Precision Flavour Physics as a Probe beyond the Standard Model

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Why do we believe in TeV Physics? What can Flavour tell us?

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Why Study Flavour Physics?

T. Mannel, Siegen University Precision Flavour Physics

Why do we believe in TeV Physics? What can Flavour tell us?

- The Standard Model passed all tests up to the 100 GeV Scale:
- LEP: test of the gauge Structure
- Flavour factories: test of the Flavour Sector



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Precision Flavour Physics

Why do we believe in TeV Physics? What can Flavour tell us?

No significant deviation has been found (yet)!

... only a few "tensions" (= Observables off by 2σ or even less)



LHC will perform a direct test of the TeV Scale



Why do we believe in TeV Physics? What can Flavour tell us?

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Why do we believe in TeV Physics?

- Theoretical argument:
- Stabilization of the electroweak scale:



Quadratic Dependence on the cut-off

$$\Delta m_{H}^2 = -rac{\lambda_f^2}{8\pi^2}\Lambda_{
m UV}^2$$

• Drives the Higgs mass up to the UV cut off $\Lambda_{\rm UV} \sim \textit{M}_{\rm PL}$

Why do we believe in TeV Physics? What can Flavour tell us?

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• Stabilization at the TeV scale: e.g. through SUSY:



Only logarithmic divergence

$$\Delta m_{H}^{2} = m_{\mathrm{soft}}^{2} \frac{\lambda}{16\pi^{2}} \ln \left(\frac{\Lambda_{\mathrm{UV}}}{m_{\mathrm{soft}}} \right)$$

*m*_{soft} ~ O(TeV): Splitting between particles and particles

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- How strong are these arguments?
- Could there something be wrong with our understanding of
 - electroweak symmetry breaking?
 - scale and conformal invariance? (c.f. Lee Wick Model)
 - ...
- Does flavour tell us something about this? and what?

Why do we believe in TeV Physics? What can Flavour tell us?

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What can Flavour tell us?

- Flavour Physics ↔ No new physics at the TeV scale with a generic flavour structure
- Parametrization of new physics: Higher Dimensional Operators:

$$\mathcal{L} = \mathcal{L}_{\mathrm{SM}} + \frac{1}{\Lambda} \mathcal{L}^{(5)} + \frac{1}{\Lambda^2} \mathcal{L}^{(6)} + \cdots \qquad \mathcal{L}^{(n)} = \sum_j C_j O_j^{(n)}$$

- Λ: New Physics scale
- $O_j^{(n)}$: Local Operators of dimension *n*

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• Some of the $O_j^{(n)}$ may mediate flavour transitions: e.g.

- $$\begin{split} &O_1^{(6)} = (\bar{s}_L \gamma_\mu d) (\bar{s}_L \gamma^\mu d) & (\text{Kaon Mixing}) \\ &O_2^{(6)} = (\bar{b}_L \gamma_\mu d) (\bar{b}_L \gamma^\mu d) & (B_d \text{ Mixing}) \\ &O_3^{(6)} = (\bar{b}_L \gamma_\mu 2) (\bar{b}_L \gamma^\mu s) & (B_s \text{ Mixing}) \\ &O_4^{(6)} = (\bar{c}_L \gamma_\mu u) (\bar{c}_L \gamma^\mu u) & (D \text{ Mixing}) \end{split}$$
- $\Lambda \sim 1000$ TeV from Kaon mixing ($C_i = 1$)
- $\Lambda \sim 1000$ TeV from D mixing
- $\Lambda \sim 400$ TeV from B_d mixing
- $\Lambda \sim 70$ TeV from B_s mixing

Why do we believe in TeV Physics? What can Flavour tell us?

News from Charm: CP Violation?

• Recent LHCb result on CP violation in D decays :

$$egin{aligned} \Delta A_{
m CP} &= A_{
m CP}(D^0 o K^+ K^-) - A_{
m CP}(D^0 o \pi^+ p i^-) \ &= egin{cases} -(0.82 \pm 0.21 \pm 0.11)\% & {
m LHCb} \ -(0.68 \pm 0.18)\% & {
m world average} \end{aligned}$$



• "Old" or "New" Physics?

