

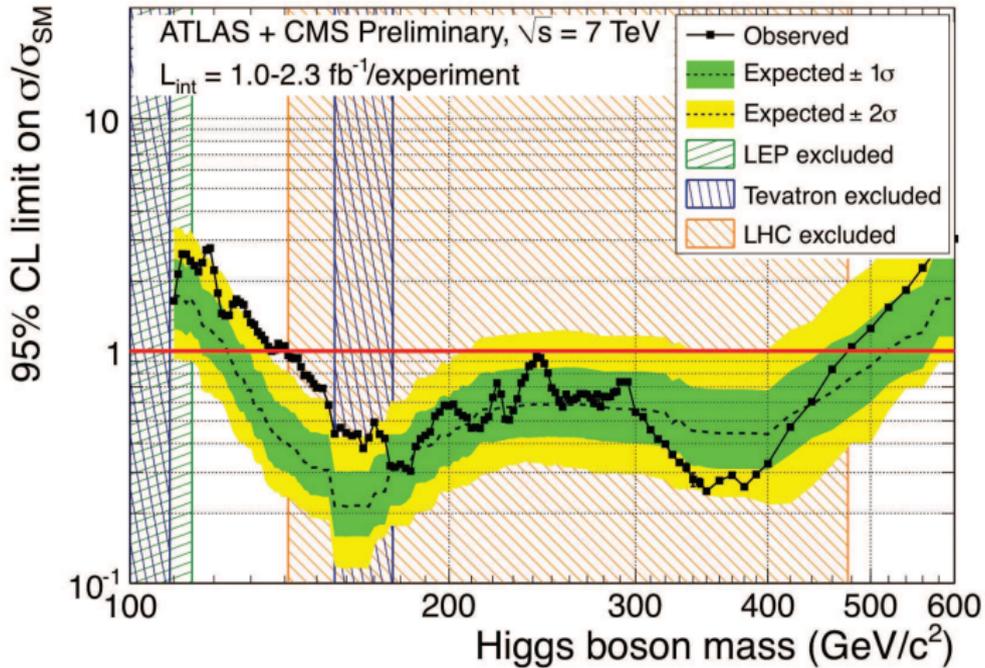
Constraints on Multi-Higgs-Doublet Models: Flavour Alignment

Antonio Pich

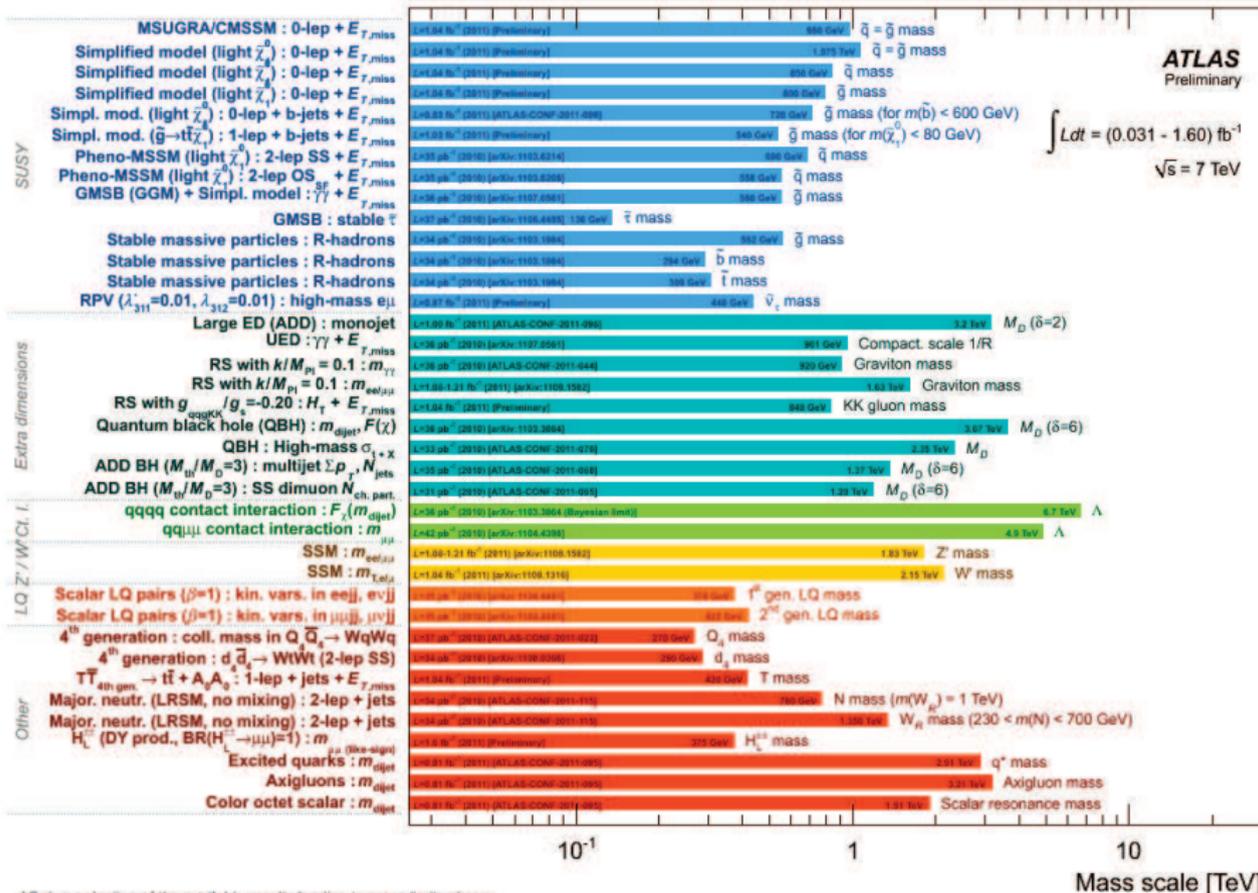
IFIC, Univ. Valencia - CSIC



HCP 11, Paris, 18 November 2011

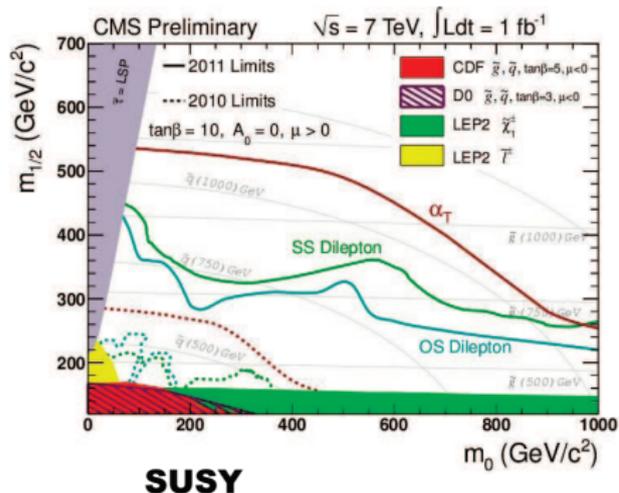


Excluded: $M_{\text{H}} (\text{GeV}) \in [141, 476]$



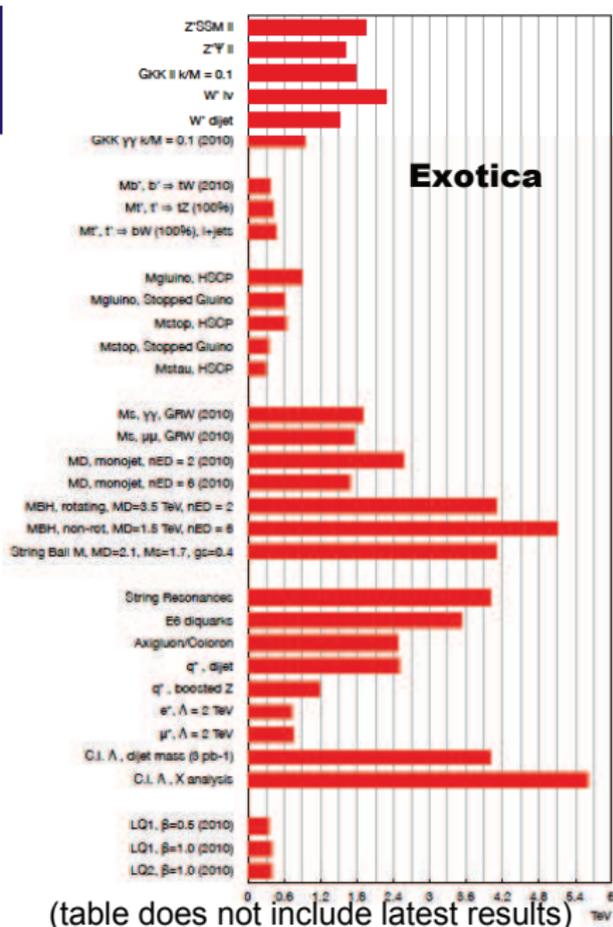
*Only a selection of the available results leading to mass limits shown

