

# DY PRODUCTION AT SMALL $Q_T$ AND THE COLLINEAR ANOMALY

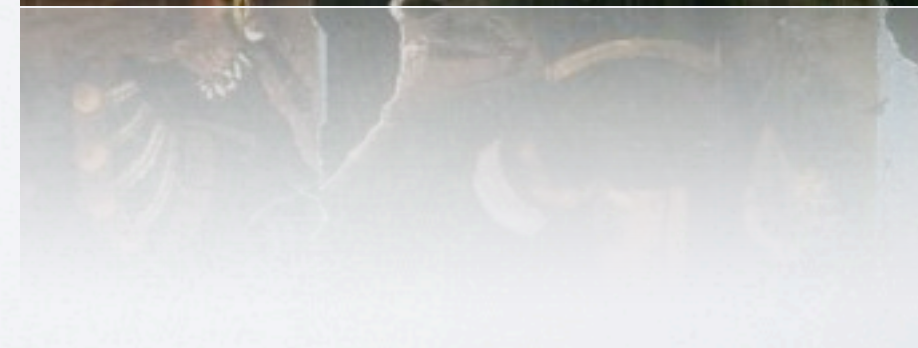
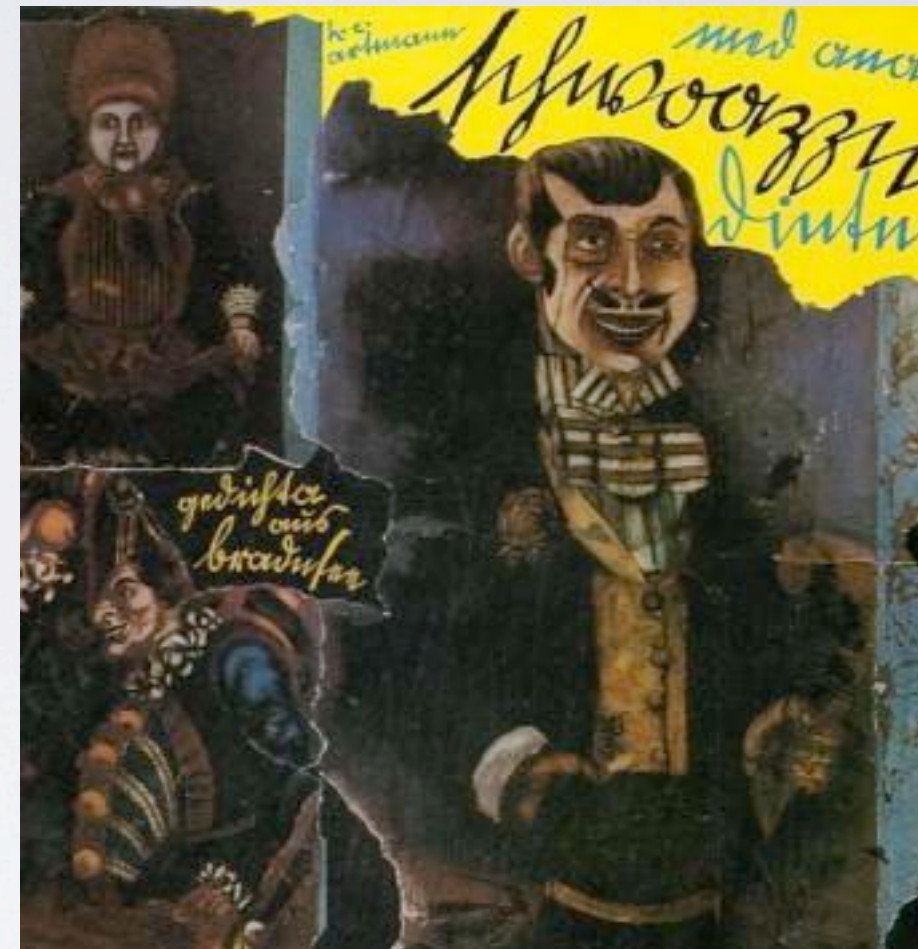
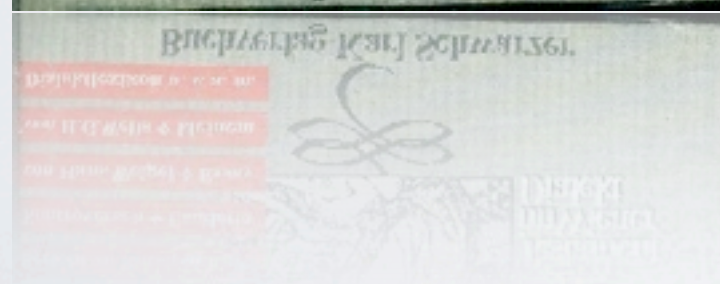
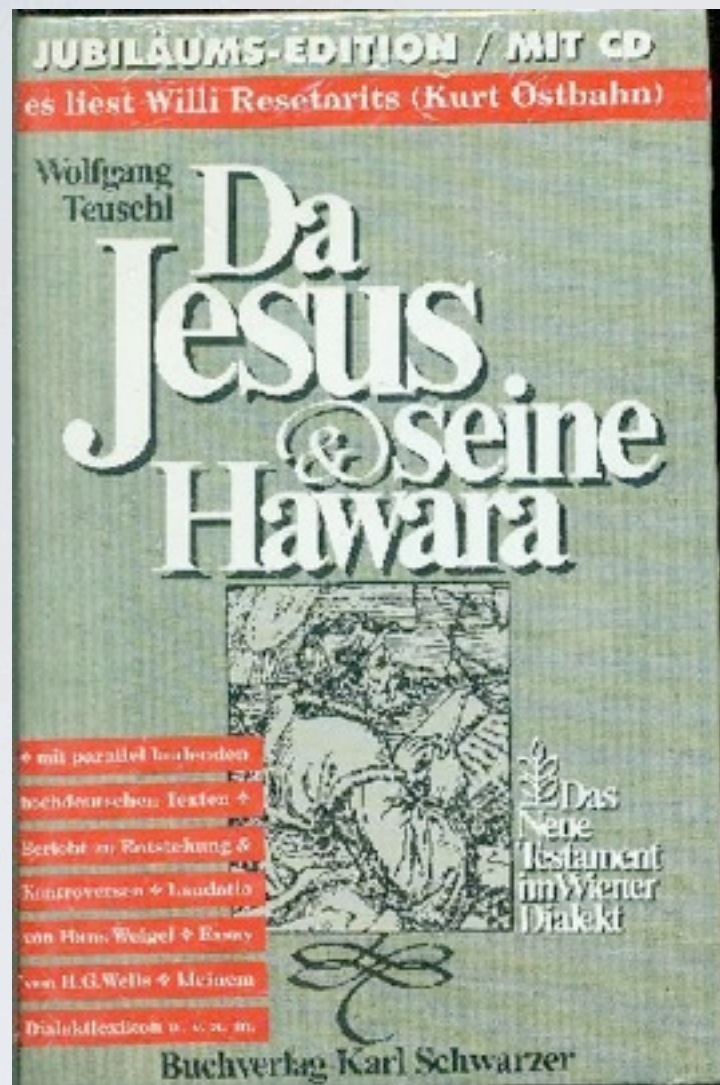
1007.4005, with Matthias Neubert | 109.6027 + Daniel Wilhelm  
| 12.3907 with Guido Bell

Thomas Becher

Universität Bern

Seminar in Wien, Jan. 12, 2012



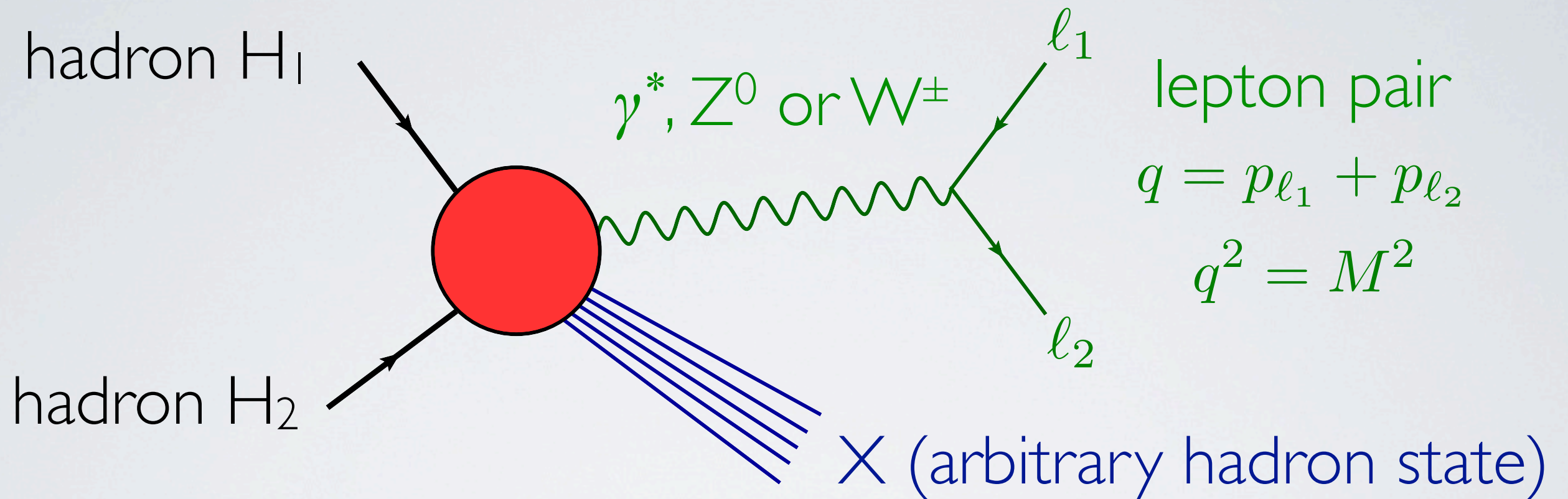




# OUTLINE

- Introduction
  - Drell-Yan process
  - Soft-Collinear Effective Theory
- Factorization at low transverse momentum  $q_T$ 
  - The collinear anomaly and the definition of transverse position dependent PDFs
  - Resummation of large log's, relation to CSS formalism
- Analytic regularization
- Expansions from hell and non-perturbative short-distance physics at low  $q_T$ . Numerical results.

# DRELL-YAN PROCESSES



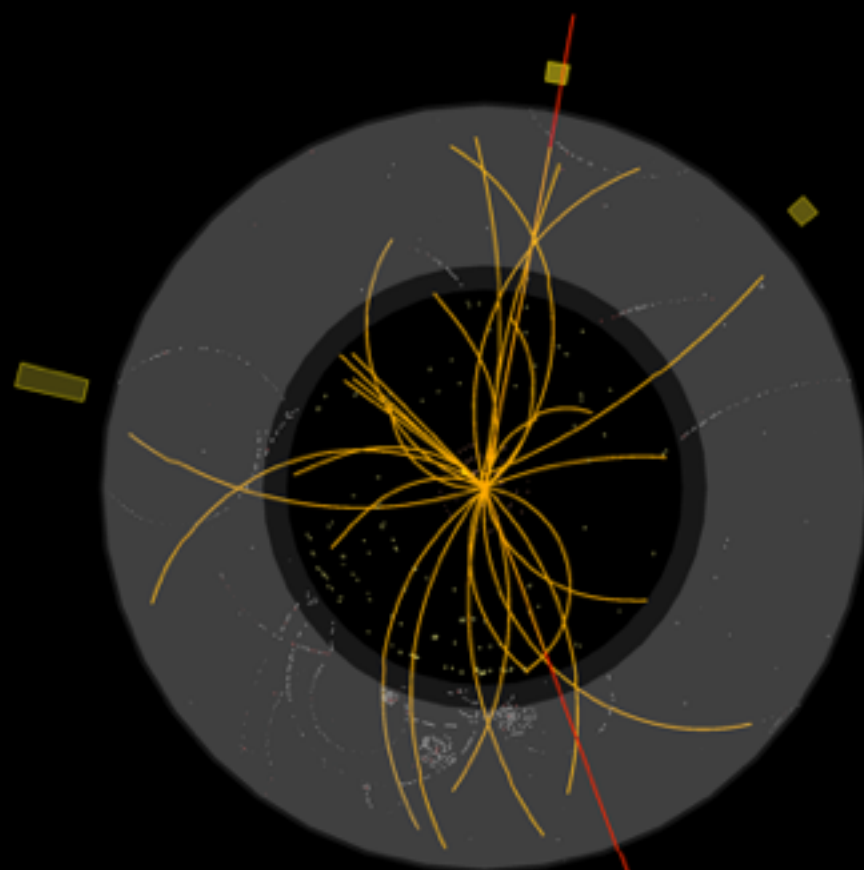
The production of a lepton pair with large invariant mass is the most basic hard-scattering process at a hadron collider.