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- "New physics" is around the corner??
- Are the flavour data a hint at a new physics scale well above the TeV scale?
- ... there are a few corners where O(1) flavour effects are still possible, c.f. Charm CPV
- Are there lessons from history?

Why do we believe in TeV Physics? What can Flavour tell us?

The Top Quark Story

- First indirect hint to a heavy top quark:
 B B Oscillation of ARGUS (1987)
- The world in 1987 ("PETRA Days"): The top was believed to be at ~ 25 GeV ... based on good theoretical arguments
- ARGUS could not have seen anything with a 25 GeV Top (within SM)



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- The consequences:
 - (-) No Toponium
 - (-) No Top quark discovery at LEP and SLC
 - (-) No "New Physcis $\mathcal{O}(30 \text{ GeV})$ " just around the corner
 - (+) CP violation in the *B* sector may become observable
 - (+) GIM is weak for bottom quarks
- This was actually good for Flavour Physics ...
- GIM suppressed decays as a probe for large scales
- From current data: TeV "New Physics" must have a flavour structure close to the one of the SM
- $\bullet \rightarrow$ Concept of "Minimal Flavour Violation" (MFV)

Why do we believe in TeV Physics? What can Flavour tell us?

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Peculiarities of SM Flavour Parametrization

- Strong CP remains mysterious
- Flavour diagonal CP Violation is well hidden:
 e.g electric dipole moments:
 For quarks at least three loops (Shabalin)



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- Pattern of mixing and mixing induced CP violation determined by GIM: Tiny effects in the up quark sector
 - $\Delta C = 2$ is very small
 - Mixing with third generation is small: charm physics basically "two family"
 - $\bullet \ \to \mathsf{CP}$ violation in charm should be small in the SM
- Fully consistent with particle physics observations
- ... but inconsistent with matter-antimatter asymmetry

Why do we believe in TeV Physics? What can Flavour tell us?

??? Many Open Questions ???

- Our Understanding of Flavour is unsatisfactory:
 - 22 (out of 27) free Parameters of the SM originate from the Yukawa Sector (including Lepton Mixing)
 - Why is the CKM Matrix hierarchical?
 - Why is CKM so different from the PMNS?
 - Why are the quark masses (except the top mass) so small compared with the electroweak VEV?
 - Why do we have three families?
- Why is CP Violation in Flavour-diagonal Processes not observed? (e.g. z.B. electric dipolmoments of electron and neutron)
- Where is the CP violation needed to explain the matter-antimatter asymmetry of the Universe?

Introduction: Why Study Flavour Physics? Effective Weak Hamiltonian Theory Tools for Precision Flavour Physics Achivements Approximate Flavour Symmetries

Theory Tools for Precision Flavour Physics

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Effective Weak Hamiltonian Heavy Quark Expansions Approximate Flavour Symmetries

Tools I: Effective Weak Hamiltonian

Integrate out the weak bosons and the top:

$$\begin{split} \mathcal{H}_{eff} &= \frac{4G_F}{\sqrt{2}} \lambda_{CKM} \sum_k \hat{C}_k(\mu) \mathcal{O}_k(\mu) \\ \mathcal{O}_1 &= \left(\bar{c}_{L,i\gamma\mu} s_{L,j} \right) \left(\bar{d}_{L,j\gamma\mu} u_{L,i} \right) , \quad \mathcal{O}_2 = \left(\bar{c}_{L,i\gamma\mu} s_{L,i} \right) \left(\bar{d}_{L,j\gamma\mu} u_{L,j} \right) , \\ \mathcal{O}_3 &= \left(\bar{s}_{L,i\gamma\mu} b_{L,i} \right) \sum_{q=u,d,s,c,b} \left(\bar{q}_{L,j\gamma^{\mu}} q_{L,j} \right) , \quad \mathcal{O}_4 = \left(\bar{s}_{L,i\gamma\mu} b_{L,j} \right) \sum_{q=u,d,s,c,b} \left(\bar{q}_{L,j\gamma^{\mu}} q_{L,i} \right) , \\ \mathcal{O}_5 &= \left(\bar{s}_{L,i\gamma\mu} b_{L,i} \right) \sum_{q=u,d,s,c,b} \left(\bar{q}_{R,j\gamma^{\mu}} q_{R,j} \right) , \quad \mathcal{O}_6 = \left(\bar{s}_{L,i\gamma\mu} b_{L,j} \right) \sum_{q=u,d,s,c,b} \left(\bar{q}_{R,j\gamma^{\mu}} q_{R,i} \right) . \\ \mathcal{O}_7 &= \frac{e}{16\pi^2} m_b (\bar{s}_{L,\alpha} \sigma_{\mu\nu} b_{R,\alpha}) F^{\mu\nu} , \quad \mathcal{O}_8 = \frac{g}{16\pi^2} m_b (\bar{s}_{L,\alpha} T^a_{\alpha\beta} \sigma_{\mu\nu} b_{R,\alpha}) G^{a\mu\nu} , \\ \mathcal{O}_9 &= \frac{1}{2} (\bar{s}_L \gamma_\mu b_L) (\bar{\ell}\gamma^{\mu} \ell) , \quad \mathcal{O}_{10} = \frac{1}{2} (\bar{s}_L \gamma_\mu b_L) (\bar{\ell}\gamma^{\mu} \gamma_5 \ell) \end{split}$$

Coefficients in the SM are known to NLO!

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Tools II: Heavy Quark Expansions

- Main development for precision flavour physics of heavy quarks: Heavy Mass Expansion Methods: HQET, HQE, SCET ...
- Remarkable Progress:
 In many cases this has pushed hadronic uncertainties back to the 1/mb corrections
- Systematic calculatons of radiative corrections is possible in these effective theories
- Works well for leptonics and semi-leptonics Exclusive as well as Inclusive
- Still a few problems with non-leptonics ... in particular for exclusive non-leptonics

Effective Weak Hamiltonian Heavy Quark Expansions Approximate Flavour Symmetries

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Heavy Quark Symmetries: Exclusive Decays

- Kinematic variable for a heavy quark: Four Velovity v
- Differential Rates

$$\begin{split} & \frac{d\Gamma}{d\omega} (B \to D^* \ell \bar{\nu}_{\ell}) \!\!\!= \!\!\! \frac{G_F^2}{48\pi^3} |V_{cb}|^2 m_{D^*}^3 (\omega^2 - 1)^{1/2} P(\omega) (\mathcal{F}(\omega))^2 \\ & \frac{d\Gamma}{d\omega} (B \to D \ell \bar{\nu}_{\ell}) \!\!\!= \!\!\! \frac{G_F^2}{48\pi^3} |V_{cb}|^2 (m_B + m_D)^2 m_D^3 (\omega^2 - 1)^{3/2} (\mathcal{G}(\omega))^2 \end{split}$$

- with $\omega = vv'$ and
- $P(\omega)$: Calculable Phase space factor
- \mathcal{F} and \mathcal{G} : Form Factors

Effective Weak Hamiltonian Heavy Quark Expansions Approximate Flavour Symmetries

Heavy Quark Symmetries

- Normalization of the Form Factors is known at vv' = 1: (both initial and final meson at rest)
- Corrections can be calculated / estimated

$$\mathcal{F}(\omega) = \eta_{\text{QED}} \eta_A \left[1 + \delta_{1/\mu^2} + \cdots \right] + (\omega - 1)\rho^2 + \mathcal{O}((\omega - 1)^2)$$
$$\mathcal{G}(1) = \eta_{\text{QED}} \eta_V \left[1 + \mathcal{O}\left(\frac{m_B - m_D}{m_B + m_D}\right) \right]$$

• Parameter of HQS breaking: $\frac{1}{\mu} = \frac{1}{m_c} - \frac{1}{m_b}$ • $\eta_A = 0.960 \pm 0.007, \ \eta_V = 1.022 \pm 0.004, \ \delta_{1/\mu^2} = -(8 \pm 4)\%, \ \eta_{\text{QED}} = 1.007$

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$B \rightarrow \overline{D^{(*)}}$ Form Factors from the Lattice