Summary (CMS)



(only a selection of results)

Henri Bachacou, Irfu CEA-Saclay



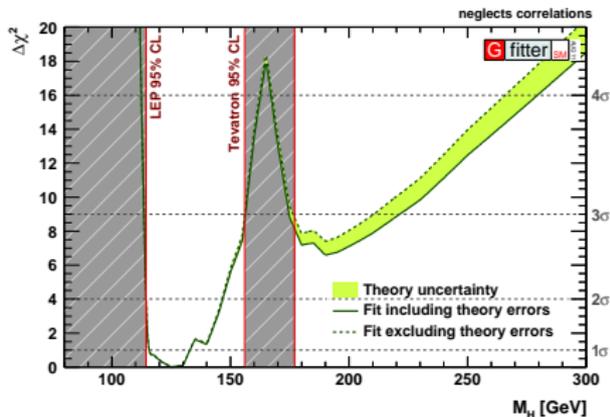
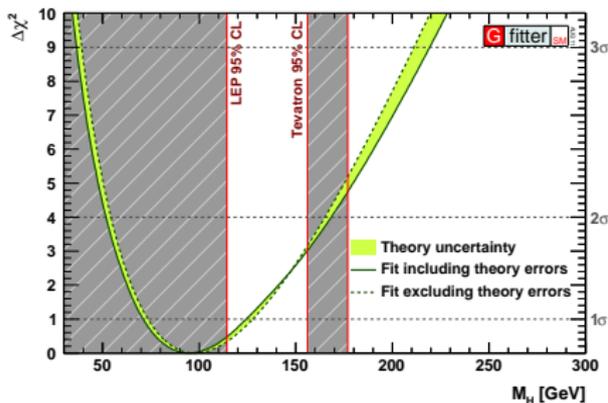
Lepton-Photon 2011

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Possible Scenarios:

① Light SM Higgs:

$$M_H \text{ (GeV)} \in [114.4, 141]$$



Favoured by EW precision tests

Possible Scenarios:

① Light SM Higgs.

Favoured by EW precision tests

② Alternative perturbative EW SSB.

Scalar Doublets and singlets (ρ)

③ Heavy Higgs.

Non-perturbative EW SSB

④ No Higgs.

Dynamical EW SSB

Standard Model

$$\bar{Q}'_L \equiv (\bar{u}'_L, \bar{d}'_L) \quad , \quad \tilde{\Phi} \equiv i\tau_2 \Phi^*$$

One Higgs Doublet $\Phi = \begin{pmatrix} \phi^{(+)} \\ \phi^{(0)} \end{pmatrix}$, $\langle 0|\Phi|0\rangle = \begin{pmatrix} 0 \\ \frac{v}{\sqrt{2}} \end{pmatrix}$

$$\mathcal{L}_Y = -\bar{Q}'_{iL} \Gamma_{ij} \Phi d'_{jR} - \bar{Q}'_{iL} \Delta_{ij} \tilde{\Phi} u'_{jR} - \bar{L}'_{iL} \Pi_{ij} \Phi l'_{jR} + \text{h.c.}$$

↓ SSB

$$M'_d = \frac{v}{\sqrt{2}} \Gamma \quad , \quad M'_u = \frac{v}{\sqrt{2}} \Delta \quad , \quad M'_l = \frac{v}{\sqrt{2}} \Pi$$

Diagonalization \rightarrow $\left\{ \begin{array}{l} \text{GIM Mechanism (Unitarity)} \\ \text{Yukawas proportional to masses} \end{array} \right.$

No Flavour-Changing Neutral Currents

Two Higgs Doublets: ϕ_a ($a = 1, 2$)

$$\langle 0 | \phi_a^T(x) | 0 \rangle = \frac{1}{\sqrt{2}} (0, v_a e^{i\theta_a}) \quad , \quad \theta_1 = 0 \quad , \quad \theta \equiv \theta_2 - \theta_1$$

Higgs basis: $v \equiv \sqrt{v_1^2 + v_2^2}$, $\tan \beta \equiv v_2/v_1$

$$\begin{pmatrix} \Phi_1 \\ -\Phi_2 \end{pmatrix} \equiv \begin{bmatrix} \cos \beta & \sin \beta \\ \sin \beta & -\cos \beta \end{bmatrix} \begin{pmatrix} \phi_1 \\ e^{-i\theta} \phi_2 \end{pmatrix}$$

→ $\Phi_1 = \begin{bmatrix} G^+ \\ \frac{1}{\sqrt{2}} (v + S_1 + iG^0) \end{bmatrix}$, $\Phi_2 = \begin{bmatrix} H^+ \\ \frac{1}{\sqrt{2}} (S_2 + iS_3) \end{bmatrix}$

Mass eigenstates: H^\pm , $\varphi_i^0(x) \equiv \{h(x), H(x), A(x)\} = \mathcal{R}_{ij} S_j(x)$

Yukawa Interactions in 2HDMs

$$\mathcal{L}_Y = -\bar{Q}'_L (\Gamma_1 \phi_1 + \Gamma_2 \phi_2) d'_R - \bar{Q}'_L (\Delta_1 \tilde{\phi}_1 + \Delta_2 \tilde{\phi}_2) u'_R \\ - \bar{L}'_L (\Pi_1 \phi_1 + \Pi_2 \phi_2) l'_R + \text{h.c.}$$

↓ SSB

$$\mathcal{L}_Y = -\frac{\sqrt{2}}{v} \left\{ \bar{Q}'_L (M'_d \Phi_1 + Y'_d \Phi_2) d'_R + \bar{Q}'_L (M'_u \tilde{\Phi}_1 + Y'_u \tilde{\Phi}_2) u'_R \right. \\ \left. + \bar{L}'_L (M'_l \Phi_1 + Y'_l \Phi_2) l'_R + \text{h.c.} \right\}$$

M'_f and Y'_f unrelated → FCNCs

$$\sqrt{2} M'_d = v_1 \Gamma_1 + v_2 \Gamma_2 e^{i\theta} \quad , \quad \sqrt{2} M'_u = v_1 \Delta_1 + v_2 \Delta_2 e^{-i\theta}$$

$$\sqrt{2} Y'_d = v_1 \Gamma_2 e^{i\theta} - v_2 \Gamma_1 \quad , \quad \sqrt{2} Y'_u = v_1 \Delta_2 e^{-i\theta} - v_2 \Delta_1$$

Avoiding FCNCs

• Very large scalar masses \rightarrow THDM irrelevant at low energies

• Very small scalar couplings

• Type III model: $(Y_f)_{ij} \propto \sqrt{m_i m_j}$ Yukawa textures
(Cheng - Sher '87)

• Discrete \mathcal{Z}_2 symmetries: only one $\phi_a(x)$ couples to a given $f_R(x)$
(Glashow - Weinberg '77)

$$\mathcal{Z}_2: \quad \phi_1 \rightarrow \phi_1 \quad , \quad \phi_2 \rightarrow -\phi_2 \quad , \quad Q_L \rightarrow Q_L \quad , \quad L_L \rightarrow L_L \quad , \quad f_R \rightarrow \pm f_R$$



CP conserved in the scalar sector

Aligned 2HDM

(Pich - Tuzón '09)

Require alignment in Flavour Space of Yukawa couplings:

$$\Gamma_2 = \xi_d e^{-i\theta} \Gamma_1 \quad , \quad \Delta_2 = \xi_u^* e^{i\theta} \Delta_1 \quad , \quad \Pi_2 = \xi_l e^{-i\theta} \Pi_1$$



$$Y_{d,l} = s_{d,l} M_{d,l}, \quad Y_u = s_u^* M_u, \quad s_f \equiv \frac{\xi_f - \tan \beta}{1 + \xi_f \tan \beta}$$

$$\mathcal{L}_Y = -\frac{\sqrt{2}}{v} H^+ \left\{ \bar{u} \left[s_d V_{\text{CKM}} M_d \mathcal{P}_R - s_u M_u^\dagger V_{\text{CKM}} \mathcal{P}_L \right] d + s_l (\bar{\nu} M_l \mathcal{P}_R l) \right\} \\ - \frac{1}{v} \sum_{\varphi_i^0, f} y_f^{\varphi_i^0} \varphi_i^0 (\bar{f} M_f \mathcal{P}_R f) + \text{h.c.}$$

- Fermionic couplings proportional to fermion masses.
- Neutral Yukawas are diagonal in flavour

$$y_{d,l}^{\varphi_i^0} = \mathcal{R}_{i1} + (\mathcal{R}_{i2} + i \mathcal{R}_{i3}) \varsigma_{d,l} \quad , \quad y_u^{\varphi_i^0} = \mathcal{R}_{i1} + (\mathcal{R}_{i2} - i \mathcal{R}_{i3}) \varsigma_u^*$$