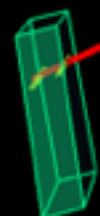
# ATLAS EXPERIMENT

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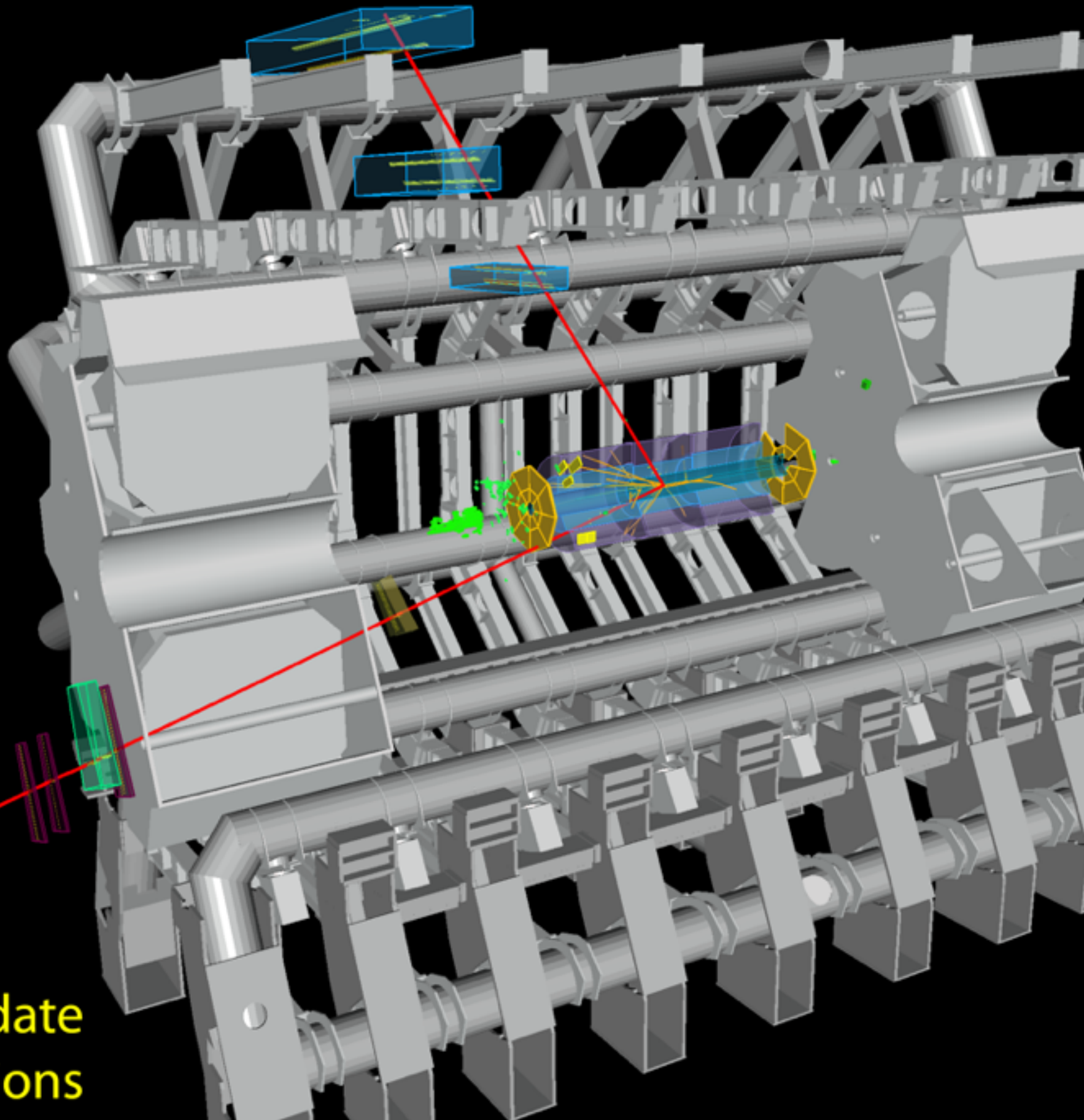


$p_T(\mu^-) = 27 \text{ GeV}$   $\eta(\mu^-) = 0.7$   
 $p_T(\mu^+) = 45 \text{ GeV}$   $\eta(\mu^+) = 2.2$

$M_{\mu\mu} = 87 \text{ GeV}$



**$Z \rightarrow \mu\mu$  candidate  
in 7 TeV collisions**



# DRELL-YAN PROCESSES

The production of a single electroweak boson  $\gamma^*, Z, W^\pm, H$  is of great interest for

- $W$  mass and width measurements,
- PDF determinations, luminosity monitoring,
- New physics searches at high  $q^2$

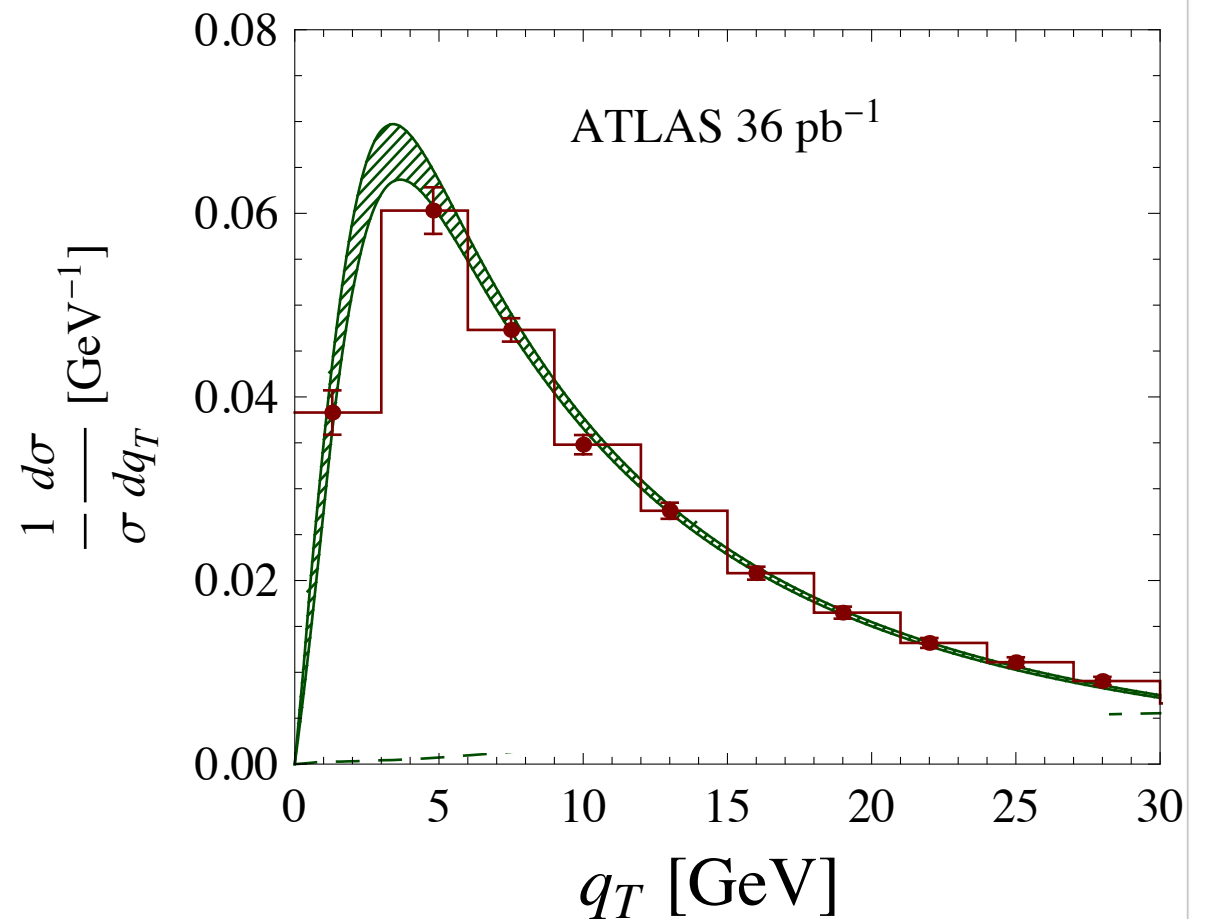
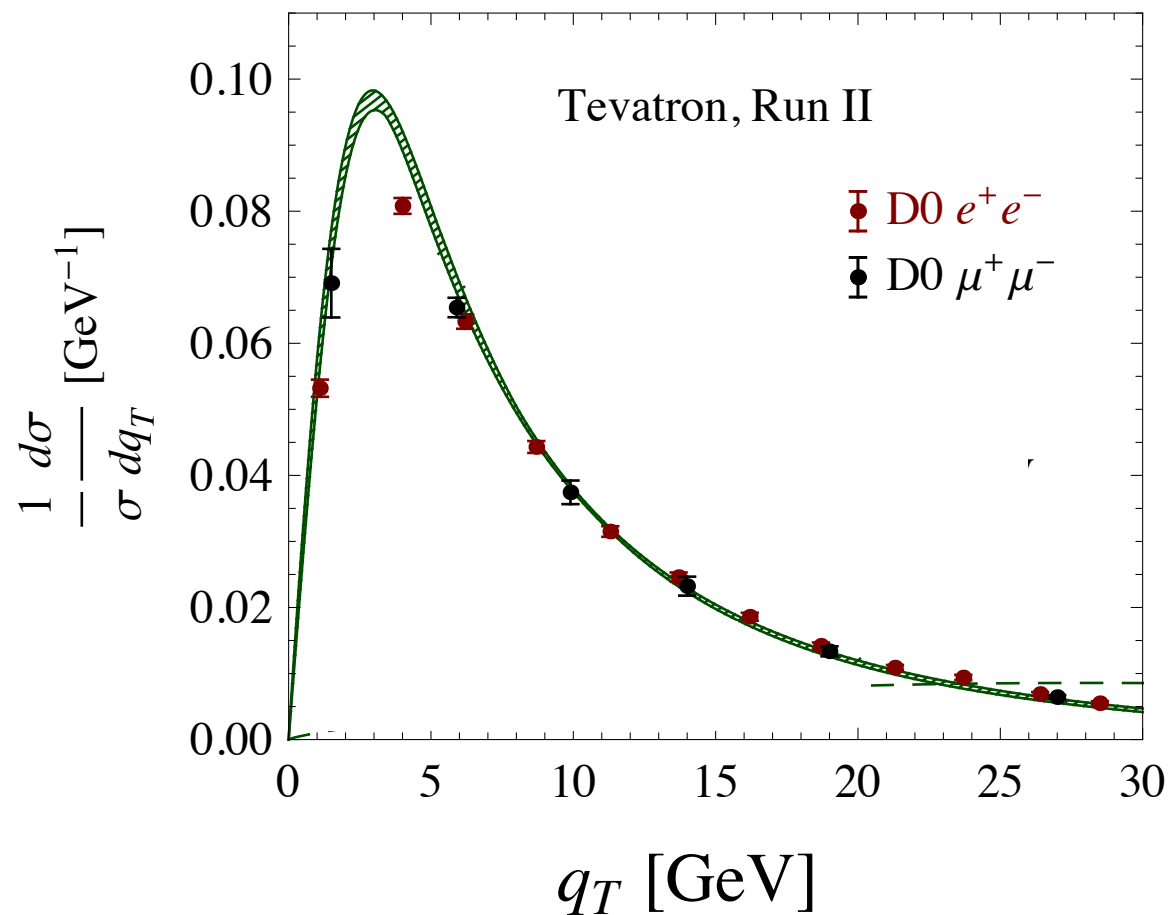
Low transverse momentum  $q_T$  is particularly relevant

- to extract  $W$  mass
- to reduce background for Higgs search



# TRANSVERSE MOMENTUM SPECTRUM

$$pp \rightarrow Z + X \rightarrow \ell^+ \ell^- + X$$



New experimental results both from Tevatron and LHC. LHC results still based on tiny fraction the  $\sim 5 \text{ fb}^{-1}$  of data .

# PERTURBATIVE EXPANSION

The perturbative expansion of the  $q_T$  spectrum contains singular terms of the form ( $M$  is the invariant mass of the lepton pair)

$$\frac{d\sigma}{dq_T^2} = \frac{1}{q_T^2} \left[ A_1^{(1)} \alpha_s \ln \frac{M^2}{q_T^2} + \alpha_s A_0^{(1)} + A_3^{(2)} \alpha_s^2 \ln^3 \frac{M^2}{q_T^2} + \dots \right. \\ \left. + A_{2n-1}^{(n)} \alpha_s^n \ln^{2n-1} \frac{M^2}{q_T^2} + \dots \right] + \dots$$

which ruin the perturbative expansion at  $q_T \ll M$  and must be resummed to all orders.

Classic example of an observable which needs resummation!  
Achieved by Collins, Soper and Sterman (CSS) '84.