- Unquenched Calculations become available!
- Heavy Mass Limit is not used
- Lattice Calculations of the deviation from unity

$${\cal F}(1) = 0.908 \pm 0.016$$

 ${\cal G}(1)=1.074\pm0.018\pm0.016$

F(1): upd. from CKM2010 , G(1): A. Kronfeld et al. 2005

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 $B \rightarrow D^{(*)}$ Form Factors: Non-Lattice Results

- $B \rightarrow D^*$ Form Factor:
 - Based on Zero Recoil Sum Rules (Uraltsev, also Ligeti et al.)
 - Including full α_s and up to $1/m_b^5$

$$\mathcal{F}(1)=0.86\pm0.04$$

(Gambino, Uraltsev, M (2010))

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• $B \rightarrow D$ Form Factor:

• Based on the "BPS limit" $\mu_{\pi}^2 = \mu_G^2$

$$\mathcal{G}(1)=1.04\pm0.02$$
 (U

Jraltsev)

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Heavy Quark Expansion in Inclusive Decays

Heavy Quark Expansion = Operator Product Expansion

(Chay, Georgi, Bigi, Shifman, Uraltsev, Vainstain, Manohar. Wise, Neubert, M,...)

$$\begin{split} &\Gamma \propto \sum_{X} (2\pi)^{4} \delta^{4} (P_{B} - P_{X}) |\langle X | \mathcal{H}_{eff} | B(v) \rangle|^{2} \\ &= \int d^{4}x \, \langle B(v) | \mathcal{H}_{eff}(x) \mathcal{H}_{eff}^{\dagger}(0) | B(v) \rangle \\ &= 2 \, \operatorname{Im} \int d^{4}x \, \langle B(v) | T \{ \mathcal{H}_{eff}(x) \mathcal{H}_{eff}^{\dagger}(0) \} | B(v) \rangle \\ &= 2 \, \operatorname{Im} \int d^{4}x \, e^{-im_{b}v \cdot x} \langle B(v) | T \{ \widetilde{\mathcal{H}}_{eff}(x) \widetilde{\mathcal{H}}_{eff}^{\dagger}(0) \} | B(v) \rangle \end{split}$$

• Last step: $b(x) = b_v(x) \exp(-im_b vx)$, corresponding to $p_b = m_b v + k$ Expansion in the residual momentum k Introduction: Why Study Flavour Physics? Effective Weak Hamiltonia Theory Tools for Precision Flavour Physics Achivements Approximate Flavour Sym

• Perform an "OPE": *m_b* is much larger than any scale appearing in the matrix element

$$\int d^4x e^{-im_b vx} T\{\widetilde{\mathcal{H}}_{eff}(x)\widetilde{\mathcal{H}}_{eff}^{\dagger}(0)\} = \sum_{n=0}^{\infty} \left(\frac{1}{2m_Q}\right)^n C_{n+3}(\mu) \mathcal{O}_{n+3}(\mu)$$

ightarrow The rate for $B
ightarrow X_c \ell ar
u_\ell$ can be written as

$$\Gamma = \Gamma_0 + \frac{1}{m_Q}\Gamma_1 + \frac{1}{m_Q^2}\Gamma_2 + \frac{1}{m_Q^3}\Gamma_3 + \cdots$$

- The Γ_i are power series in $\alpha_s(m_Q)$: \rightarrow Perturbation theory!
- Works also for differential rates!

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- Γ_0 is the decay of a free quark ("Parton Model")
- Γ₁ vanishes due to Heavy Quark Symmetries
- Γ₂ is expressed in terms of two parameters

$$2M_{H}\mu_{\pi}^{2} = -\langle H(v) | \bar{Q}_{v}(iD)^{2}Q_{v} | H(v) \rangle$$

$$2M_{H}\mu_{G}^{2} = \langle H(v) | \bar{Q}_{v}\sigma_{\mu\nu}(iD^{\mu})(iD^{\nu})Q_{v} | H(v) \rangle$$

 $\mu_{\pi} \text{:}$ Kinetic energy and $\mu_{\textit{G}} \text{:}$ Chromomagnetic moment

Γ₃ two more parameters

 $2M_{H}\rho_{D}^{3} = -\langle H(v)|\bar{Q}_{v}(iD_{\mu})(ivD)(iD^{\mu})Q_{v}|H(v)\rangle$ $2M_{H}\rho_{LS}^{3} = \langle H(v)|\bar{Q}_{v}\sigma_{\mu\nu}(iD^{\mu})(ivD)(iD^{\nu})Q_{v}|H(v)\rangle$

 ρ_D : Darwin Term and ρ_{LS} : Spin-Orbit Term

• Γ_4 and Γ_5 have been computed Bigi, Uraltsev, Turczyk, TM, ...