- V_{CKM} is the only source of flavour-changing phenomena
- All leptonic couplings are diagonal in flavour
- Only three new (universal) couplings ς_f .
- The usual Z_2 models are recovered in the limits $\xi_f \rightarrow 0, \infty$

The *inert* doublet model corresponds to $\varsigma_f = 0$ ($\xi_f = \tan \beta$)

- ς_f are arbitrary complex numbers

➡ New sources of CP violation without tree-level FCNCs

A2HDM: General phenomenological setting without tree-level FCNCs

$$\mathcal{L}_Y = -\frac{\sqrt{2}}{v} H^+ \left\{ \bar{u} \left[s_d V_{CKM} M_d \mathcal{P}_R - s_u M_u^\dagger V_{CKM} \mathcal{P}_L \right] d + s_l (\bar{\nu} M_l \mathcal{P}_R l) \right\} \\ - \frac{1}{v} \sum_{\varphi_i^0, f} y_f^{\varphi_i^0} \varphi_i^0 (\bar{f} M_f \mathcal{P}_R f) + \text{h.c.}$$

Z_2 models:

Model	s_d	s_u	s_l
Type I	$\cot \beta$	$\cot \beta$	$\cot \beta$
Type II	$-\tan \beta$	$\cot \beta$	$-\tan \beta$
Type X	$\cot \beta$	$\cot \beta$	$-\tan \beta$
Type Y	$-\tan \beta$	$\cot \beta$	$\cot \beta$
Inert	0	0	0

Quantum Corrections

$\mathcal{L}_{\text{A2HDM}}$ invariant under the phase transformation: $[\alpha'_i = \alpha'_i]$

$$f_L^i(x) \rightarrow e^{i\alpha_i^{f,L}} f_L^i(x) \quad , \quad f_R^i(x) \rightarrow e^{i\alpha_i^{f,R}} f_R^i(x)$$

$$V_{\text{CKM}}^{ij} \rightarrow e^{i\alpha_i^{u,L}} V_{\text{CKM}}^{ij} e^{-i\alpha_j^{d,L}} \quad , \quad M_{f,ij} \rightarrow e^{i\alpha_i^{f,L}} M_{f,ij} e^{-i\alpha_j^{f,R}}$$

- Leptonic FCNCs absent to all orders in perturbation theory
- Loop-induced FCNCs local terms take the form:

$$\bar{u}_L V_{\text{CKM}} (M_d M_d^\dagger)^n V_{\text{CKM}}^\dagger (M_u M_u^\dagger)^m M_u u_R$$

$$\bar{d}_L V_{\text{CKM}}^\dagger (M_u M_u^\dagger)^n V_{\text{CKM}} (M_d M_d^\dagger)^m M_d d_R$$

MFV structure

(D'Ambrosio et al, Chivukula-Georgi, Hall-Randall, Buras et al, Cirigliano et al)

Minimal Flavour Violation in 2HDMs

$SU(N_G)^5$ Flavour Symmetry in the Gauge Sector $(Q_L, u_R, d_R, L_L, l_R)$

(Chivukula-Georgi '87)

Spurion Formalism:

(D'Ambrosio et al '02, Buras et al '10)

- $\Gamma_1 \sim (N_G, 1, \bar{N}_G, 1, 1)$
- $\Delta_1 \sim (N_G, \bar{N}_G, 1, 1, 1)$
- $\Pi_1 \sim (1, 1, 1, N_G, \bar{N}_G)$



**Aligned Yukawas
are also invariant**

Allowed Operators:

$$\bar{Q}'_L (\Gamma_1 \Gamma_1^\dagger)^n (\Delta_1 \Delta_1^\dagger)^m \Delta_1 u'_R$$

$$\bar{Q}'_L (\Delta_1 \Delta_1^\dagger)^n (\Gamma_1 \Gamma_1^\dagger)^m \Gamma_1 d'_R$$

FCNCs at one Loop

General 2HDM 1-loop Renormalization Group Eqs. known (Cvetic et al, Ferreira et al)



(Jung-Pich-Tuzón, Braeuninger-Ibarra-Simonetto)

$$\begin{aligned}
 \mathcal{L}_{\text{FCNC}} = & \frac{C(\mu)}{4\pi^2 v^3} (1 + \zeta_u^* \zeta_d) \sum_i \varphi_i^0(x) \\
 & \times \left\{ (\mathcal{R}_{i2} + i \mathcal{R}_{i3}) (\zeta_d - \zeta_u) \left[\bar{d}_L V_{\text{CKM}}^\dagger M_u M_u^\dagger V_{\text{CKM}} M_d d_R \right] \right. \\
 & \quad \left. - (\mathcal{R}_{i2} - i \mathcal{R}_{i3}) (\zeta_d^* - \zeta_u^*) \left[\bar{u}_L V_{\text{CKM}} M_d M_d^\dagger V_{\text{CKM}}^\dagger M_u u_R \right] \right\} \\
 & + \text{h.c.}
 \end{aligned}$$

- $C(\mu) = C(\mu_0) - \log(\mu/\mu_0)$
- Vanish in all \mathcal{Z}_2 models as it should
- Suppressed by $m_q m_{q'}^2 / (4\pi^2 v^3)$ and $V_{\text{CKM}}^{qq'}$ $\rightarrow \bar{s}_L b_R, \bar{c}_L t_R$

Phenomenological Constraints Jung-Pich-Tuzón

- $\tau \rightarrow \mu/e$: $|g_\mu/g_e|^2 = 1.0036 \pm 0.0029$



$$|s_l|/M_{H^\pm} < 0.40 \text{ GeV}^{-1} \quad (95\% \text{ CL})$$

- $\Gamma(P^- \rightarrow l^- \bar{\nu}_l) = \frac{m_P}{8\pi} \left(1 - \frac{m_l^2}{m_P^2}\right)^2 |G_F m_l f_P V_{CKM}^{ij}|^2 |1 - \Delta_{ij}|^2$

$$\Delta_{ij} = \frac{m_P^2}{M_{H^\pm}^2} s_l^* \frac{s_u m_{u_i} + s_d m_{d_j}}{m_{u_i} + m_{d_j}}$$

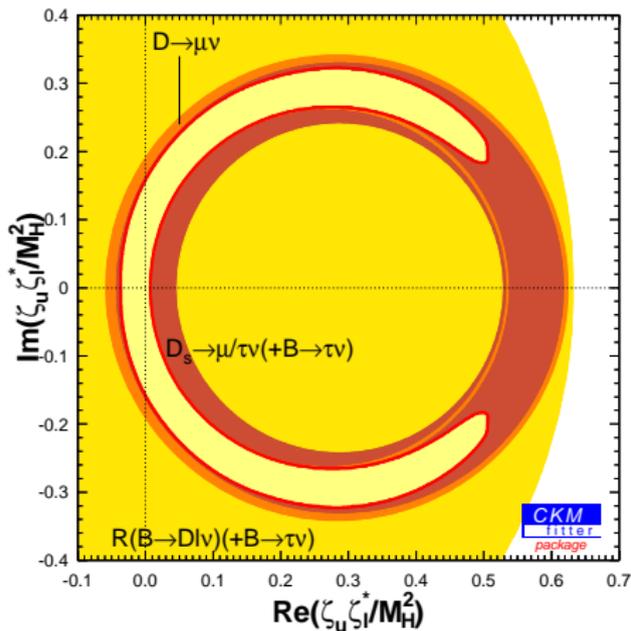
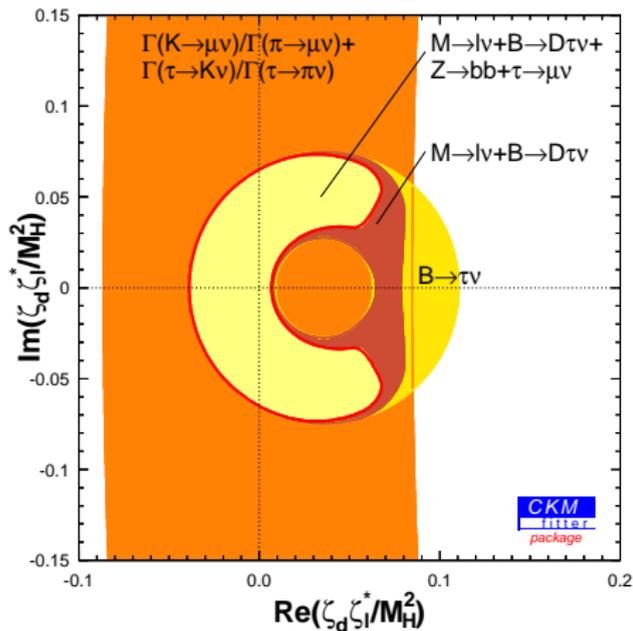
- $\Gamma(P \rightarrow P' l^- \bar{\nu}_l) \rightarrow$ Scalar form factor: $\tilde{f}_0(t) = f_0(t) (1 + \delta_{ij} t)$

$$\delta_{ij} \equiv -\frac{s_l^*}{M_{H^\pm}^2} \frac{m_i s_u - m_j s_d}{m_i - m_j}$$