# PARTY LIKE IT'S 1984

A lot of recent work on transverse momentum resummation

- Higher accuracy.
  - Computation of all singular terms at  $O(\alpha_s^2)$  accuracy. Catani and Grazzini '09, '11
  - New NNLL codes (in addition to RESBOS) Bozzi, Catani Ferrera, de Florian, Grazzini '10; TB, Neubert, Wilhelm, in preparation
  - derivation of missing NNLL coefficient  $A^{(3)}$  TB, Neubert '10
  - NNLL threshold resummation at large  $q_T$  TB, Lorentzen, Schwartz '11
- Factorization of the cross section, definition of transverse PDFs
  - using Soft-Collinear Effective Theory Mantry Petriello '09, '10; TB Neubert '10
  - traditional framework Collins '11

# SOFT-COLLINEAR EFFECTIVE THEORY

Bauer, Pirjol, Stewart et al. 2001, 2002; Beneke et al. 2002; ...

CSS used diagrammatic methods to factorize contributions with different scales, we will instead use effective field theory.

SCET has been used to perform soft gluon resummation for many processes:

- DIS at large  $x$ , Drell-Yan rapidity spectrum, inclusive Higgs production, top production, direct photon production, single top production,  $e^+e^-$  event shapes, ...

Would like to use framework to resum higher logs in multi-jet processes at hadron colliders. To do so, we first need to understand “initial state showering”.

- The  $q_T$ -spectrum in DY provides simple setting to study issue





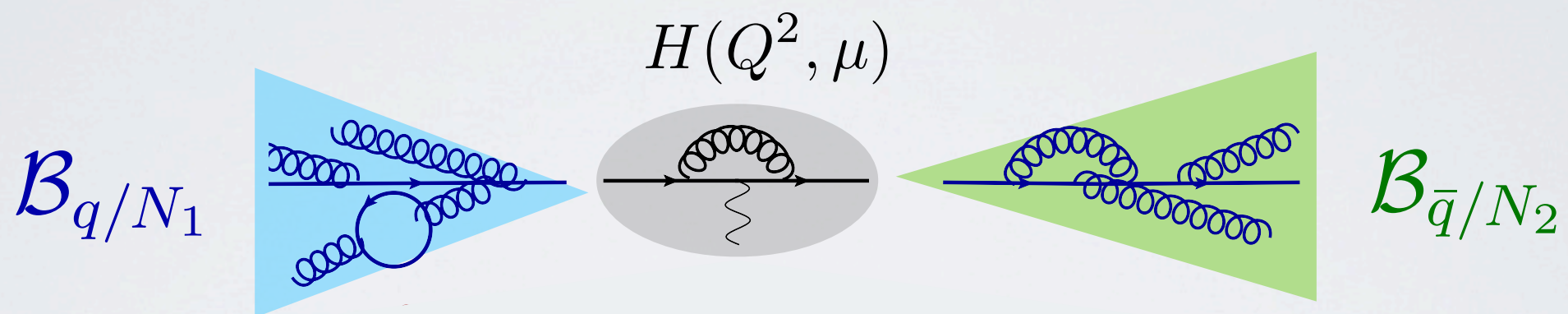
FACTORIZATION ANOMALY



# FACTORIZATION

Factorization at low  $q_T$  proceeds in two steps

1.) Use  $q_T \ll M_Z$  to factorize cross section



“hard function”  $\times$  “transverse PDF”  $\times$  “transverse PDF”

2.) Use  $\Lambda_{QCD} \ll q_T$  to factorize

$$\mathcal{B}_{i/N}(\xi, x_T^2, \mu) = \sum_j \int_{\xi}^1 \frac{dz}{z} \mathcal{I}_{i \leftarrow j}(z, x_T^2, \mu) \phi_{j/N}(\xi/z, \mu) + \mathcal{O}(\Lambda_{QCD}^2 x_T^2)$$

“transverse PDF” = “matching coefficient”  $\times$  “standard PDF”



# REGULARIZATION

Well known that transverse PDF

$$\mathcal{B}_{q/N}(z, \underset{\uparrow}{x_T^2}, \mu) = \frac{1}{2\pi} \int dt e^{-izt\bar{n}\cdot p} \langle N(p) | \bar{\chi}(t\bar{n} + \underset{\uparrow}{x_\perp}) \frac{\not{n}}{2} \chi(0) | N(p) \rangle$$

$\nwarrow \bar{n}^2 = 0$

is not defined without additional regulators.

Different possibilities

- Use non-light-like gauge [CSS '84](#)
- Keep power suppressed small light-cone component, (i.e. use “fully unintegrated PDF”) [Mantry Petriello '09](#)
- Following [Smirnov '97](#), we use analytic regulator [TB, Neubert '10; TB, Bell '11](#)
- Multiply with with strategically chosen combination of light-like and time-like Wilson lines. [Collins '11](#)

# FACTORIZATION ANOMALY

*What God has joined together, let no man separate...*

Regularization of *individual* PDFs is delicate, but the **product of PDFs is well defined** and the regulator can be removed.

However, regulator induces dependence on the the hard scale  $M$ , which remains even when the regulator is sent to zero. We prove that this **anomalous  $M$  dependence exponentiates** in the form

$$[\mathcal{B}_{q/N_1}(z_1, x_T^2, \mu) \mathcal{B}_{\bar{q}/N_2}(z_2, x_T^2, \mu)]_{M^2} = \left( \frac{x_T^2 M^2}{4e^{-2\gamma_E}} \right)^{-F_{q\bar{q}}(x_T^2, \mu)} B_{q/N_1}(z_1, x_T^2, \mu) B_{\bar{q}/N_2}(z_2, x_T^2, \mu),$$

**Anomaly:** Classically,  $\langle N_1(p) | \bar{\chi}_{hc}(x_+ + x_\perp) \not{n} \chi_{hc}(0) | N_1(p) \rangle$  is invariant under a rescaling of the momentum of the other nucleon  $N_2$ . Quantum theory needs regularization. Symmetry cannot be recovered after removing regulator. Not an anomaly of QCD, but of the low energy theory (the factorization theorem).



# FACTORIZATION ANOMALY

- RG invariance of the cross section implies presence  $M$  dependence of product of transverse PDFs. Anomaly exponent must fulfill

$$\frac{dF_{q\bar{q}}(x_T^2, \mu)}{d \ln \mu} = 2\Gamma_{\text{cusp}}^F(\alpha_s)$$

- Anomaly also affects other observables
  - Processes with small masses, e.g. EW Sudakov resummation  
Chiu, Golf, Kelley and Manohar '07
  - Jet-broadening. Have derived all-order form of anomaly for small broadening. TB, Bell, Neubert '11

# RESUMMED RESULT FOR CROSS SECTION

$$\frac{d^3\sigma}{dM^2 dq_T^2 dy} = \frac{4\pi\alpha^2}{3N_c M^2 s} \sum_q e_q^2 \sum_{i=q,g} \sum_{j=\bar{q},g} \int_{\xi_1}^1 \frac{dz_1}{z_1} \int_{\xi_2}^1 \frac{dz_2}{z_2} \\ \times \left[ C_{q\bar{q} \rightarrow ij} \left( \frac{\xi_1}{z_1}, \frac{\xi_2}{z_2}, q_T^2, M^2, \mu \right) \phi_{i/N_1}(z_1, \mu) \phi_{j/N_2}(z_2, \mu) + (q, i \leftrightarrow \bar{q}, j) \right]$$

The hard-scattering kernel is

$$C_{q\bar{q} \rightarrow ij}(z_1, z_2, q_T^2, M^2, \mu) = \underset{\downarrow}{H(M^2, \mu)} \frac{1}{4\pi} \int d^2x_\perp e^{-iq_\perp \cdot x_\perp} \left( \frac{x_T^2 M^2}{4e^{-2\gamma_E}} \right)^{\downarrow -F_{q\bar{q}}(x_T^2, \mu)} \\ \times I_{q \leftarrow i}(z_1, x_T^2, \mu) I_{\bar{q} \leftarrow j}(z_2, x_T^2, \mu)$$

- Two sources of  $M$  dependence: **hard function** and **anomaly**
- Fourier transform can be evaluated numerically or analytically, if higher-log terms are expanded out.



# RELATION TO CSS

If adopt the choice  $\mu = \mu_b = 2e^{-\gamma_E}/x_\perp$  in our result reduces to CSS formula, provided we identify (see backup slide for definition of A,B,C)

$$\begin{aligned}
 A(\alpha_s) &= \Gamma_{\text{cusp}}^F(\alpha_s) - \frac{\beta(\alpha_s)}{2} \frac{dg_1(\alpha_s)}{d\alpha_s}, \\
 B(\alpha_s) &= 2\gamma^q(\alpha_s) + g_1(\alpha_s) - \frac{\beta(\alpha_s)}{2} \frac{dg_2(\alpha_s)}{d\alpha_s}, \\
 C_{ij}(z, \alpha_s(\mu_b)) &= [H(\mu_b^2, \mu_b)]^{1/2} I_{i \leftarrow j}(z, 0, \alpha_s(\mu_b)),
 \end{aligned}
 \left| \begin{array}{l}
 \text{anomaly contribution} \\
 g_1(\alpha_s) = F(0, \alpha_s) \\
 g_2(\alpha_s) = \ln H(\mu^2, \mu)
 \end{array} \right.$$

Use these relations to derive unknown three-loop coefficient, necessary for NNLL resummation

$$A^{(3)} = \Gamma_2^F + \beta_0 g_1''(0) = 239.2 - 652.9 \neq \Gamma_2^F$$

Not equal to the cusp anom. dim. as was usually assumed!



# ANALYTIC REGULARIZATION IN SCET



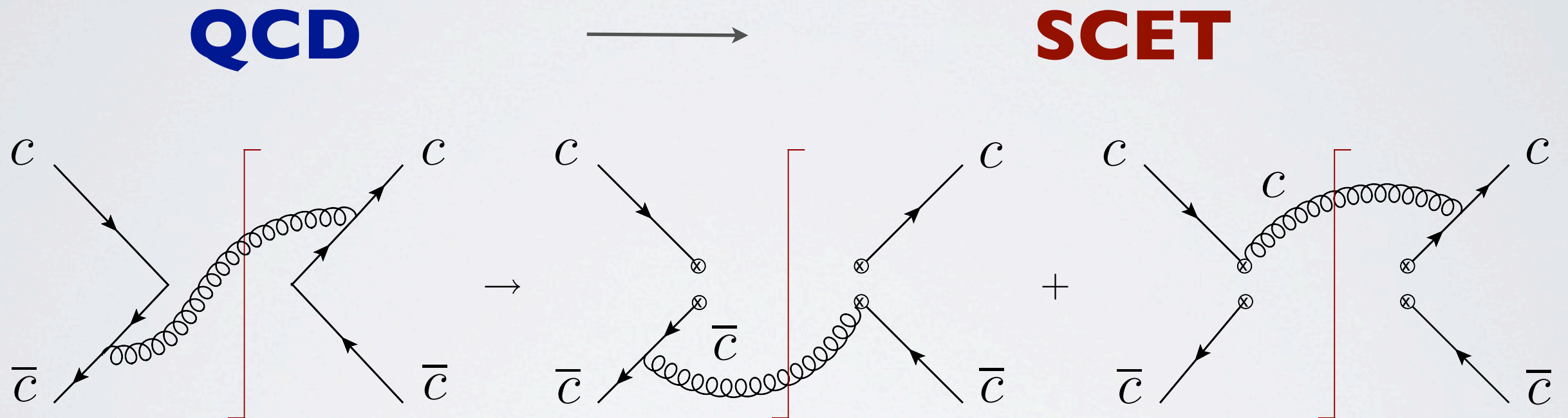
# ANALYTIC REGULARIZATION

$$\frac{1}{k^2 + i\epsilon} \longrightarrow \frac{(\nu^2)^\alpha}{(k^2 + i\epsilon)^{1+\alpha}} ,$$

- Large amount of freedom...
  - which propagators are regularized?
  - one or several regulators?
- ... but in general bad properties
  - destroys gauge invariance
  - destroys eikonal structure of soft radiation: problems in factorization proofs

# REGULARIZATION IN SCET

Original QCD diagrams are regularized dimensionally, problem only arises, when splitting the QCD result into left- and right-collinear pieces.



Need additional regulator to make both pieces separately well-defined. Can be removed in the sum.



# PHASE-SPACE REGULARIZATION

TB, Bell III 2.3907

Have presented strong arguments that regularization problems only affect real-emissions:

- In massless loop diagrams regularization dim. reg. regularization of transverse directions regularizes also light-cone integrations.

$$k_\mu = k_+ \frac{\bar{n}^\mu}{2} + k_- \frac{n^\mu}{2} + k_\perp^\mu$$

$$n^2 = \bar{n}^2 = 0 \quad n \cdot \bar{n} = 2$$

- In phase-space integrals constraints on the transverse momentum can lead to unregularized integrals over light-cone directions.