Effective Weak Hamiltonian Heavy Quark Expansions Approximate Flavour Symmetries

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Structure of the HQE

• Structure of the expansion (@ tree):

$$d\Gamma = d\Gamma_{0} + \left(\frac{\Lambda_{\text{QCD}}}{m_{b}}\right)^{2} d\Gamma_{2} + \left(\frac{\Lambda_{\text{QCD}}}{m_{b}}\right)^{3} d\Gamma_{3} + \left(\frac{\Lambda_{\text{QCD}}}{m_{b}}\right)^{4} d\Gamma_{4}$$
$$+ d\Gamma_{5} \left(a_{0} \left(\frac{\Lambda_{\text{QCD}}}{m_{b}}\right)^{5} + a_{2} \left(\frac{\Lambda_{\text{QCD}}}{m_{b}}\right)^{3} \left(\frac{\Lambda_{\text{QCD}}}{m_{c}}\right)^{2}\right)$$
$$+ \dots + d\Gamma_{7} \left(\frac{\Lambda_{\text{QCD}}}{m_{b}}\right)^{3} \left(\frac{\Lambda_{\text{QCD}}}{m_{c}}\right)^{4}$$

- $d\Gamma_3 \propto \ln(m_c^2/m_b^2)$
- Power counting $m_c^2 \sim \Lambda_{\rm QCD} m_b$

Present state of the $b \rightarrow c$ semileptonic Calculations

- Tree level terms up to and including $1/m_b^5$ known Bigi, Zwicky, Uraltsev, Turczyk, TM, ...
- $\mathcal{O}(\alpha_s)$ and full $\mathcal{O}(\alpha_s^2)$ for the partonic rate known Melnikov, Czarnecki, Pak
- Proper mass definitions for *m_b* and *m_c* and precise input values have been given

Hoang, Gambino, Kühn Steinhauser

- $\mathcal{O}(\alpha_s)$ for the μ_π^2/m_b^2 is known Becher, Boos, Lunghi, Gambino
- In the pipeline:
 - Complete α_s/m_b^2 , including the μ_G terms
 - More on the "Intrinsic charm" and "weak annihilation" contributions

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Effective Weak Hamiltonian Heavy Quark Expansions Approximate Flavour Symmetries

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Tools III: Flavour Symmetries and Diagramm Topologies

- Avoid to deal with QCD dynamics: Use symmetries of QCD
- I-spin, V-Spin, U-Spin or full Flavour SU(3)
- Discuss breaking of SU(3)
- Supplement group theory by "diagrammatic considerations" such as "Penguins are smaller than trees"
- Improvement by more data possible

Effective Weak Hamiltonian Heavy Quark Expansions Approximate Flavour Symmetries

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Tools IV: Lattice QCD

... ask the lattice experts ...

Semileptonic Decays Nonleptonic Decays Rare Decays

Semileptonic Decays

• The $1/m_b$ Expansion: an enormous progress

$$V_{\textit{cb,incl}} = (41.54 \pm 0.72) imes 10^{-3}$$
 (HQE)

A theo. uncertainty of 1% in $V_{cb,incl}$ looks plausible!

$$V_{cb,excl} = (38.7 \pm 1.1) imes 10^{-3}$$
 (Lattice, 2008)

 $V_{cb,excl} = (39.7 \pm 1.1) \times 10^{-3}$ (Lattice, 2010)

 $V_{cb,excl} = (41.0 \pm 1.5) \times 10^{-3}$ (ZR Sum Rules. prelim.)

