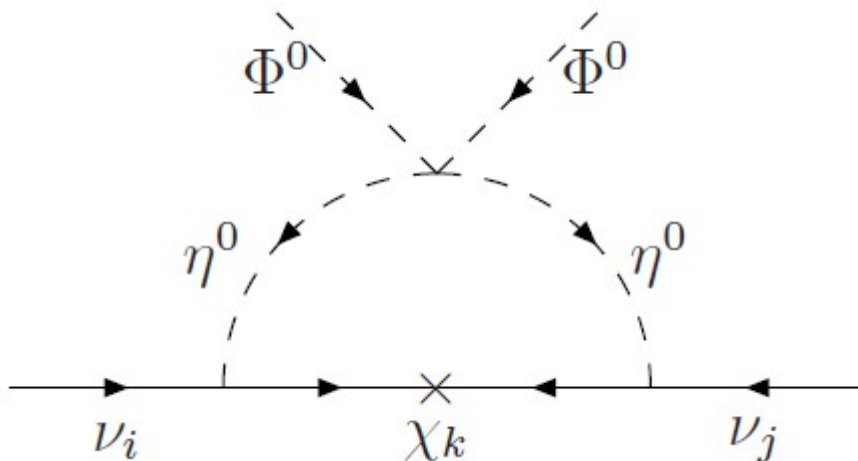


	L_1, L_2, L_3	e_{R1}, e_{R2}, e_{R3}	Φ	χ_1, χ_2, χ_3	η
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Z_2	+	+	+	-	-

If the Z_2 symmetry is exact (or very weakly broken) the model contains a dark matter candidate (η or χ_1).

Due to the Z_2 symmetry, η does not acquire a vev \rightarrow no neutrino mass at tree level.

All neutrino masses are generated at the one loop level



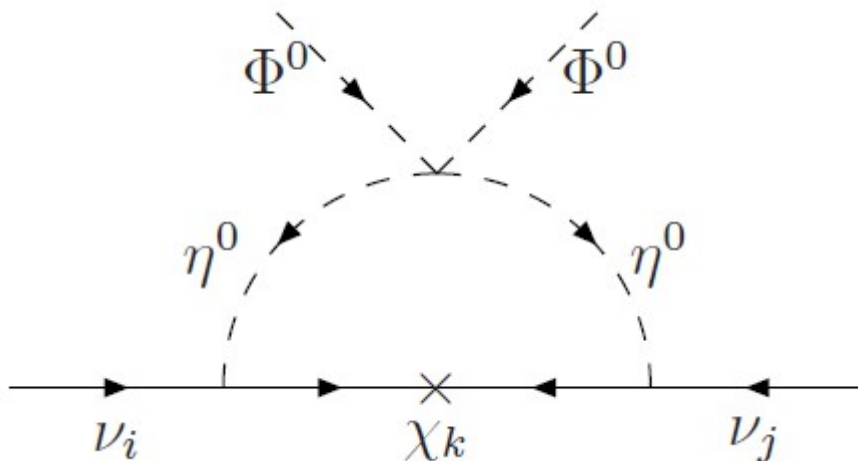
For appropriate choices of the parameters, the masses of the new particles could be at the TeV scale
 \rightarrow Collider signatures

	L_1, L_2, L_3	e_{R1}, e_{R2}, e_{R3}	Φ	χ_1, χ_2, χ_3	η
spin	1/2	1/2	0	1/2	0
$SU(2)_L \times U(1)_Y$	(2, -1/2)	(1, 1)	(2, 1/2)	(1, 0)	(2, 1/2)
Z_2	+	+	+	-	-

If the Z_2 symmetry is exact (or very weakly broken) the model contains a dark matter candidate (η or χ_1).

Due to the Z_2 symmetry, η does not acquire a vev \rightarrow no neutrino mass at tree level.