# PHASE-SPACE REGULARIZATION

Have shown that the following prescription regularizes these singularities:

$$\int d^d k \, \delta(k^2) \, \theta(k^0) \quad \Rightarrow \quad \int d^d k \, \left( \frac{\nu_+}{k_+} \right)^\alpha \delta(k^2) \, \theta(k^0)$$

Since the amplitudes themselves do not need additional regularization,

- gauge invariance is maintained
- structure of the effective is unchanged

Divergences in  $\alpha$  cancel when the contributions from the different sectors of SCET are combined.



# RESULT FOR MATCHING

Taking first  $\alpha \rightarrow 0$ , then  $\epsilon \rightarrow 0$ , one finds ( $L_\perp = \ln \frac{x_T^2 \mu^2}{4e^{-2\gamma_E}}$ )

$$\mathcal{I}_{q \leftarrow q}(z, x_T^2, \mu) = \delta(1-z) - \frac{C_F \alpha_s}{2\pi} \left\{ \left( \frac{1}{\epsilon} + L_\perp \right) \left[ \left( \frac{2}{\alpha} + 2 \ln \frac{\nu_+ M}{\mu^2} \right) \delta(1-z) + \frac{1+z^2}{(1-z)_+} \right] \right. \\ \left. + \delta(1-z) \left( -\frac{2}{\epsilon^2} + L_\perp^2 + \frac{\pi^2}{6} \right) - (1-z) \right\}$$

$$\mathcal{I}_{\bar{q} \leftarrow \bar{q}}(z, x_T^2, \mu) = \delta(1-z) - \frac{C_F \alpha_s}{2\pi} \left\{ \left( \frac{1}{\epsilon} + L_\perp \right) \left[ \left( -\frac{2}{\alpha} - 2 \ln \frac{\nu_+}{M} \right) \delta(1-z) \right. \right. \\ \left. \left. + \frac{1+z^2}{(1-z)_+} \right] - (1-z) \right\}$$

In the product the  $1/\alpha$  divergences vanish, but **anomalous  $M^2$  dependence** remains.



# DIVERGENT EXPANSIONS, AND OTHER SURPRISES



# TRANSVERSE MOMENTUM SPECTRUM

The spectrum has a number of quite remarkable features which we now discuss in turn:

- Expansion in  $\alpha_s$  : strong factorial divergence
- $q_T$ -spectrum:
  - calculable, even near  $q_T = 0$
  - expansion around  $q_T = 0$  : extremely divergent
- Long-distance effects associated with  $\Lambda_{\text{QCD}}$ 
  - small, but OPE breaks down

# LEADING MOMENTUM DEPENDENCE

Up to corrections suppressed by powers of  $\alpha_s$ , the  $q_T$ -dependence of our formula result has the form

$$\frac{1}{4\pi} \int d^2 x_\perp e^{-i q_\perp \cdot x_\perp} e^{-\eta L_\perp - \frac{1}{4} a L_\perp^2} \equiv \frac{e^{-2\gamma_E}}{\mu^2} K\left(\eta, a, \frac{q_T^2}{\mu^2}\right)$$

with  $L_\perp = \ln \frac{x_T^2 \mu^2}{4e^{-2\gamma_E}}$ , and the two quantities

$$\eta = \frac{C_F \alpha_s}{\pi} \ln \frac{M^2}{\mu^2} = \mathcal{O}(1) \quad a = \alpha_s(\mu) \times \mathcal{O}(1)$$

Since  $a$  is suppressed one can try to expand  $K$  in it.



# FACTORIAL DIVERGENCE

Unfortunately, the series in  $a$  is strongly factorially divergent:

$$K(\eta, a, 1)|_{\text{exp}} = \sum_{n=0}^{\infty} \frac{(2n)!}{n!} \left(-\frac{a}{4}\right)^n \left[ \frac{1}{(1-\eta)^{2n+1}} - e^{-2\gamma_E} \right] + \dots$$

first noted by Frixione, Nason, Ridolfi '99

Can Borel resum it, which makes the nonperturbative and highly nontrivial  $a$  dependence explicit

$$K(\eta, a, 1)|_{\text{Borel}} = \sqrt{\frac{\pi}{a}} \left\{ e^{\frac{(1-\eta)^2}{a}} \left[ 1 - \text{Erf} \left( \frac{1-\eta}{\sqrt{a}} \right) \right] - e^{-2\gamma_E + \frac{1}{a}} \left[ 1 - \text{Erf} \left( \frac{1}{\sqrt{a}} \right) \right] \right\} + \dots$$

In practice, it is simplest, to use the exact expression and evaluate  $K$ -function numerically.

# VERY LOW $Q_T$

For moderate  $q_T$ , the natural scale choice is  $\mu = q_T$ .  
However, detailed analysis shows that near  $q_T \approx 0$  the Fourier integral is dominated by

$$\langle x_T^{-1} \rangle = q_* = M \exp \left( -\frac{\pi}{2C_F \alpha_s(q_*)} \right) = 1.9 \text{ GeV for } M = M_Z$$

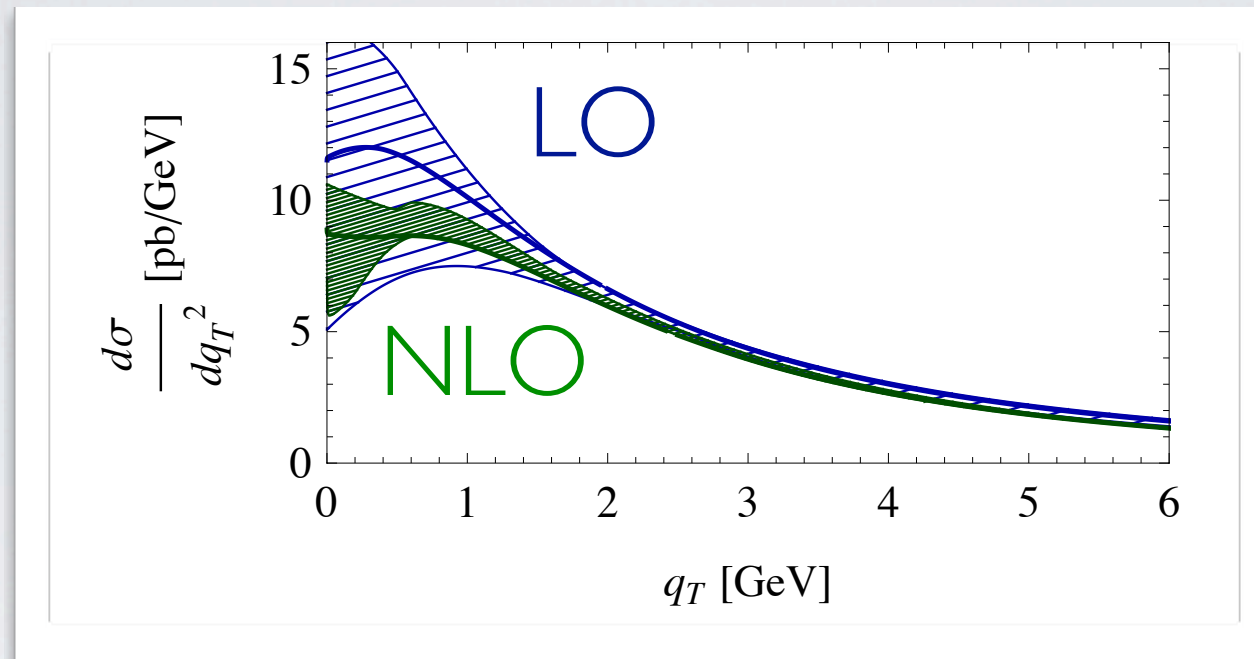
which corresponds to  $\eta=1$ .

→ Spectrum can be computed with short-distance methods down to  $q_T=0$ !



# INTERCEPT AT $Q_T=0$

$$\frac{d\sigma}{dq_T^2}$$



bands from  
scale-variation  
by factor 2

- Dedicated analysis of  $q_T \rightarrow 0$  limit yields:

$$\frac{d\sigma}{dq_T^2} \sim \frac{\mathcal{N}}{\sqrt{\alpha_s}} e^{-\#/\alpha_s} (1 + c_1 \alpha_s + \dots)$$

Parisi, Petronzio 1979;  
Collins, Soper, Sterman 1985; Ellis, Veseli 1998

- Essential singularity at  $\alpha_s=0$  ! We have computed the normalization  $\mathcal{N}$  and NLO coefficient  $c_1$  .

# SLOPE AT $Q_T=0$ ?

Given our result for the intercept, we can also try to obtain derivatives with respect to  $q_T^2$ . Leading term is obtained by expanding

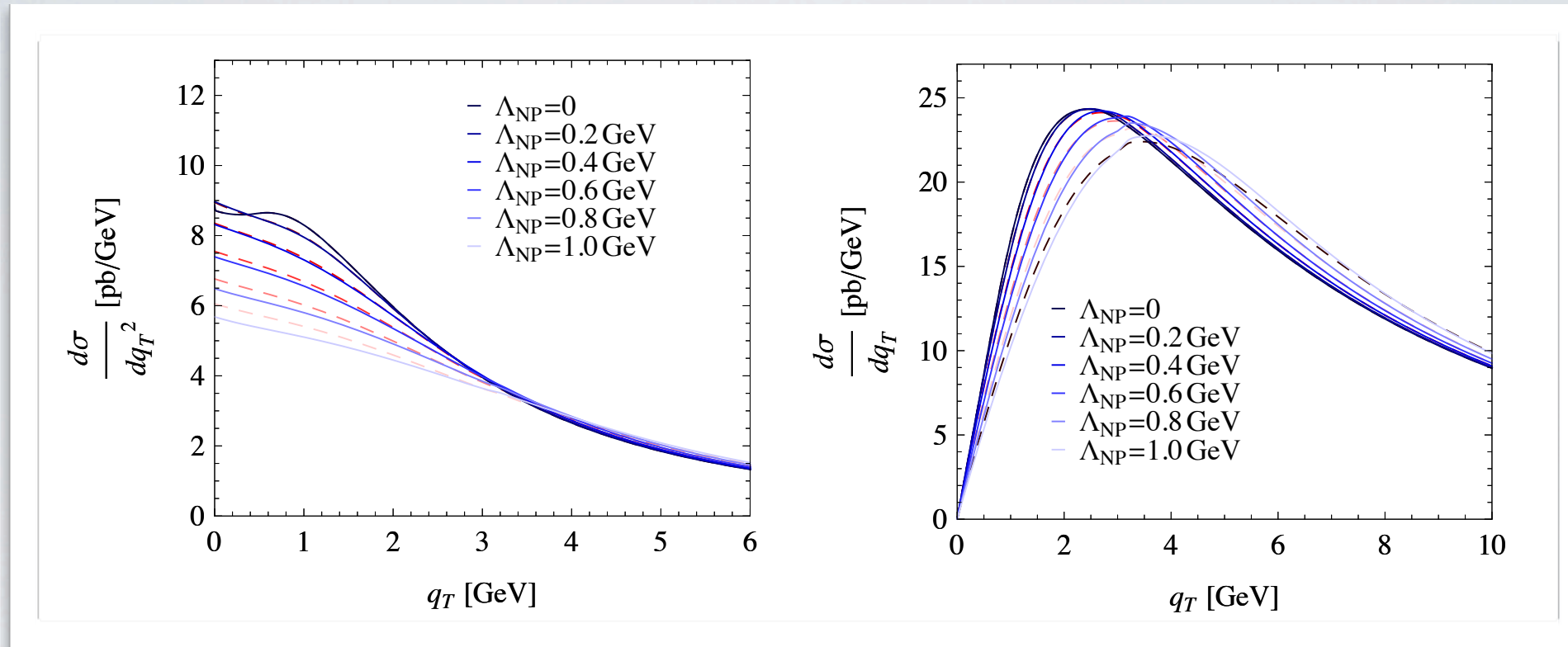
$$\frac{1}{4\pi} \int d^2 x_{\perp} e^{-i q_{\perp} \cdot x_{\perp}} e^{-\eta L_{\perp} - \frac{1}{4} a L_{\perp}^2} \equiv \frac{e^{-2\gamma_E}}{\mu^2} K\left(\eta, a, \frac{q_T^2}{\mu^2}\right)$$

Yields violently divergent series

$$K(\eta = 1, a, q_T) \big|_{\text{exp}} \sim \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{\sqrt{a}} e^{n^2/a} \left(\frac{q_T^2}{q_*^2}\right)^{n-1}$$