Global fit to $P \rightarrow l\nu_l, \tau \rightarrow P\nu_\tau, P \rightarrow P'l\nu_l$

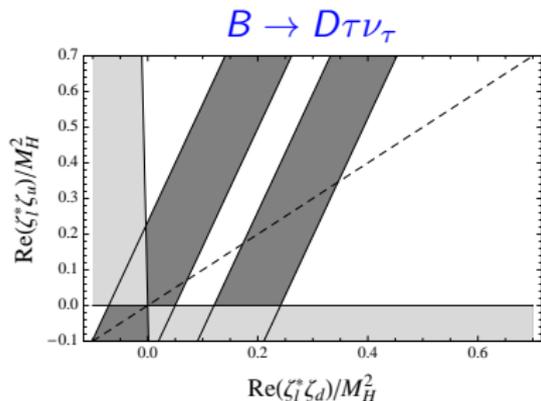
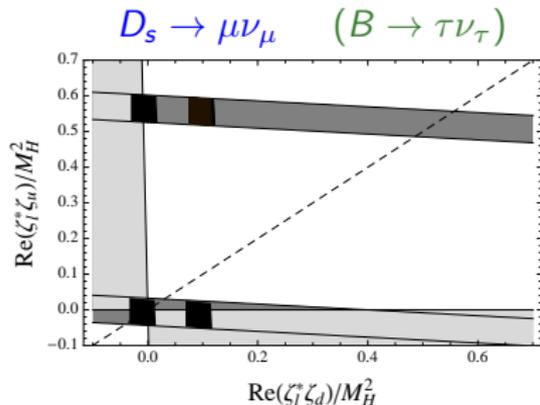
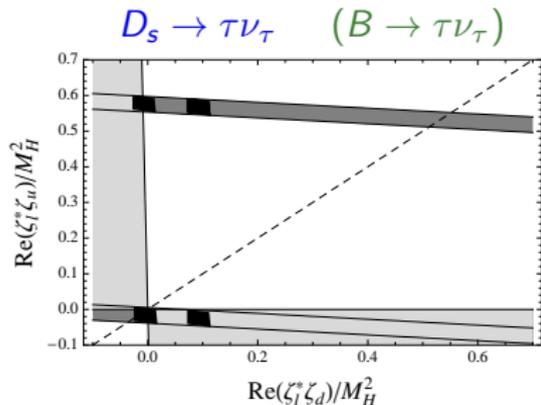
(95% CL)

Jung-Pich-Tuzón



(GeV⁻² units)

Real Couplings:



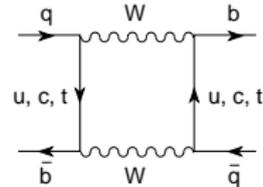
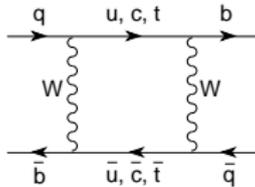
(95% CL, GeV^{-2} units)

Type I/X: Dashed Line

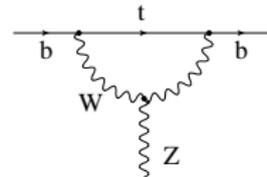
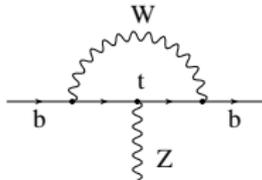
Types II/Y: Lighter grey area, $\tan \beta \in [0.1, 60]$

1-Loop Constraints on H^\pm Couplings

$B^0-\bar{B}^0$ Mixing



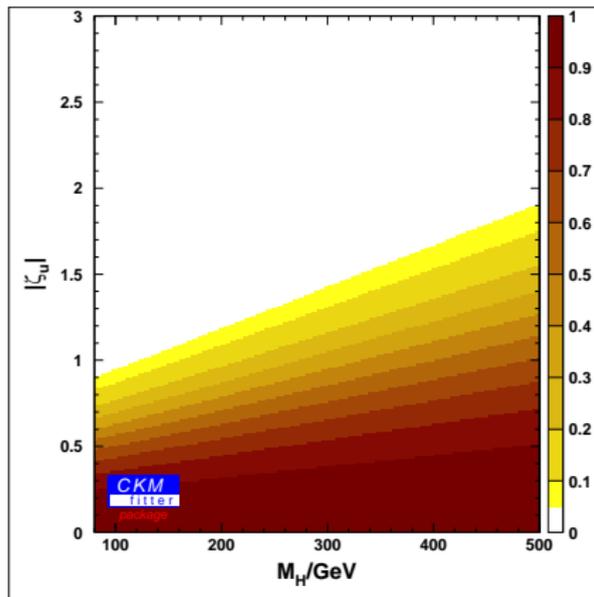
$Z \rightarrow b\bar{b}$



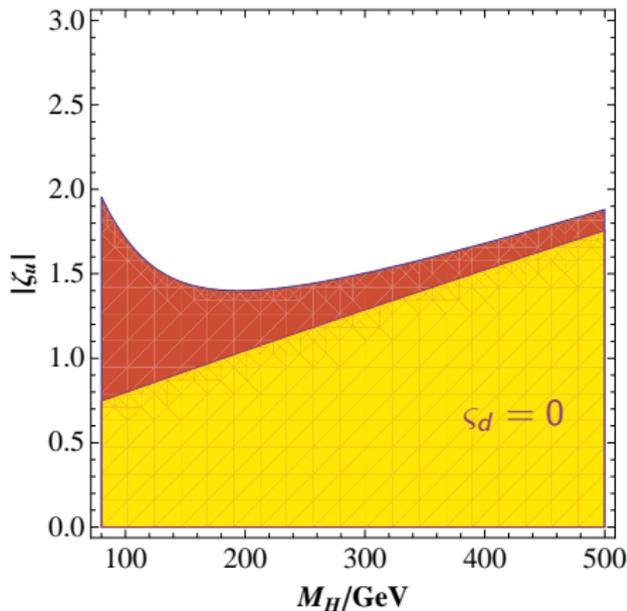
Virtual H^\pm / W^\pm . Top-dominated contributions

Constraints from $Z \rightarrow b\bar{b}$ and ΔM_{B_s} (95% CL) Jung-Pich-Tuzón

$Z \rightarrow b\bar{b}$ ($|\zeta_d| < 50$)



ΔM_{B_s} ($|\zeta_d| < 50$)



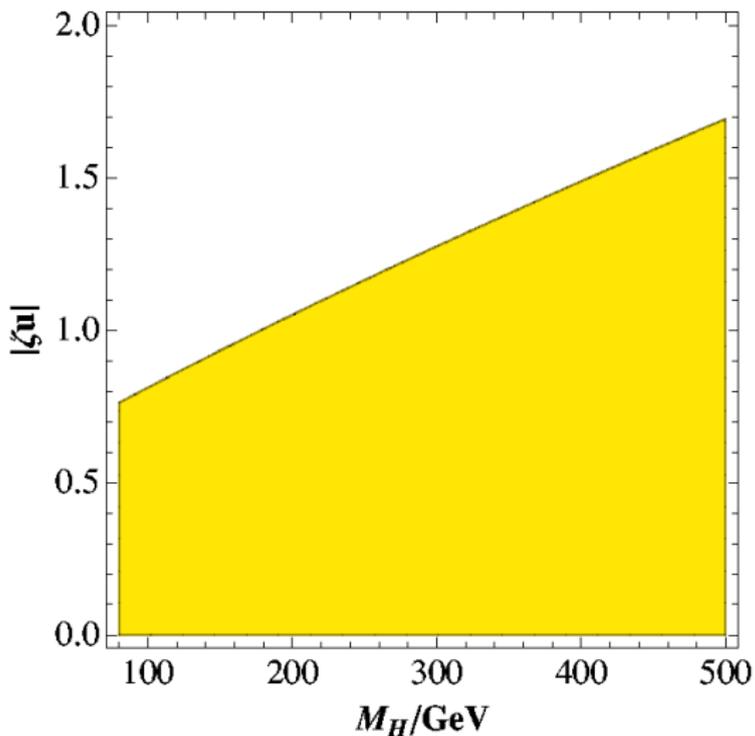
$$|\zeta_u|/M_{H^\pm} < 0.011 \text{ GeV}^{-1}$$