All neutrino masses are generated at the one loop level



If $M_k^2 \gg m_0^2$, then

$$(\mathcal{M}_\nu)_{ij} = \frac{\lambda_5 v^2}{8\pi^2} \sum_k \frac{h_{ik} h_{jk}}{M_k} \left[\ln \frac{M_k^2}{m_0^2} - 1 \right].$$

However, the model generically predicts large neutrino mass hierarchies

Our modification

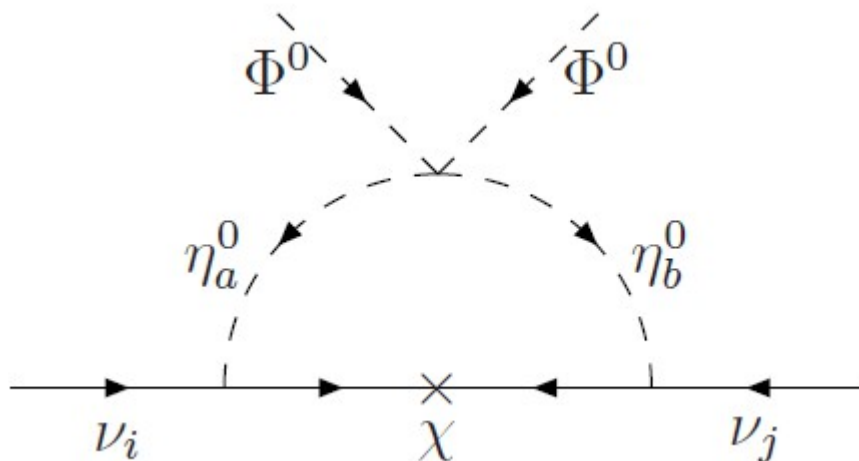
Hehn, AI, arXiv:1208.3162

	L_1, L_2, L_3	e_{R1}, e_{R2}, e_{R3}	Φ	χ	η_1, η_2
spin	1/2	1/2	0	1/2	0
$SU(2)_L \times U(1)_Y$	(2, -1/2)	(1, 1)	(2, 1/2)	(1, 0)	(2, 1/2)
Z_2	+	+	+	-	-

If the Z_2 symmetry is exact (or very weakly broken) the model contains a dark matter candidate (η_1 or χ).

Due to the Z_2 symmetry, η_1, η_2 do not acquire a vev \rightarrow no neutrino mass at tree level.