# NON-PERTURBATIVE EFFECTS



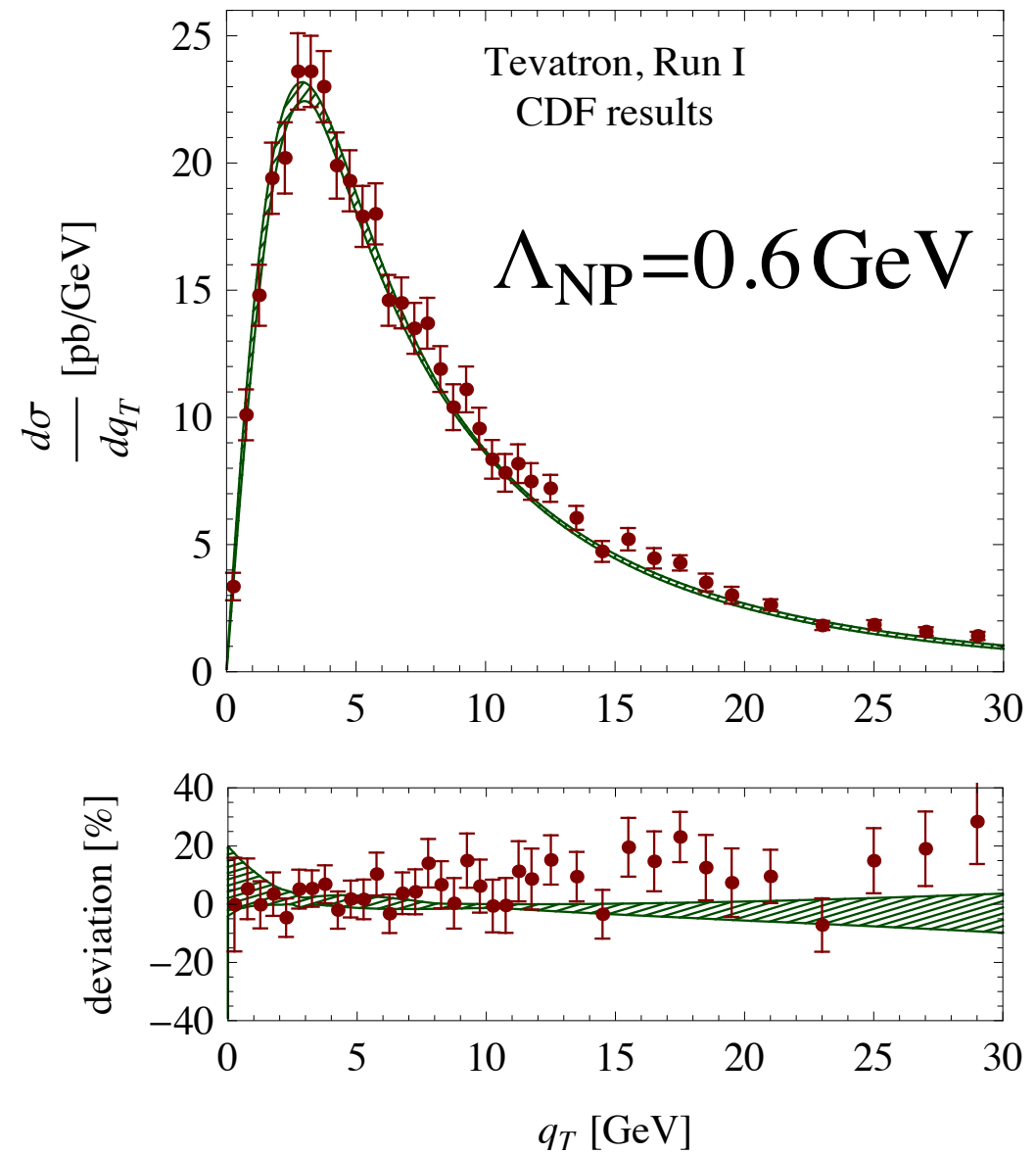
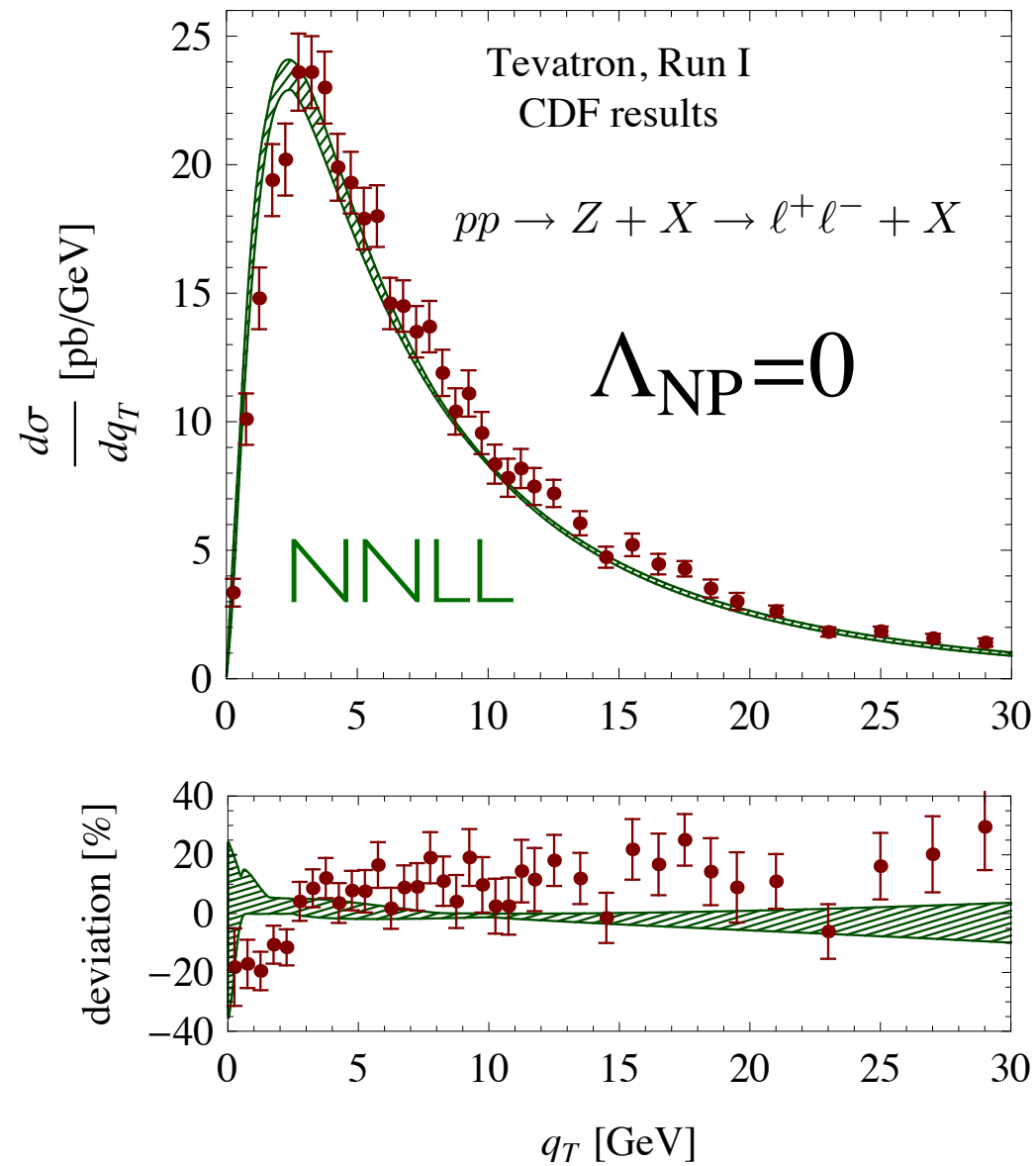
$$B_{q/N}(\xi, x_T^2, \mu) = f_{\text{hadr}}(x_T \Lambda_{\text{NP}}) B_{q/N}^{\text{pert}}(\xi, x_T^2, \mu)$$

- Blue curves: Gaussian cutoff, red dashed lines: dipole cutoff.

$$f_{\text{hadr}}^{\text{gauss}}(x_T \Lambda_{\text{NP}}) = \exp(-\Lambda_{\text{NP}}^2 x_T^2), \quad f_{\text{hadr}}^{\text{pole}}(x_T \Lambda_{\text{NP}}) = \frac{1}{(1 + \frac{1}{2} \Lambda_{\text{NP}}^2 x_T^2)}$$

- Slight shift of the peak, largely independent of the form of the cutoff

# TEVATRON, RUN I



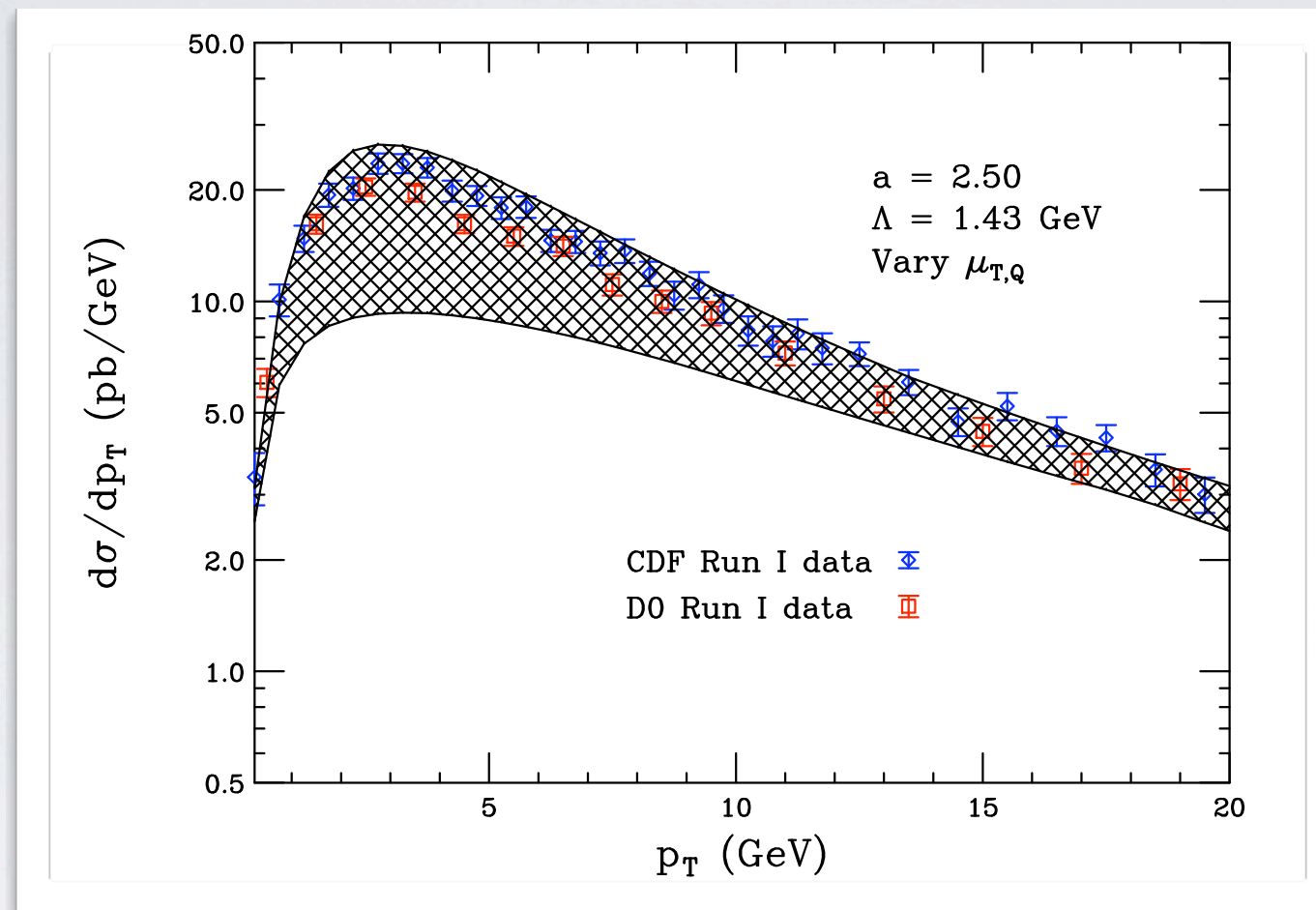
TB, Neubert, Wilhelm, I 09.6027

- Scale variation by factor of 2 from default  $\mu = q_* + q_T$ .