$$|\zeta_u \zeta_j^*|/M_{H^\pm}^2 < 0.005 \text{ GeV}^{-2}$$

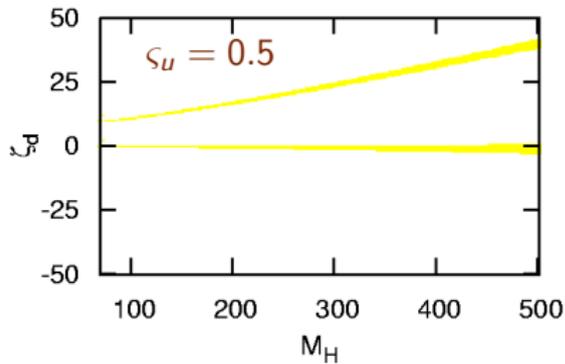
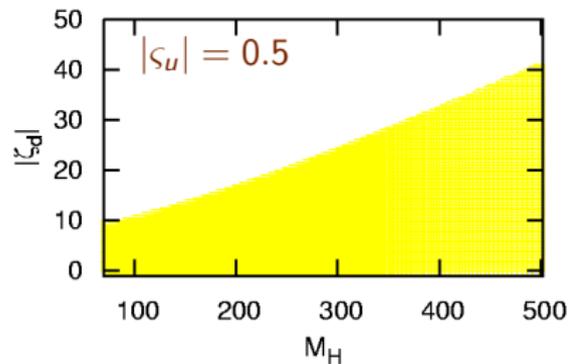
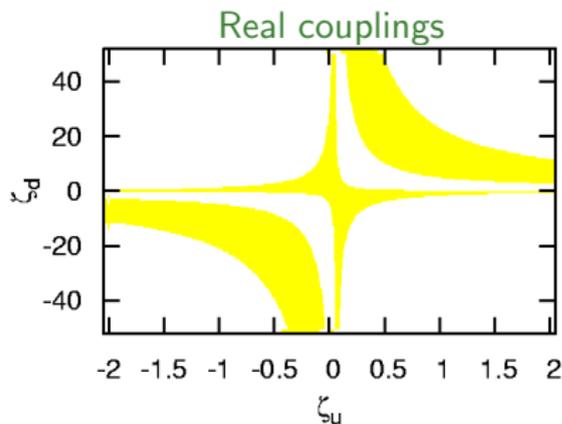
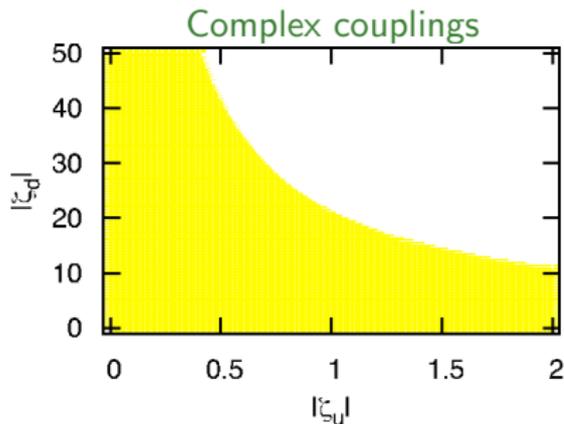
Constraints from ϵ_K (95% CL)

Jung-Pich-Tuzón



Constraints from $b \rightarrow s\gamma$ (95% CL)

Jung-Pich-Tuzón

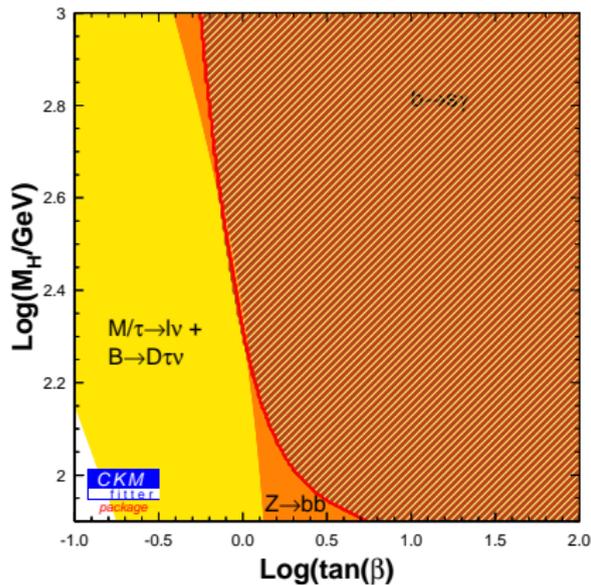


$$C_i^{\text{eff}}(\mu_W) = C_{i,SM} + |c_{su}|^2 C_{i,uu} - (c_{su}^* c_{sd}) C_{i,ud}$$

Global Constraints on \mathcal{Z}_2 Models (95% CL)

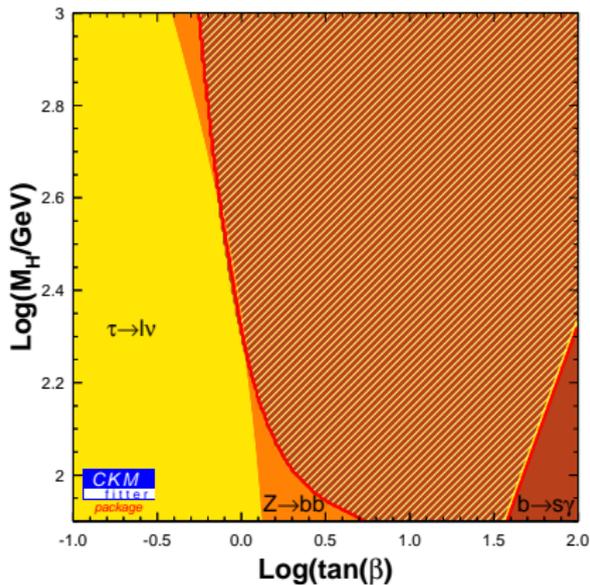
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Type I



$$\varsigma_u = \varsigma_d = \varsigma_l = \cot \beta$$

Type X

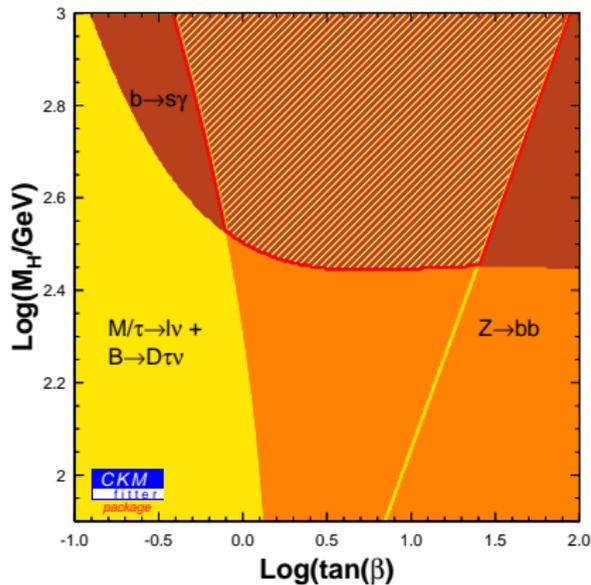


$$\varsigma_u = \varsigma_d = -\varsigma_l^{-1} = \cot \beta$$

Global Constraints on Z_2 Models (95% CL)