Tension between $V_{cb,incl}$ and $V_{cb,excl}$ is about to disappear!

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Nonleptonic Decays

- The golden modes $B \rightarrow J/\psi K_s$ and $B_s \rightarrow J/\psi \phi$:
- How golden are these golden modes?
- Look at a decay $B \rightarrow f$, (f: Some CP eigentstate)

$$A(B^0
ightarrow f) = \mathcal{A}\left[1 + r_f \, e^{i\delta_f} \, e^{i\theta_f}
ight]$$

- δ_f : Weak Phase and θ_f : Strong phase
- Penguin-over-Tree ratio:

$$r_f = \lambda_{\text{CKM},f} a_f$$

- *a_f*: Modulus of a ratio of hadronic matrix elements
- $\lambda_{\text{CKM,f}}$: Modulus of a ratio of CKM matrix elements

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• Key Observable: Time-Dependent CP Asymmetries

$$A_{\rm CP}(t;f) \equiv \frac{\Gamma(B^0(t) \to f) - \Gamma(\bar{B}^0(t) \to f)}{\Gamma(B^0(t) \to f) + \Gamma(\bar{B}^0(t) \to f)}$$

General Expression

$$\mathcal{A}_{\rm CP}(t; f) = \frac{\mathcal{A}_{\rm D}^f \cos(\Delta M_q t) + \mathcal{A}_{\rm M}^f \sin(\Delta M_q t)}{\cosh(\Delta \Gamma_q t/2) - \mathcal{A}_{\Delta \Gamma}^f \sinh(\Delta \Gamma_q t/2)}$$

• Neglecting the lifetime difference (for the B_d)

$$A_{\rm CP}(t; f) = A^f_{\rm D} \cos(\Delta M_q t) + A^f_{\rm M} \sin(\Delta M_q t)$$

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 In terms of the parameters of the amplitude an the mixing phase φ_s

$$\begin{aligned} A_{\rm D}^{f} &= -2r_{f}\sin\theta_{f}\sin\delta_{f} \\ A_{\rm M}^{f} &= \left[\sin\phi_{s} + 2r_{f}\cos\theta_{f}\sin(\phi_{s} + \delta_{f}) + r_{f}^{2}\sin(\phi_{s} + 2\delta_{f})\right] \\ A_{\Delta\Gamma}^{f} &= \dots \text{ not needed here} \end{aligned}$$

• Golden Modes: For $B_d \rightarrow J/\psi K_s$ and $B_s \rightarrow J/\psi \phi$:

$$\lambda_{\rm CKM,f} = \left| \frac{V_{ub} V_{us}^*}{V_{cb} V_{cs}^*} \right| \sim 5\%$$

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(Bigi, Sanda)

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• Thus: In the Standard Model $r_{J/\Psi K} \leq 5\%$:

 $C(J/\psi K_{\mathrm{S,L}}) pprox \mathbf{0}, \quad S(J/\psi K_{\mathrm{S,L}}) pprox -\eta_{\mathrm{S,L}} \sin 2\beta$

- Penguin contamination small, suppressed by λ_{CKM}
- Is it really small ?
- If not, what can be the sensitivity to a new physics contribution?



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- Use of data: Employ Flavour Symmetries (M. Ciuchini, M. Pierini and L. Silvestrini, Phys. Rev. Lett. 95, 221804 (2005), S. Faller, R. Fleischer, M. Jung and T. M., Phys. Rev. D79:014030,2009.)
- Problem: Flavour SU(3) is severely broken
- Two Strategies:
 - Assume SU(3), allow for generous uncertainties
 - Try to get a hand on SU(3) breaking
- In the case at hand:

Compare $b \rightarrow s\bar{c}c$ with its SU(3) friend $b \rightarrow d\bar{c}c$

• Parametrize ($\phi_d = B - \overline{B}$ Mixing phase)

$$S(J/\Psi K_S) = \sin(\phi_d + \Delta \phi_d)$$

$$\tan \Delta \phi_{d} = \frac{2\lambda_{\rm CKM} a\cos\theta\sin\gamma + \lambda_{\rm CKM}^2 a^2\sin2\gamma}{1 + 2\lambda_{\rm CKM} a\cos\theta\cos\gamma + \lambda_{\rm CKM}^2 a^2\cos2\gamma}$$