All neutrino masses are generated at the one loop level

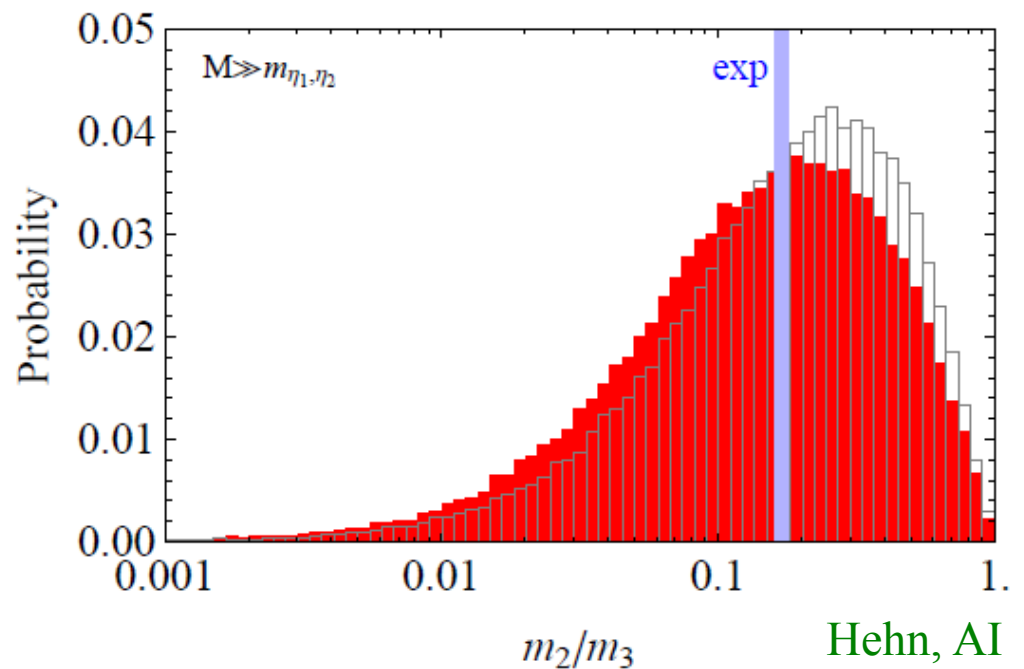
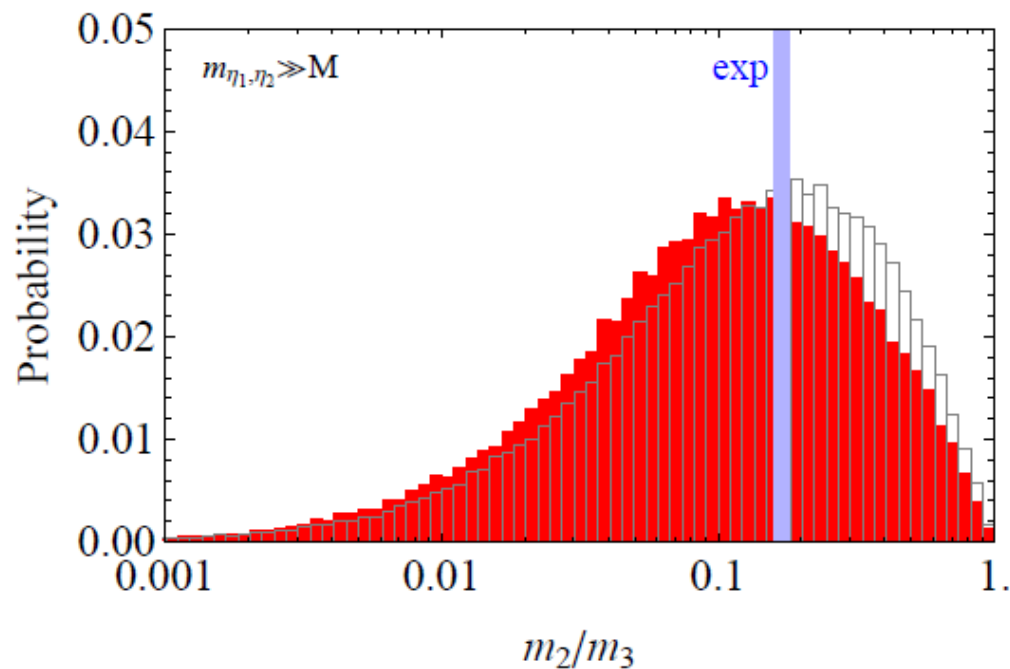


$$(\mathcal{M}_\nu)_{ij} \simeq - \frac{Y_i^{(a)} Y_j^{(b)} \lambda_5^{(ab)} v^2}{8\pi^2} \frac{1}{M} \times \left\{ \frac{m_{\eta_b}^2}{m_{\eta_a}^2 - m_{\eta_b}^2} \log \frac{m_{\eta_a}^2}{m_{\eta_b}^2} + \log \frac{m_{\eta_a}^2}{M^2} \right\}$$

$$|Y^{(1)}| \sim |Y^{(2)}| \text{ (coupling to the same } \chi \text{)}$$

$$\lambda_5^{(11)} \sim \lambda_5^{(12)} \sim \lambda_5^{(22)}$$

Mild mass hierarchy generically expected



Features:

- Small neutrino mass due to the see-saw mechanism.
- Mild neutrino mass hierarchy due to the presence of a second scalar doublet.
- No need to invoke a flavor symmetry to explain the intergenerational mass hierarchy in the neutrino sector, although it might be necessary to explain the pattern of mixing angles.
- The model contains a dark matter candidate and can generate the observed matter-antimatter asymmetry in the Universe through leptogenesis

Conclusions

	SM	SM + heavy RH neutrinos
Flavour, CP, ECPD		
Tiny neutrino masses		
Mild ν mass hierarchy		
Neutrino Mixing angles		
Baryogenesis		
Dark matter		
Strong CP problem		
Hierarchy problem		
Cosmological constant problem		

Conclusions

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Thank you for your attention!