Jung-Pich-Tuzón

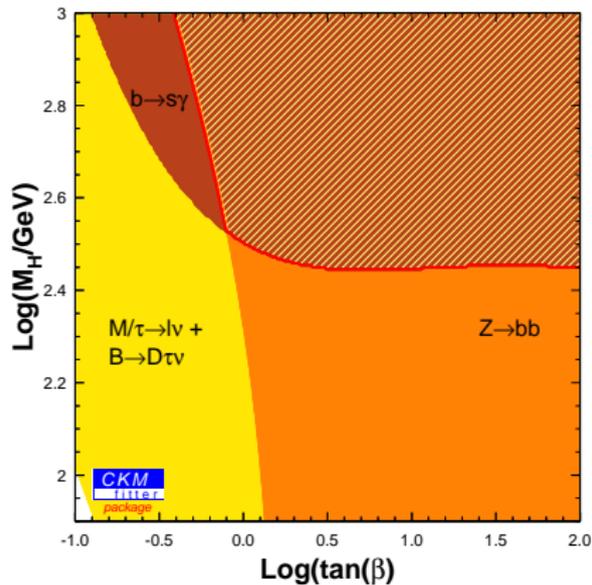
Type II



$$\zeta_u = -\zeta_d^{-1} = -\zeta_l^{-1} = \cot \beta$$

$M_{H^\pm} > 277 \text{ GeV}$

Type Y



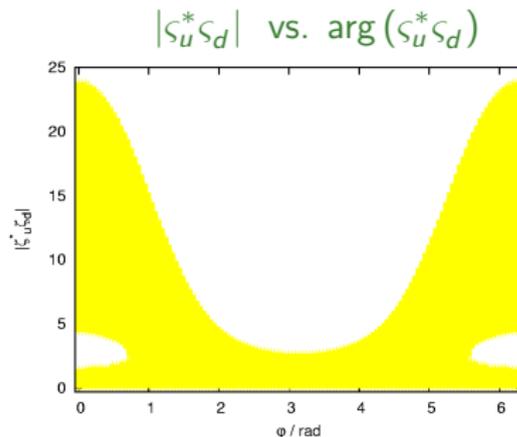
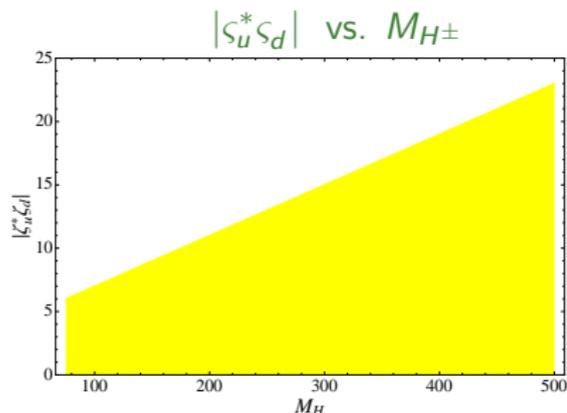
$$\zeta_u = -\zeta_d^{-1} = \zeta_l = \cot \beta$$

In agreement with previous analyses

(Aoki et al, Wahab et al, Deschamps et al, Flacher et al, Bona et al, Mahmoudi-Stal, Misiak et al ...)

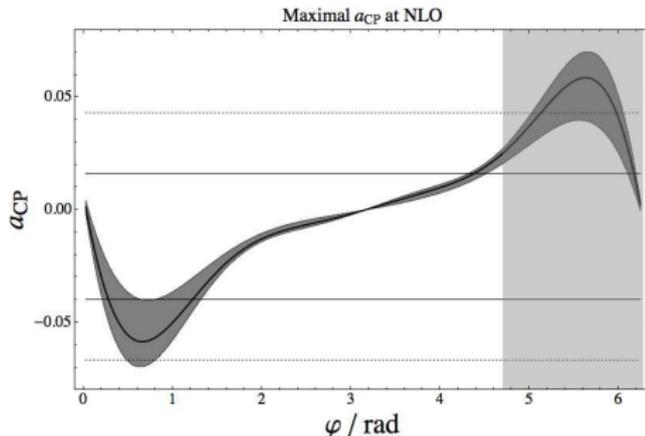
Important Correlations:

$$C_i^{\text{eff}}(\mu_W) = C_{i,SM} + |\zeta_u|^2 C_{i,uu} - (\zeta_u^* \zeta_d) C_{i,ud}$$



- Stronger constraint for small Scalar Masses
- For $\varphi \equiv \arg(\zeta_u^* \zeta_d) = \pi$ (0) constructive (destructive) interference
- Important restriction on CP asymmetries

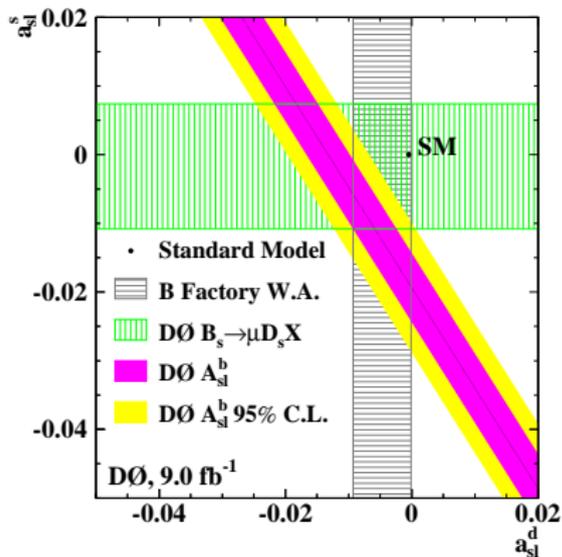
- Small in the SM (Ali et al '98, Kagan-Neubert '98, Hurth et al '05)
- Potentially large in general 2HDMs (Borzumati-Greub '98)
- However, **strongly constrained by $\text{Br}(b \rightarrow s\gamma)$**



$$a_{\text{CP}} \equiv \frac{\Gamma - \bar{\Gamma}}{\Gamma + \bar{\Gamma}}$$

Compatible with measurement, but it could be sizeable

D0: $\mu^\pm \mu^\pm$ Asymmetry



$$A_{sl}^b \equiv \frac{N_b^{++} - N_b^{--}}{N_b^{++} + N_b^{--}}$$

$$a_{sl}^q \equiv \frac{\Gamma(\bar{B}_q^0 \rightarrow \mu^+ X) - \Gamma(B_q^0 \rightarrow \mu^- X)}{\Gamma(\bar{B}_q^0 \rightarrow \mu^+ X) + \Gamma(B_q^0 \rightarrow \mu^- X)}$$

$$= \frac{\Delta\Gamma_q}{\Delta M_q} \tan \phi_q$$

- LHCb does not confirm a large ϕ_s in $B_s \rightarrow J/\psi \phi$ (D0/CDF)
- D0 data seems to require new-physics contribution in $\Delta\Gamma_s$

Average of $B_s \rightarrow J/\psi\phi$ and $B_s \rightarrow J/\psi f_0$

Simultaneous fit to both samples:

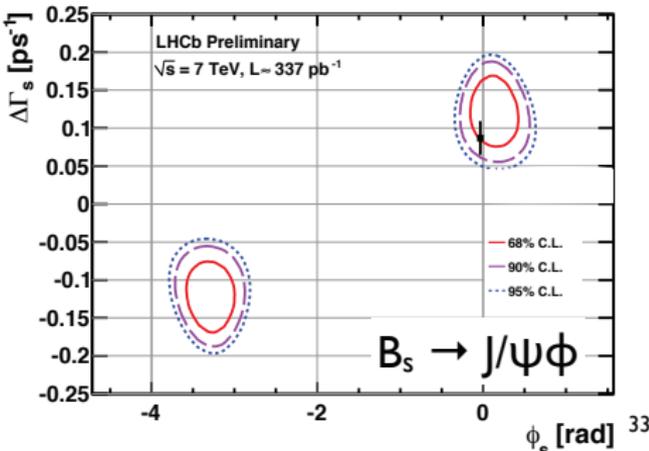
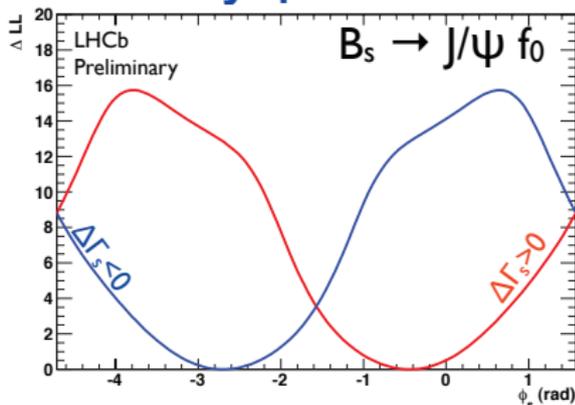
LHCb Preliminary

$$\phi_s = 0.03 \pm 0.16 \pm 0.07 \text{ rad}$$

With present statistics, no evidence for deviation from the SM.