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- Using SU(3) for *a* and θ : $\Delta \phi_d \in [-3.9, -0.8]^{\circ}$
- Allowing 50% *SU*(3) breaking in *a* and $\theta, \theta' \in [90, 270]^{\circ}$ indepedently: $\Delta \phi_d \in [-6.7, 0.0]^{\circ}$
- Hints at negative $\Delta \phi_d$
- Softens the tension with the SM fit
- However, still quite debatable SU(3) assumptions
- This is likely much larger then the perturbative estimate! (Ala Boos, Reuter, TM.)
- Also significantly larger than other estimates (e.g. Gronau Rosner 2008)

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Rare $(b \rightarrow s)$ Semileptonics

- Theory of B → K^(*)ℓ⁺ℓ⁻ is substantially different from the one for B → Dℓν̄:
- Effective Interaction:

$$egin{aligned} {\mathcal H}_{e\! f\! f} = -rac{4G_{\!F}}{\sqrt{2}} \, V_{t\!b} \, V_{t\!s}^* \! \sum_{i=1}^{10} \! C_i(\mu) O_i(\mu) \, , \end{aligned}$$

- Dominant $b \rightarrow s$ effective operators: $O_{7,9,10}$ $C_7(m_b) \simeq -0.3$, $C_9(m_b) \simeq 4.4$, $C_{10}(m_b) \simeq -4.7$
- ... can be expressed in terms of form factors

$$O_{7,9,10} \propto \langle K^{(*)}({m p}) | ar{f s} ar{m b} | B({m p}+{m q})
angle$$

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Charm Loops

Buchalla, Isidori, Feldmann, Khodjamirin, TM, Pivovarov, Wang

Charm-loop effect: a combination of the (sc)(cb) weak interaction (O_{1,2}) and e.m.interaction (cc)(ll)



new hadronic matrix elements, not a form factor

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- Light cone expansion of the charm loop
- Expansion parameter $\frac{\Lambda_{QCD}^2}{(4m_p^2 q^2)}$
- Leads to a non-local operator ("shape-function-like" operator)

$$\widetilde{\mathcal{O}}_{\mu}(\boldsymbol{q}) = \int \boldsymbol{d}\omega \ \boldsymbol{I}_{\mu
holphaeta}(\boldsymbol{q}, \boldsymbol{m_{c}}, \omega) \bar{\boldsymbol{s}}_{L} \gamma^{
ho} \left(\delta[\omega - rac{(in_{+}\mathcal{D})}{2}] \widetilde{\boldsymbol{G}}_{lphaeta}\right) \boldsymbol{b}_{L} \; ,$$

• Matrix element can be calculated in a LCSR for $q^2 \leq 0$

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Semileptonic Decays Nonleptonic Decays Rare Decays

Results on $B \to K^{(*)} \ell^+ \ell^-$



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Problem to compute above the charm threshold? Problem also below charm theshold: $B \to K\phi \to K\ell^+\ell^-$... currently under consideration Khodjamirian, Wang, TM

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Concluding Remarks

In 1993 we did not know f_B nor the top mass



Enormous Progress over the past twenty years!

... experimentally as well as theoretically

 Introduction: Why Study Flavour Physics?
 Semileptonic Decays

 Theory Tools for Precision Flavour Physics
 Nonleptonic Decays

 Achivements
 Rare Decays



Introduction: Why Study Flavour Physics? Semileptonic Decays Theory Tools for Precision Flavour Physics Achivements Rare Decays

- Yet there are a few tensions in *B* decays
- ... and an interesting hint in charm decays
- ... which may be the first glimpse of the BSM era
- Flavour Physics turns out to be a sensitive indirect probe of "new physics" if
 - we have appropriate theoretical tools at least for some interesting processes
 - we have sufficient data on all types of heavy hadrons

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• ... in particular also for charm

The discovery of the Higgs may be a triumph, but not discovering the Higgs will be a revolution

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The discovery of the Higgs may be a triumph, but Flavour Physics may initiate a revolution