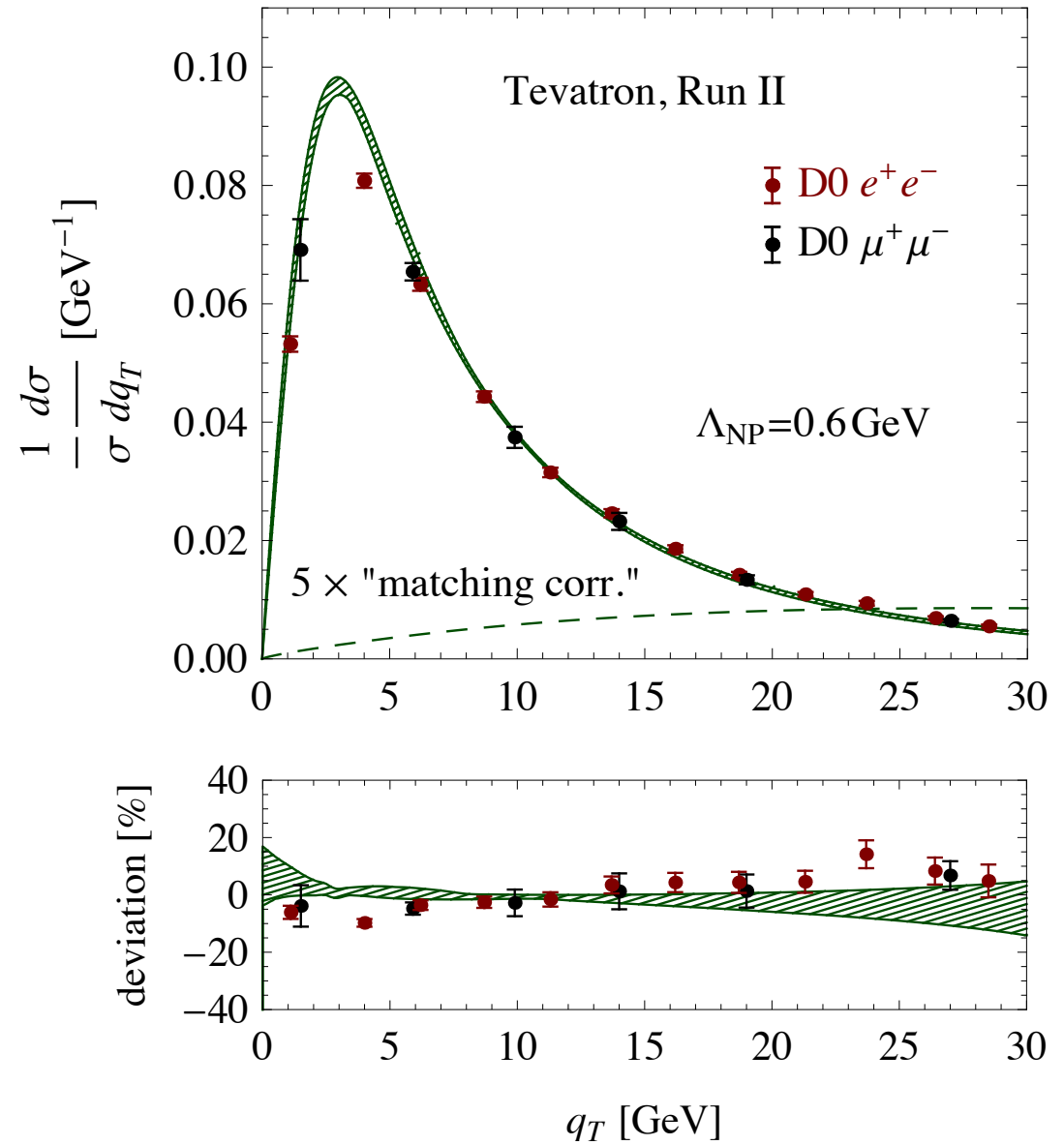
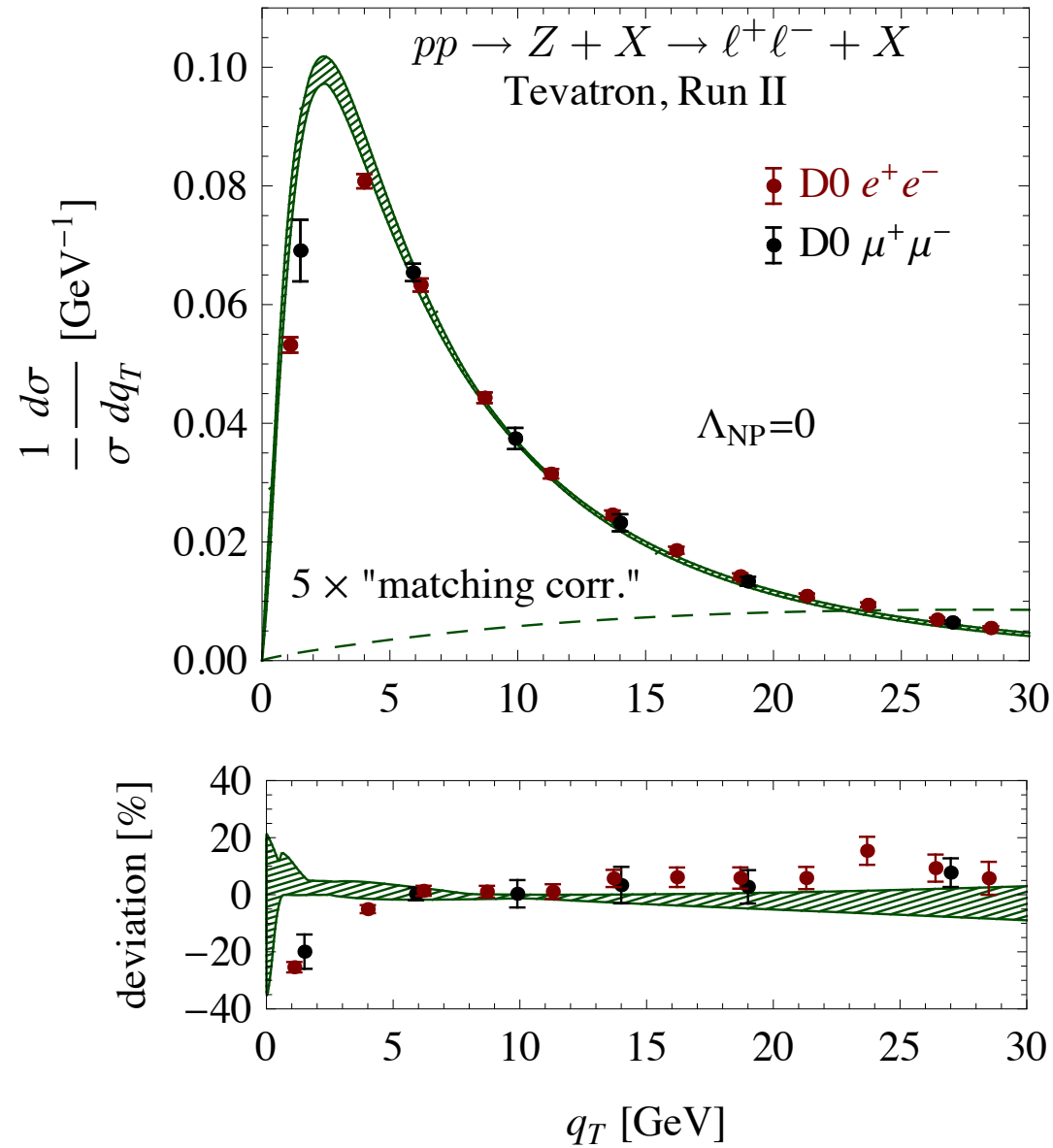
# MANTRY AND PETRIELLO

09|1.4|35, 1007.3773, 10|1.0757



- Include NP corrections. Scales are varied by a factor  $\sqrt{2}$
- Do not exponentiate anomalous log's: NLL in *amplitude*, LL in exponent.

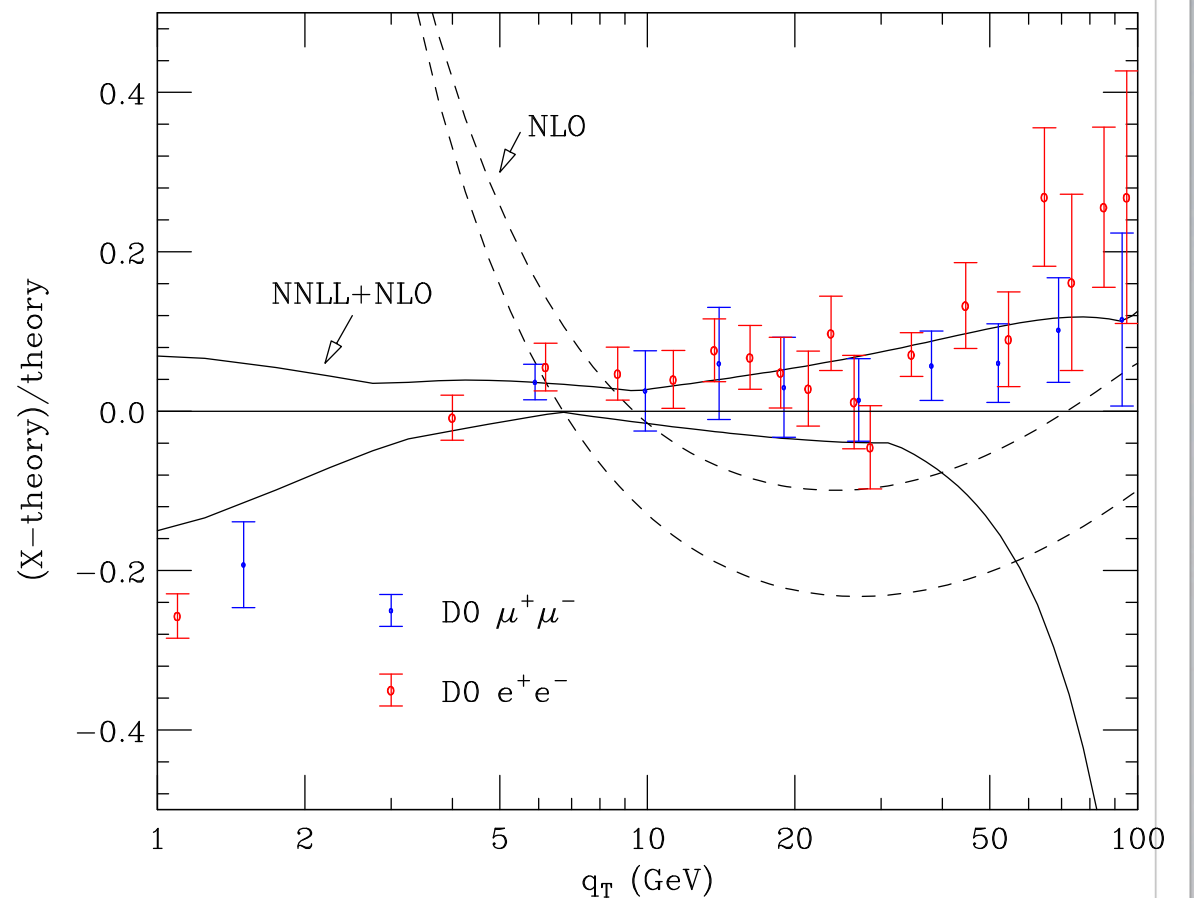
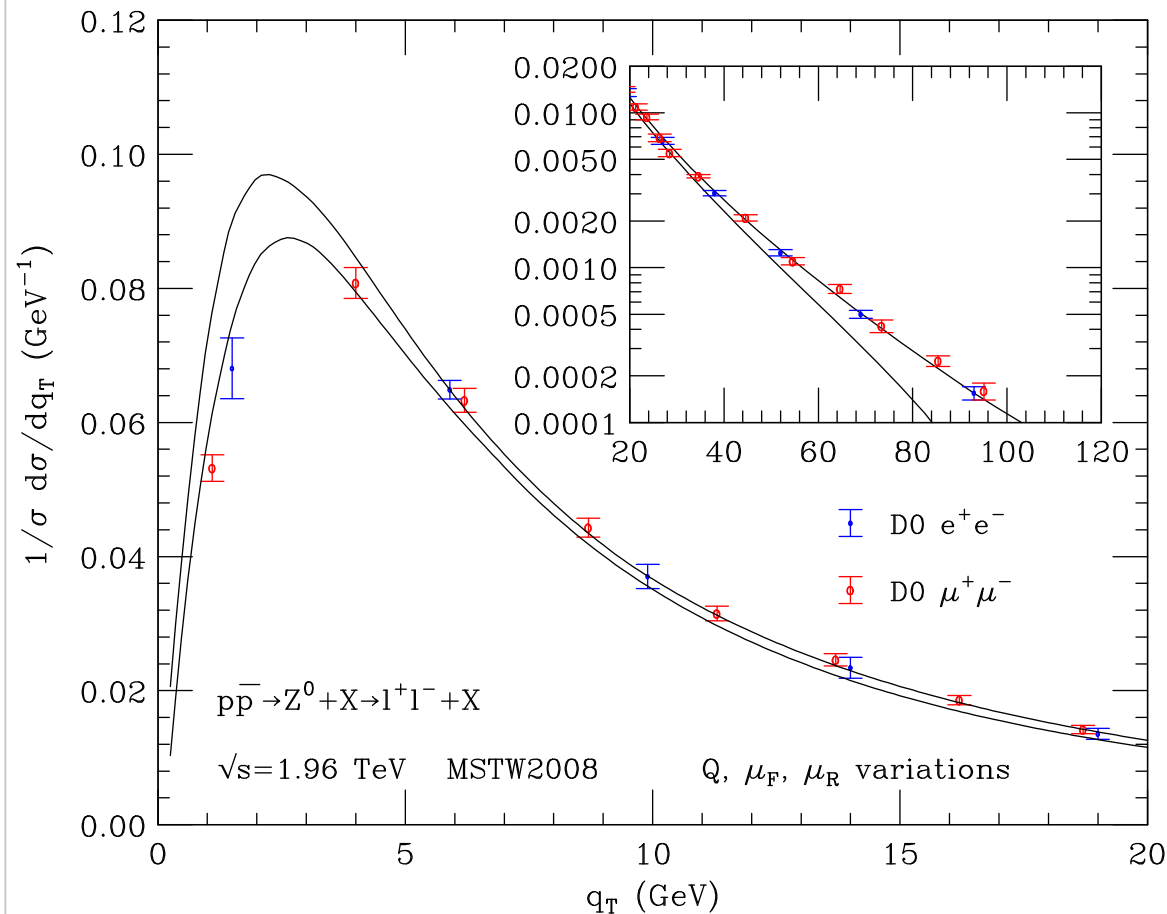
# D0, RUN II



- Correction from matching to  $\mathcal{O}(\alpha_s)$  fixed order result at has been multiplied by 5; is negligible in peak region.