Next steps:

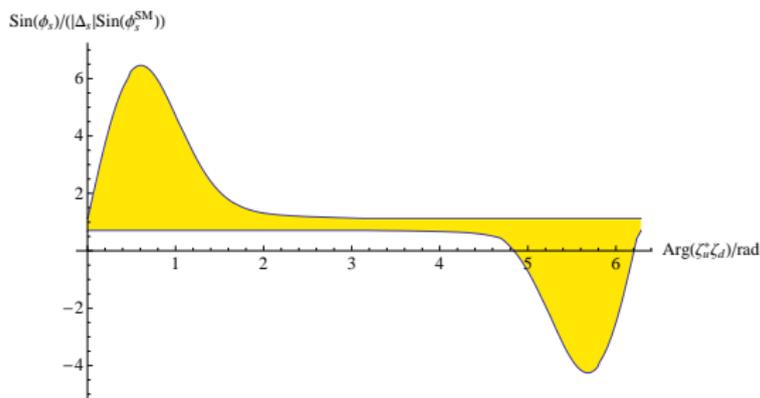
- 1) Increase statistics (luminosity)
- 2) Add same-side Kaon tagging
- 3) Break ambiguity by looking at relative S-wave phase vs. $M(KK)$ in $J/\psi\phi$



$B_s^0 - \bar{B}_s^0$ Mixing Phase within the A2HDM

Jung-Pich-Tuzón

Maximum possible enhancement from H^\pm exchanges:



$$\frac{a_{sl}}{a_{sl}|_{SM}} = \frac{\sin \phi}{|\Delta| \sin \phi^{SM}}$$

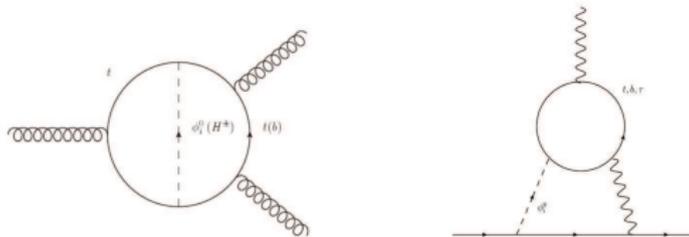
$$\phi \equiv \arg(-M_{12}/\Gamma_{12})$$

$$\Delta \equiv M_{12}/M_{12}^{SM}$$

H^\pm contributions to ΔM are too small to explain the D0 asymmetry

Electric Dipole Moments

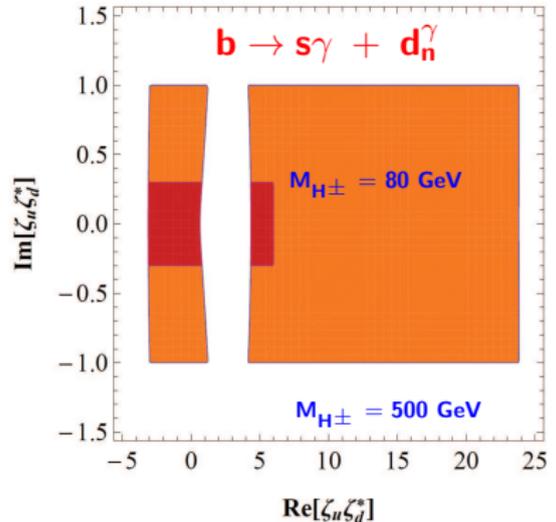
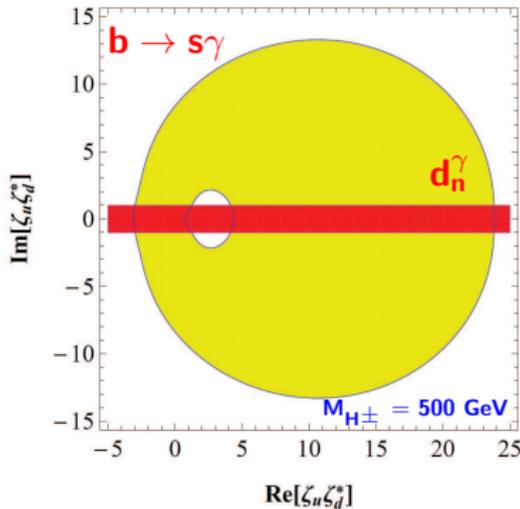
- **Highly sensitive to flavour-blind CP-violating phases**
- Stringent experimental bounds: **neutron, Thallium, Mercury . . .**
- 1-loop H^\pm contributions very suppressed by light-quark masses
- Contributions from 4-fermion operators are small (Buras et al)
(also induced by ϕ_i^0 exchange with 1-loop FCNC vertices)
- **Two-loop contributions dominate** (Weinberg '89, Dicus '90, Barr-Zee '90)



Neutron EDM dominated by H^\pm contribution to \mathcal{L}_W

$$\mathcal{L}_W = -\frac{C_W}{6} f_{abc} \epsilon^{\mu\nu\alpha\beta} G_{\mu\rho}^a G_\nu^{b\rho} G_{\alpha\beta}^c, \quad C_W \sim \text{Im}(\zeta_u \zeta_d^*)$$

Jung-Pich, preliminary

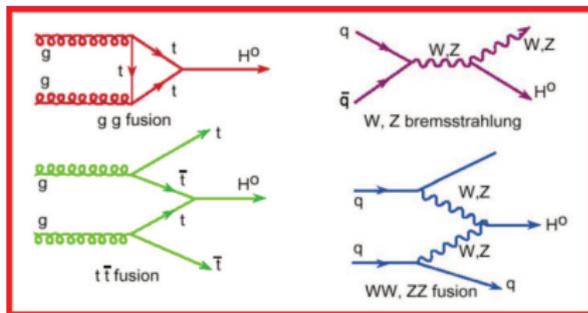


$\text{Im}(\zeta_u \zeta_d^*)$ strongly constrained, but not tiny

Higgs Production (CP assumed)

$$y_t^{h^0} = \cos \tilde{\alpha} + \varsigma_u \sin \tilde{\alpha}$$

$$y_t^{H^0} = -\sin \tilde{\alpha} + \varsigma_u \cos \tilde{\alpha}$$

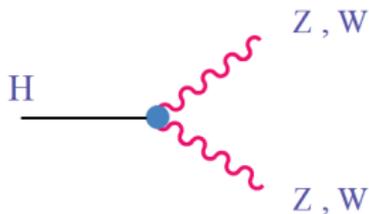


$$\lambda_{W,Z}^{h^0} = \cos \tilde{\alpha}$$

$$\lambda_{W,Z}^{H^0} = -\sin \tilde{\alpha}$$

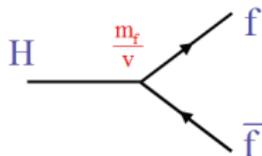
- **Charged Higgs:** $Z \rightarrow H^+ H^-$, $t \rightarrow H^+ b$, $W^+ \rightarrow H^+ h^0 (H^0)$
- **CP-odd A^0 :** $t\bar{t} \rightarrow A^0$, $W^+ \rightarrow H^+ A^0$, $Z^0 \rightarrow A^0 h^0 (H^0)$
- **CP-violation:** φ_i^0 mixing (h^0, H^0, A^0), ς_f

Higgs Decay (CP assumed)



$$\lambda_{W,Z}^{h^0} = \cos \tilde{\alpha}$$

$$\lambda_{W,Z}^{H^0} = -\sin \tilde{\alpha}$$



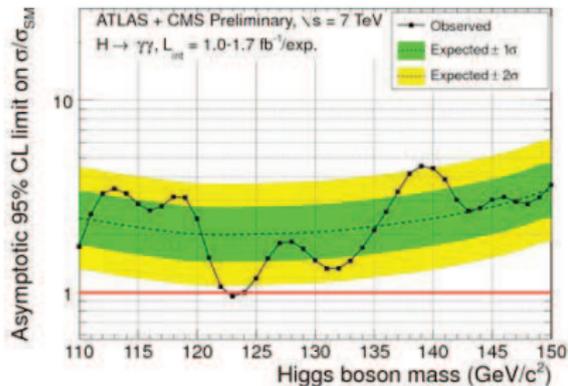
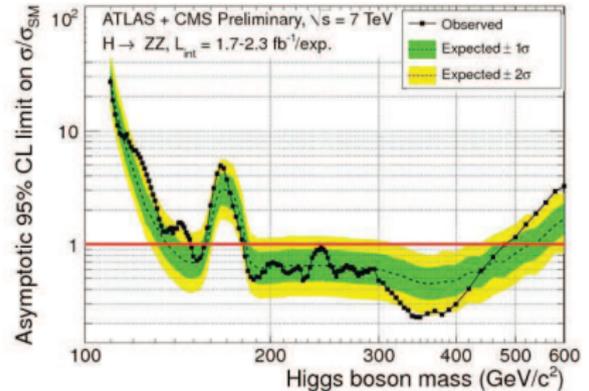
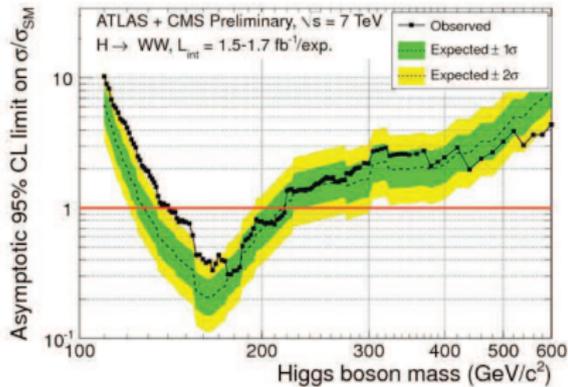
$$y_t^{h^0} = \cos \tilde{\alpha} + \varsigma_u \sin \tilde{\alpha}$$

$$y_t^{H^0} = -\sin \tilde{\alpha} + \varsigma_u \cos \tilde{\alpha}$$

- $h^0 (H^0) \rightarrow W^\pm H^\mp$, $h^0 (H^0) \rightarrow Z A^0$, $H^0 \rightarrow h^0 A^0$
- $H^+ \rightarrow t\bar{b}$, $H^+ \rightarrow W^+ h^0 (H^0)$
- $A^0 \rightarrow t\bar{t}$, $A^0 \rightarrow W^\pm H^\mp$, $A^0 \rightarrow Z^0 h^0 (H^0)$, $A^0 \rightarrow h^0 H^0$