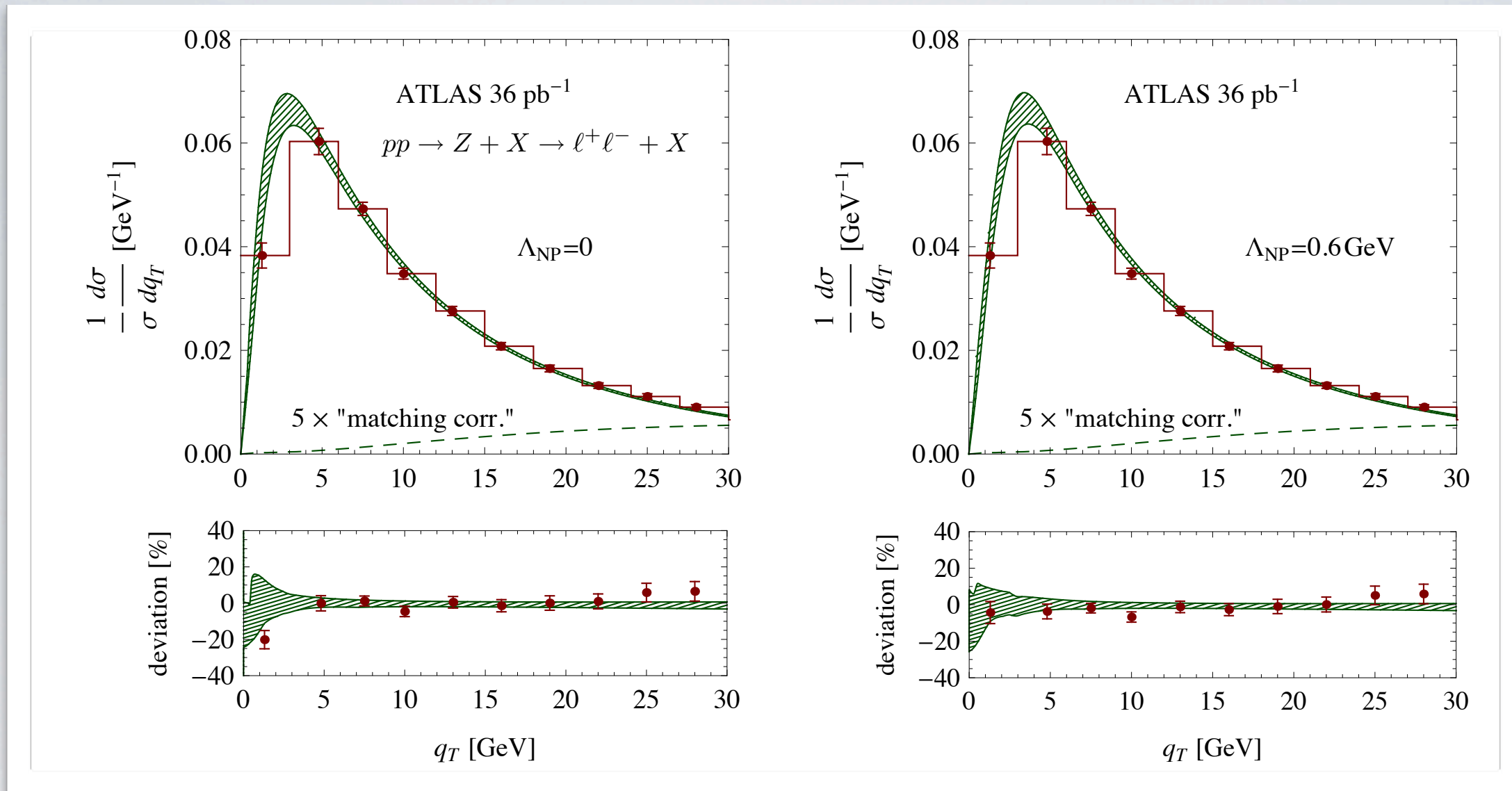
# BOZZI ET AL.



Bozzi, Catani, Ferrera, de Florian, Grazzini '10

- Nice agreement with our result within uncertainties (same peak position, our peak is 6% higher, tail about 4% lower).
- Do not use non-perturbative parameter.

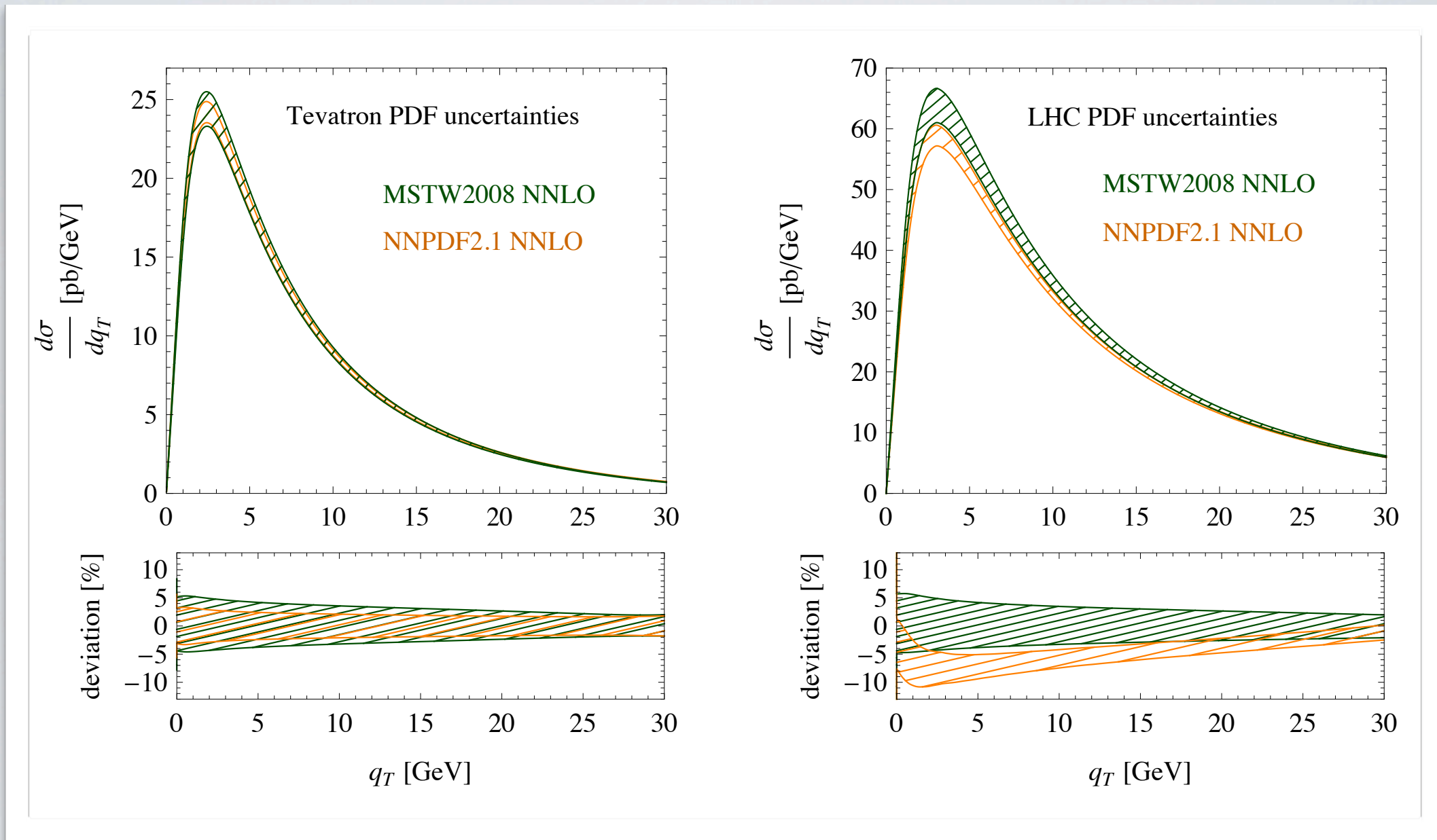
# ATLAS RESULTS



- Same non-perturbative parameter as at the Tevatron. Need finer binning for clear evidence for non-perturbative effects.
- ATLAS data (and thus also our results) agree well with RESBOS.
- Preliminary CMS result is available as well, but only with lepton cuts.



# PDF UNCERTAINTIES



- 90% C.L. for MSTW;  $1\sigma$  band for NNPDF

# LARGE $Q_T$

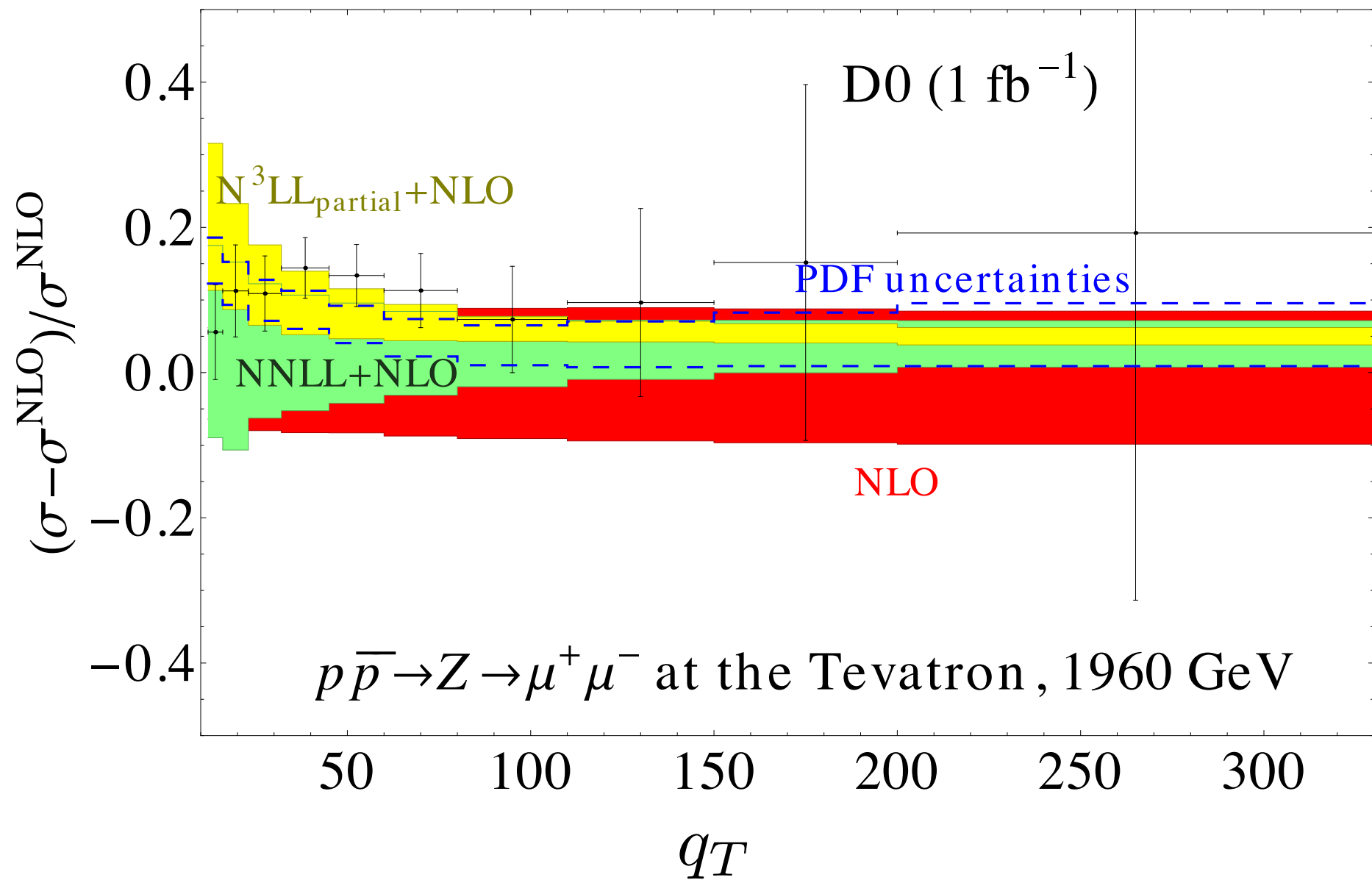
- Focussed here on low  $q_T$  , but one can also perform threshold resummation for  $q_T$  spectrum [or joint - threshold and  $q_T$  - see [Kulesza et al. '02](#)].
- Mostly relevant at large  $q_T$ : due to the fall-off of the PDFs, very high- $q_T$   $W$ 's and  $Z$ 's are mostly produced near threshold.
- Factorization theorem:

$$\frac{d\hat{\sigma}_I}{d\hat{s} d\hat{t}} = \hat{\sigma}_I^B(\hat{s}, \hat{t}) H_I(\hat{s}, \hat{t}, M_V, \mu) \times \int dk J_I(m_X^2 - 2E_J k) S_I(k, \mu),$$



# RESUMMATION TO NNLL

- Have all the necessary input for NNLL resummation and
- almost of the input for N<sup>3</sup>LL
  - All necessary anomalous dimensions [Becher, Schwartz '09](#).
    - Hard anomalous dimension follows from general results of [Magnea, Gardi '09](#) and [TB, Neubert '09](#)
  - Two-loop quark [TB, Neubert '06](#) and gluon [TB, Bell '10](#) jet functions
  - Logarithmic part of two-loop hard and soft functions



TB, Lorentzen, Schwartz, 1106.4310

Moderate shift of the central value, but much reduced scale dependence, below PDF uncertainty.