Scaling factors for A-2HDM Higgs h^0

Rolandi, HCP 11

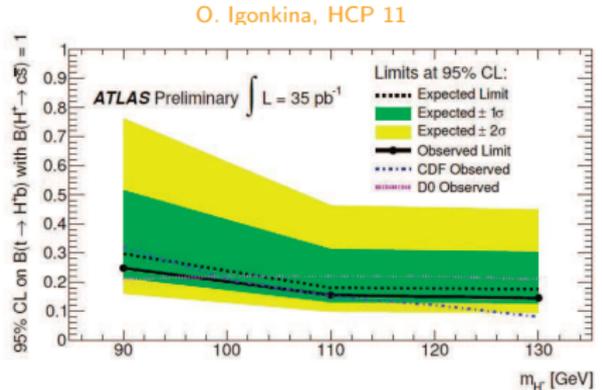
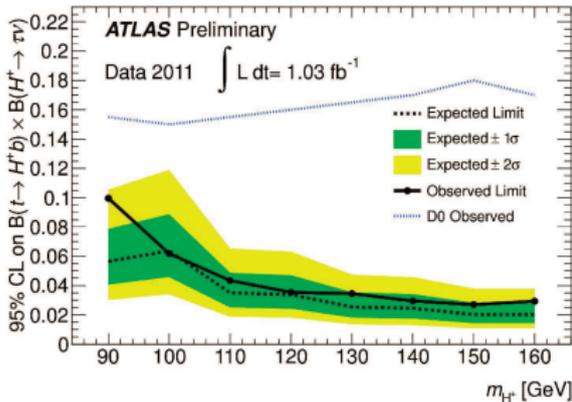


$$|y_t^{h^0}| = |\cos \tilde{\alpha} + s_u \sin \tilde{\alpha}| < 0.25 - 1$$

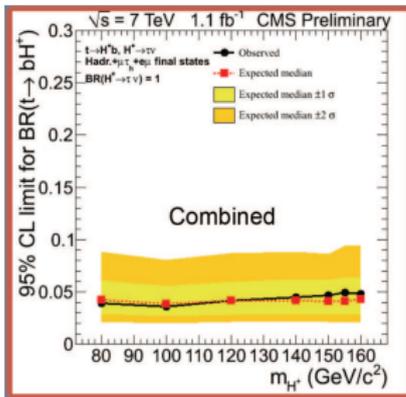
$$\text{for } M_{h^0} \in [141, 476]$$

$$Br(h^0 \rightarrow ZZ, WW) \approx 1$$

Charged Higgs



A. Savin, HCP 11



$$Br(t \rightarrow H^+ b) \approx \frac{|S_u|^2}{|S_u|^2 + R} + \mathcal{O}(m_b^2/m_t^2)$$

$$R = \left(\frac{m_t^2 - M_{W^\pm}^2}{m_t^2 - M_{H^\pm}^2} \right)^2 \left(1 + 2 \frac{M_{W^\pm}^2}{m_t^2} \right) (1 + \delta_{\text{QCD}})$$

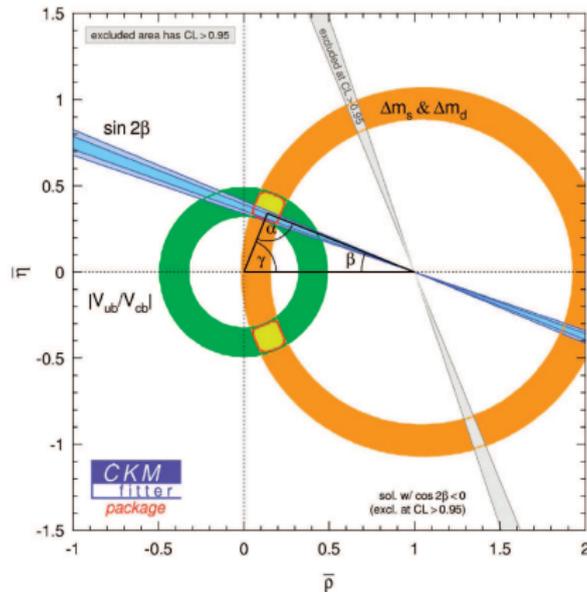
$$Br(H^+ \rightarrow \tau^+ \nu_\tau) \approx 1 - Br(H^+ \rightarrow c \bar{s}) \approx \left\{ 1 + (1.8 |S_u|^2 + 0.012 |S_d|^2) / |S_l|^2 \right\}^{-1}$$

SUMMARY

- The **Aligned THDM** provides a **general phenomenological setting**
Includes all Z_2 models
- **Tree-level FCNCs absent** by construction
- **Leptonic FCNCs forbidden to all orders**
- **Loop-induced quark FCNCs very constrained (MFV like)**
- **New sources of CP violation through S_f**
- **Satisfies flavour constraints with $S_f \sim \mathcal{O}(1)$**
- **Sizeable flavour-blind phases allowed by EDMs**
- **Interesting collider phenomenology**

Backup Slides

CKM Fit within the A2HDM



- Only the constraints from $|V_{ub}/V_{cb}|$ and $\Delta m_s/\Delta m_d$ survive
- γ from tree-level decays excludes the 2nd solution
- $\Delta m_s/\Delta m_d = (\Delta m_s/\Delta m_d)|_{\text{SM}} + \mathcal{O}[(m_s - m_d)\zeta_d/M_W]$

Parameter	Value	Comment
f_{B_s}	$(0.242 \pm 0.003 \pm 0.022)$ GeV	
f_{B_s}/f_{B_d}	$1.232 \pm 0.016 \pm 0.033$	
f_{D_s}	$(0.2417 \pm 0.0012 \pm 0.0053)$ GeV	
f_{D_s}/f_{D_d}	$1.171 \pm 0.005 \pm 0.02$	
f_K/f_π	$1.192 \pm 0.002 \pm 0.013$	
$f_{B_s} \sqrt{\hat{B}_{B_s^0}}$	$(0.266 \pm 0.007 \pm 0.032)$ GeV	
$f_{B_d} \sqrt{\hat{B}_{B_s^0}} / (f_{B_s} \sqrt{\hat{B}_{B_s^0}})$	$1.258 \pm 0.025 \pm 0.043$	
\hat{B}_K	$0.732 \pm 0.006 \pm 0.043$	
$ V_{ud} $	0.97425 ± 0.00022	
λ	0.2255 ± 0.0010	$(1 - V_{ud} ^2)^{1/2}$
$ V_{ub} $	$(3.8 \pm 0.1 \pm 0.4) \cdot 10^{-3}$	$b \rightarrow ul\nu$ (excl. + incl.)
A	$0.80 \pm 0.01 \pm 0.01$	$b \rightarrow cl\nu$ (excl. + incl.)
$\bar{\rho}$	$0.15 \pm 0.02 \pm 0.05$	Our fit
$\bar{\eta}$	$0.38 \pm 0.01 \pm 0.06$	Our fit
$\rho^2 _{B \rightarrow Dl\nu}$	$1.18 \pm 0.04 \pm 0.04$	
$\Delta _{B \rightarrow Dl\nu}$	0.46 ± 0.02	
$f_+^{K\pi}(0)$	0.965 ± 0.010	

$$\Phi_1 = \left[\begin{array}{c} G^+ \\ \frac{1}{\sqrt{2}} (v + S_1 + iG^0) \end{array} \right] , \quad \Phi_2 = \left[\begin{array}{c} H^+ \\ \frac{1}{\sqrt{2}} (S_2 + iS_3) \end{array} \right]$$

Goldstones: G^\pm, G^0

Mass eigenstates: H^\pm , $\varphi_i^0(x) = \{h(x), H(x), A(x)\}$

$$\varphi_i^0(x) = \{h(x), H(x), A(x)\} = \mathcal{R}_{ij} S_j(x)$$

CP-conserving scalar potential: $A(x) = S_3(x)$

$$\begin{pmatrix} H \\ h \end{pmatrix} = \begin{bmatrix} \cos \tilde{\alpha} & \sin \tilde{\alpha} \\ -\sin \tilde{\alpha} & \cos \tilde{\alpha} \end{bmatrix} \begin{pmatrix} S_1 \\ S_2 \end{pmatrix}$$