# SUMMARY

- Renewed interest in transverse momentum spectrum. Many surprising features
  - soft-collinear factorization broken by an anomaly,
  - product of two transverse PDFs can be defined without additional regulator, but has anomalous dependence on hard momentum transfer
  - emergence of nonperturbative scale  $q_* \sim 2\text{GeV}$ : spectrum is short-distance dominated, even at very low  $q_T$
  - strongly divergent expansions in  $\alpha_s$ ,  $q_T/q_*$ ,  $\Lambda_{\text{QCD}}/q_*$ .
- Three-loop coefficient  $A^{(3)}$ , the last missing piece needed for NNLL accuracy.
- NNLL results compare well with LHC data. It would be nice to have finer binning in the peak region to study non-perturbative effects.

EXTRA SLIDES

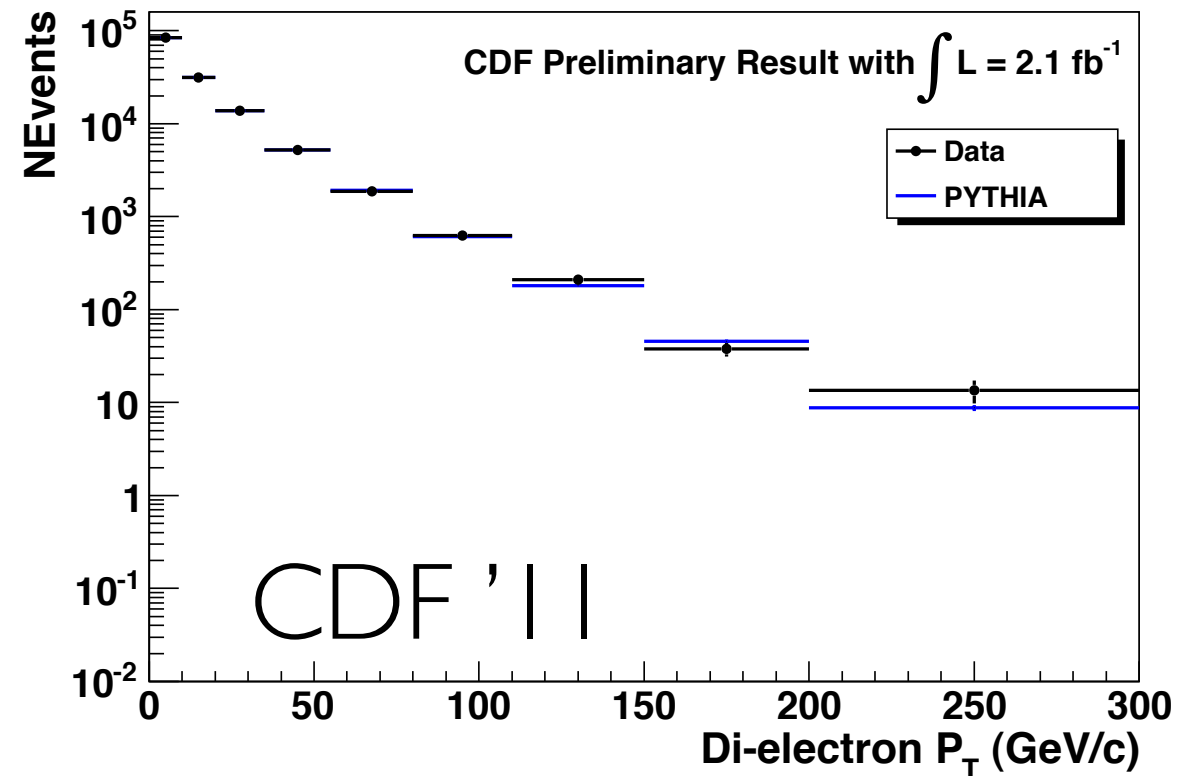
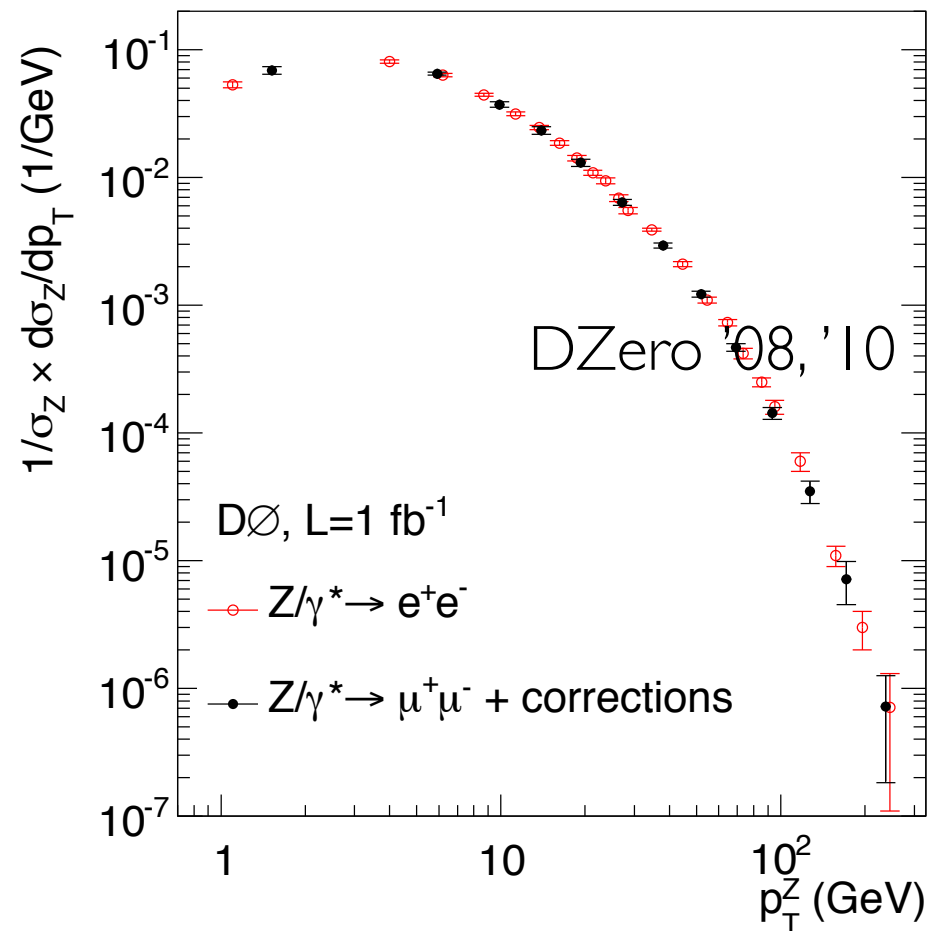


# COLLINS SOPER STERMAN FORMULA

$$\begin{aligned}
 \frac{d^3\sigma}{dM^2 dq_T^2 dy} &= \frac{4\pi\alpha^2}{3N_c M^2 s} \frac{1}{4\pi} \int d^2x_\perp e^{-iq_\perp \cdot x_\perp} \sum_q e_q^2 \sum_{i=q,g} \sum_{j=\bar{q},g} \int_{\xi_1}^1 \frac{dz_1}{z_1} \int_{\xi_2}^1 \frac{dz_2}{z_2} \\
 &\times \exp \left\{ - \int_{\mu_b^2}^{M^2} \frac{d\bar{\mu}^2}{\bar{\mu}^2} \left[ \ln \frac{M^2}{\bar{\mu}^2} A(\alpha_s(\bar{\mu})) + B(\alpha_s(\bar{\mu})) \right] \right\} \\
 &\times \left[ C_{qi}(z_1, \alpha_s(\mu_b)) C_{\bar{q}j}(z_2, \alpha_s(\mu_b)) \phi_{i/N_1}(\xi_1/z_1, \mu_b) \phi_{j/N_2}(\xi_2/z_2, \mu_b) + (q, i \leftrightarrow \bar{q}, j) \right]
 \end{aligned}$$

- The low scale is  $\mu_b = b_0/x_T$ , and we set  $b_0 = 2e^{-\gamma_E}$ .
- Landau-pole singularity in the Fourier transform. To use the formula, one needs additional prescription to deal with this.

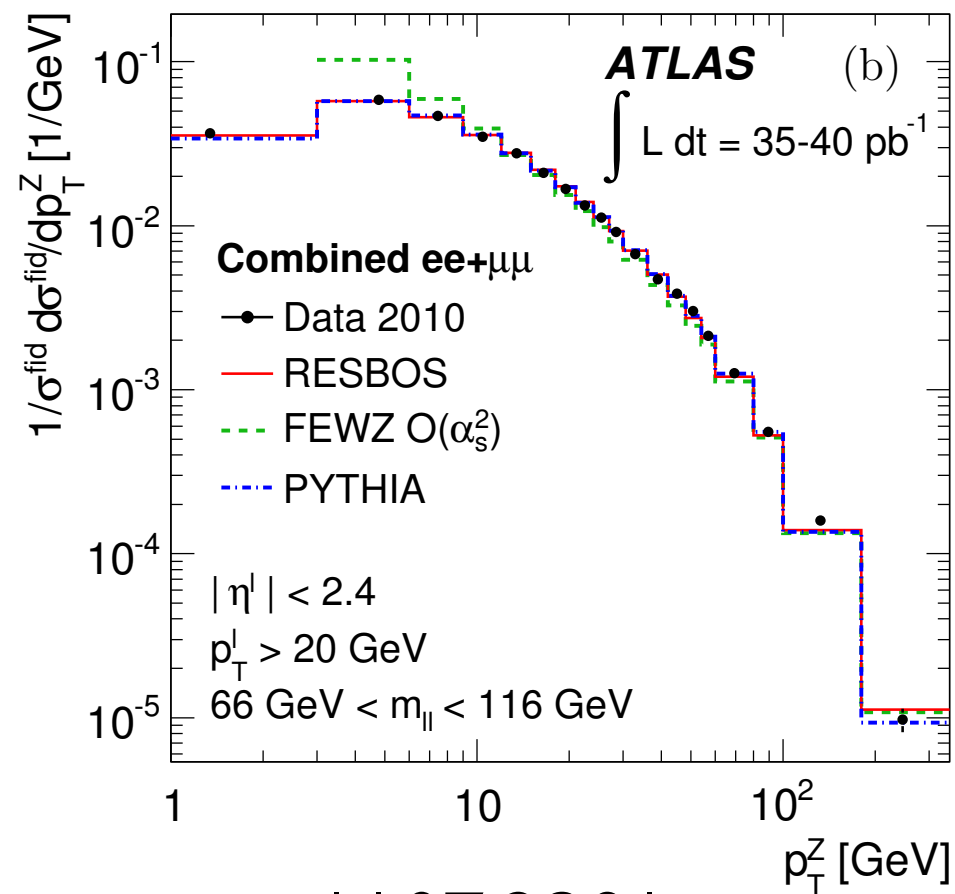
# Z-PRODUCTION AT THE TEVATRON



- 80% of all events have  $q_T < 16$  GeV, where resummation is necessary.



# NEW LHC RESULTS FOR Z-SPECTRUM



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